global SMEFT fit at e+e- Higgs factories

Barklow, Fujii, Jung, Peskin, JT, et al,
arXiv:1708.09079, 1708.08912;

+ ongoing work, paper in preparation

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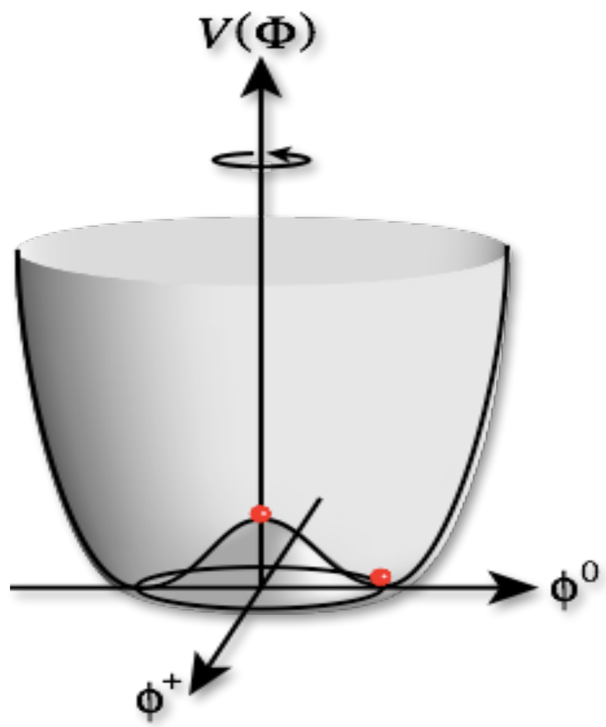
outline

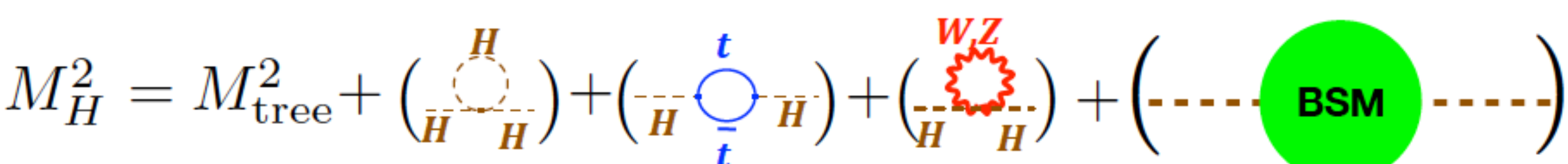
- Motivation & introduction to future e+e-
- SMEFT formalism and global fit strategy
- Highlight a few important implications
- Some ongoing work & open questions
- summary

mystery in Electroweak Symmetry Breaking

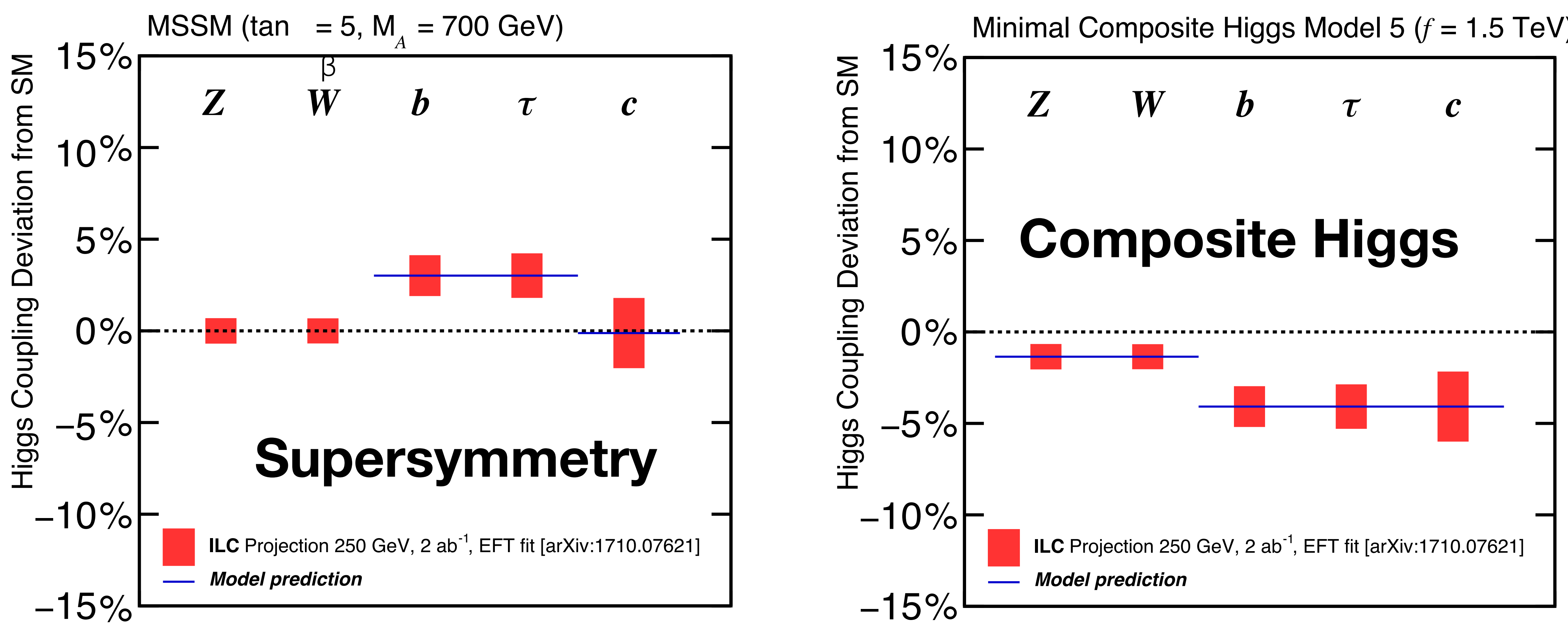
$$V(|\Phi|) = \mu^2 \Phi^\dagger \Phi + \lambda (\Phi^\dagger \Phi)^2$$



- H(125) discovery
  - elementary or composite? any siblings?
- What is the origin of EWSB?
  - why $\mu^2 < 0$? underlying dynamics?
- What BSM protects m_H?
- Connection to Dark Sector? Baryogenesis?



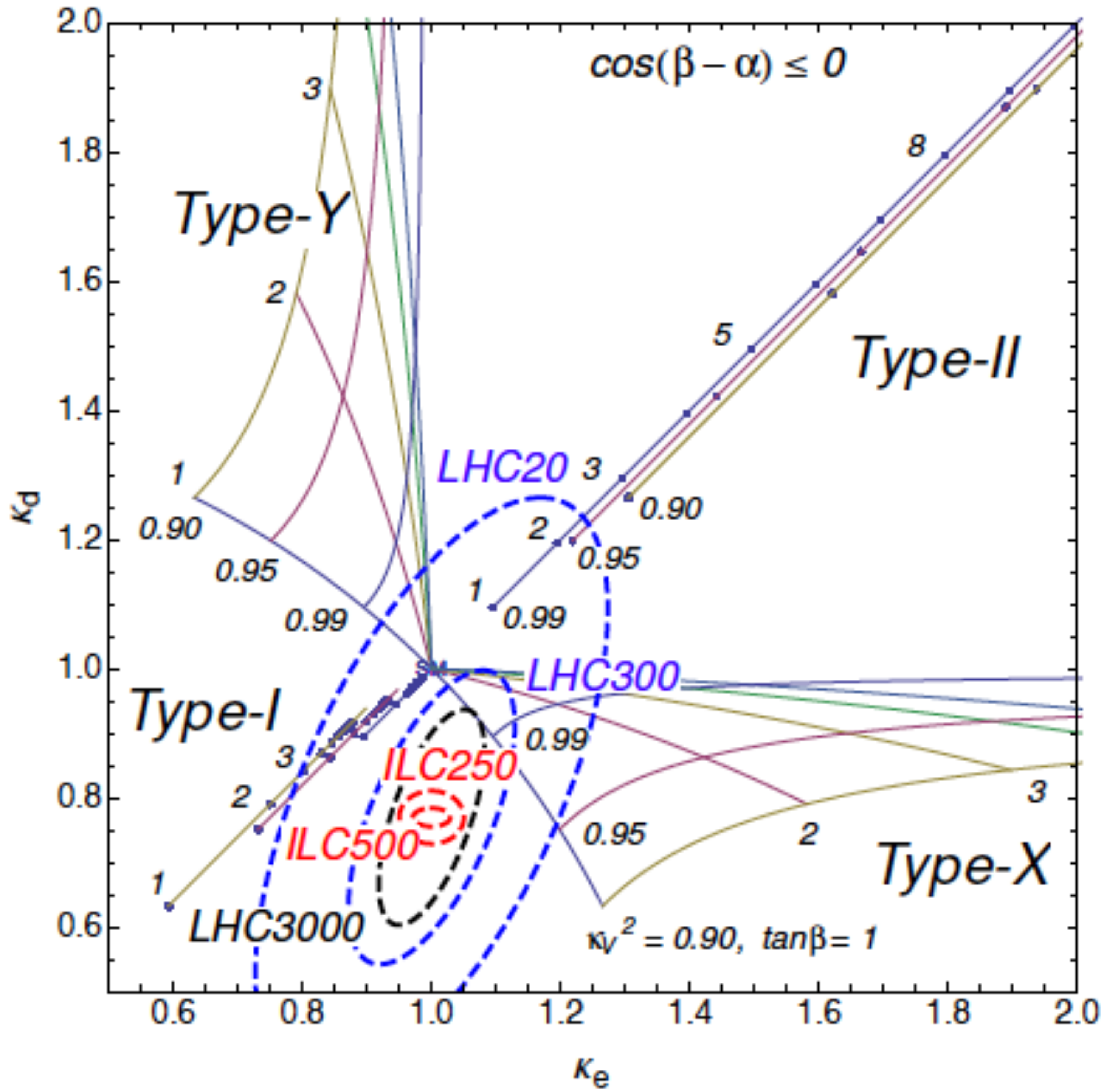
opportunities from precision Higgs couplings



arXiv: 1306.6352

- measuring deviation pattern will tell a lot about BSM

opportunities from precision Higgs couplings



Kanemura et al., arXiv: 1406.3294

fingerprint 4 types of 2HDM

general guidelines for Higgs coupling meas. @ future e+e-

—in light of what have been found at LHC

- new particles are heavy, deviation is small, 1-10% for m_{BSM}~1TeV: need measurement with 1% precision or below so that deviations with SM can be discovered

- measurement needs to be as model-independent as possible: so that the true BSM model can be discriminated from others, future HEP direction hence can be decided

proposals of future lepton colliders

	$\sqrt{s}$	beam polarisation	∫Ldt for Higgs	R&D phase
ILC	0.1 - 1 TeV	e-: 80% e+: 30% (20%)	2000 fb^{-1} @ 250 GeV 200 fb^{-1} @ 350 GeV 4000 fb-1 @ 500 GeV 8000 fb-1 @ 1 TeV	TDR
CLIC	0.35 - 3 TeV	e-: (80%) e+: 0%	500 fb^{-1} @ 380 GeV 1500 fb^{-1} @ 1.4 TeV 2500 fb^{-1} @ 3 TeV	CDR
CEPC	90 - 240 GeV	e-: 0% e+: 0%	5600 fb^{-1} @ 240 GeV	CDR
FCC-ee	90 - 365 GeV	e-: 0% e+: 0%	5000 fb^{-1} @ 240 GeV 1500 fb^{-1} @ 365 GeV	CDR

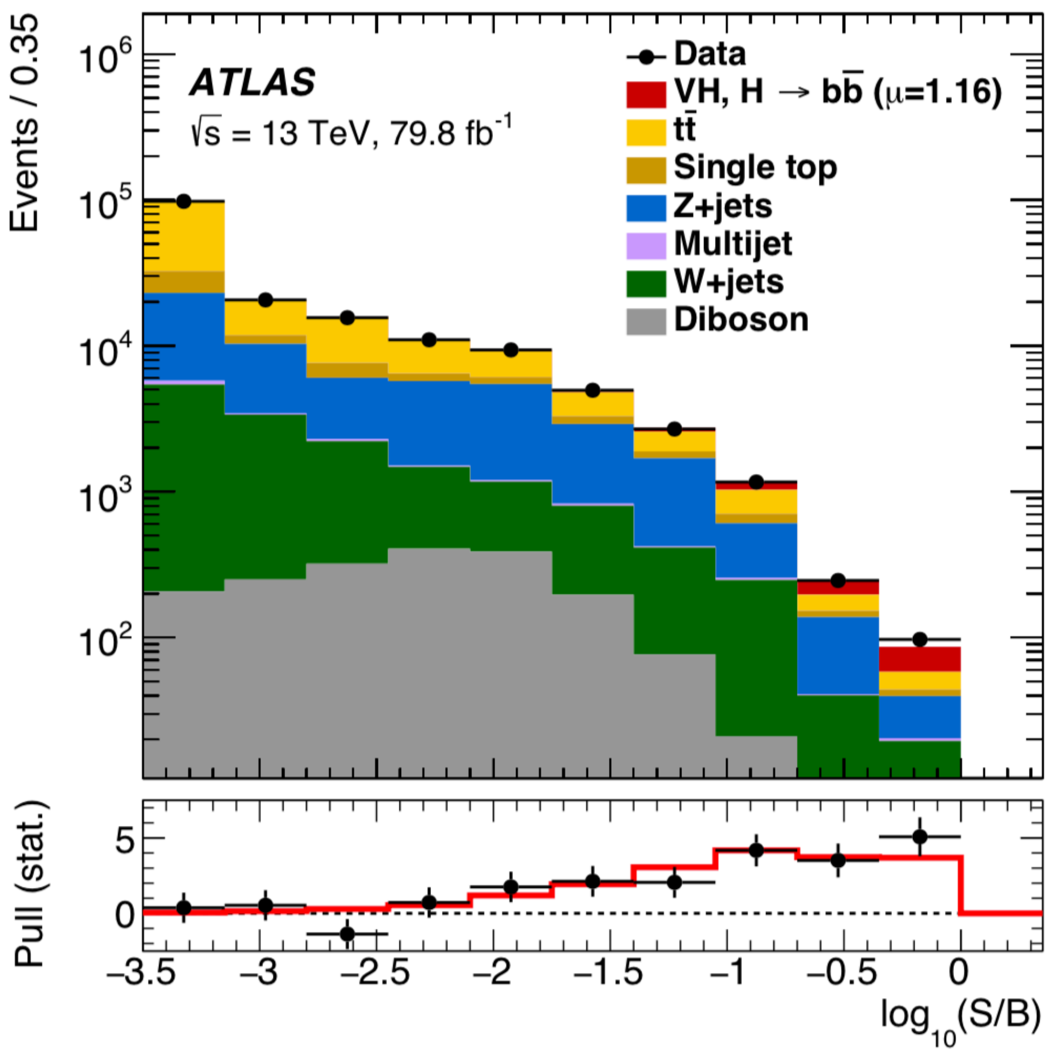
common: Higgs factory with $O(10^6)$ Higgs events

difference in Z-pole / WW runs; energy reach; L & Polarization "that is much much easier, infinitely easier, on a e+e- machine than on a proton machine"

youtube: Burton Richter #mylinearcollider, 2015

for example: H->bb discovery

at LHC



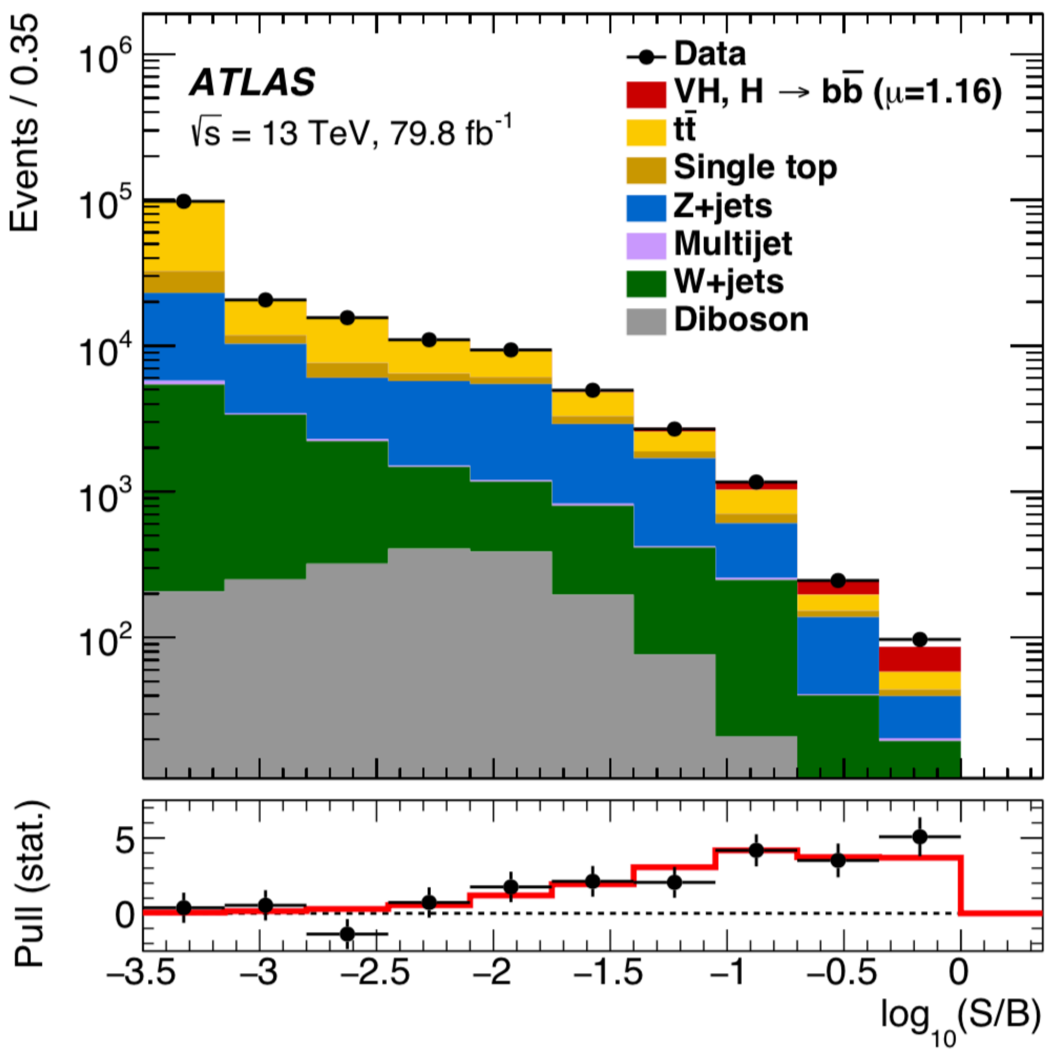
# of Higgs produced: ~4,000,000

significance: 5.4σ

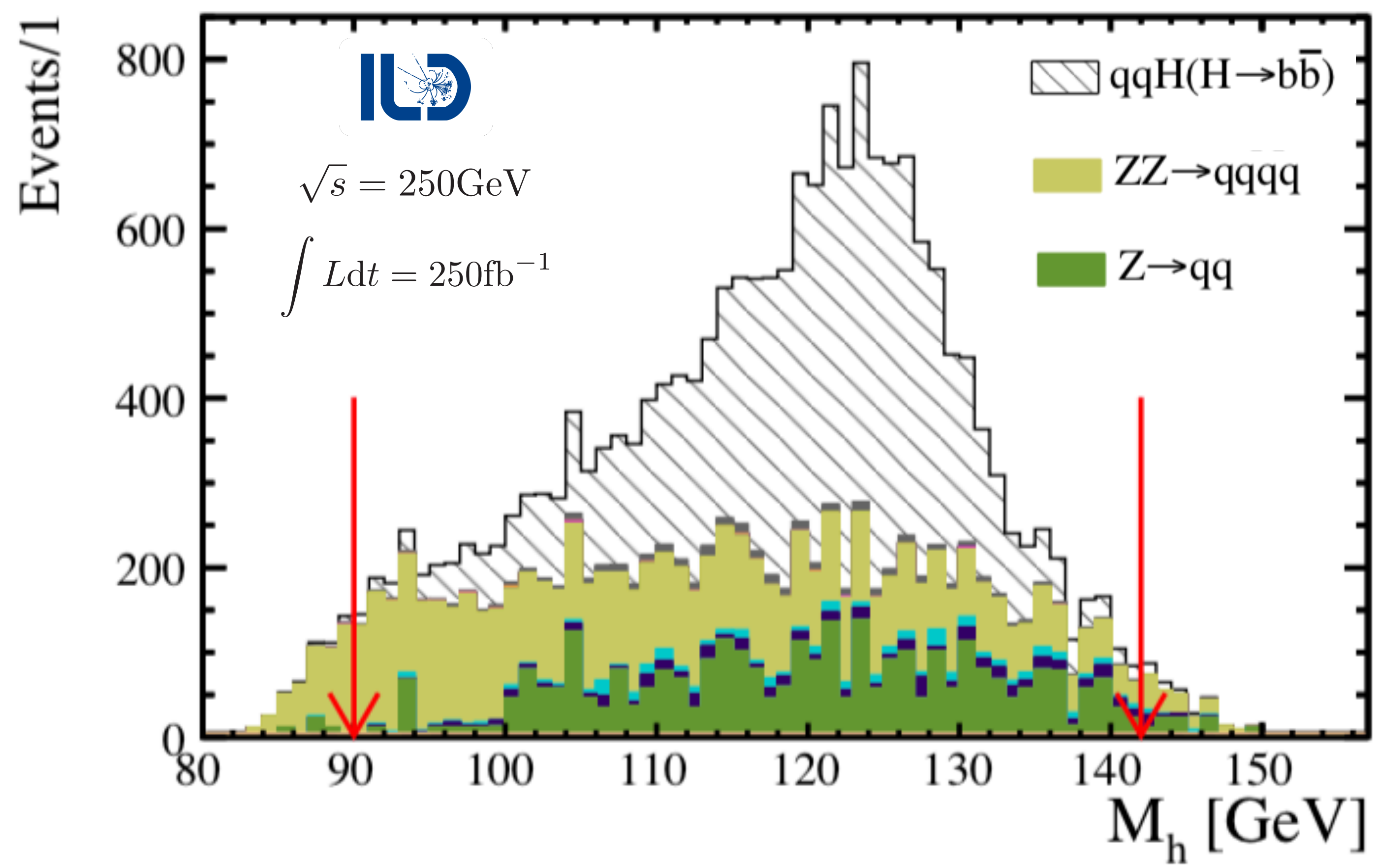
(ATLAS, 1808.08238; CMS, 1808.08242)

for example: H->bb discovery

at LHC



at e+e-



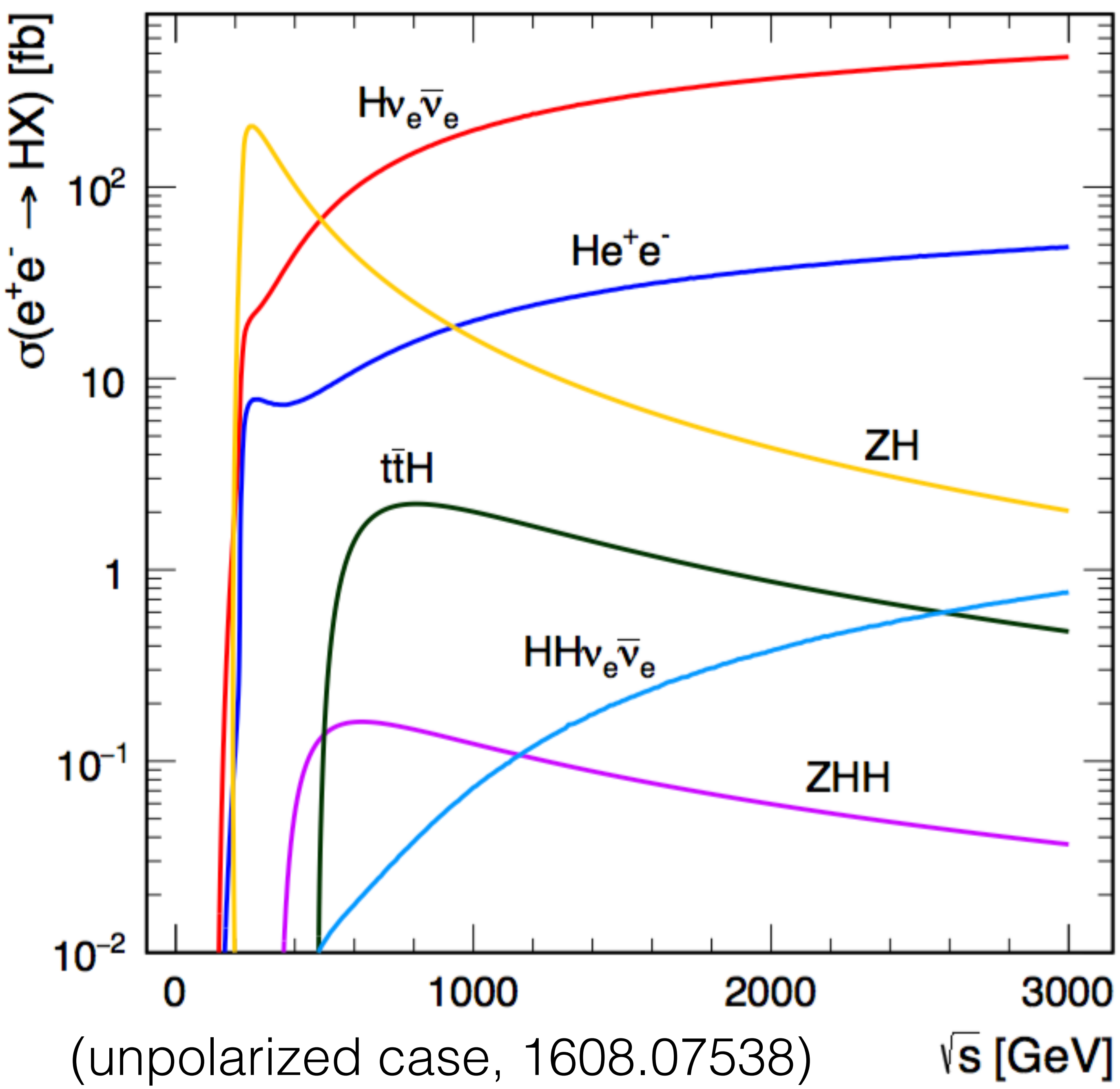
with 1.3 fb^{-1} data ~ 2 days running

	at LHC	at e+e-
# of Higgs produced:	~4,000,000	~400
significance:	5.4σ	5.2σ

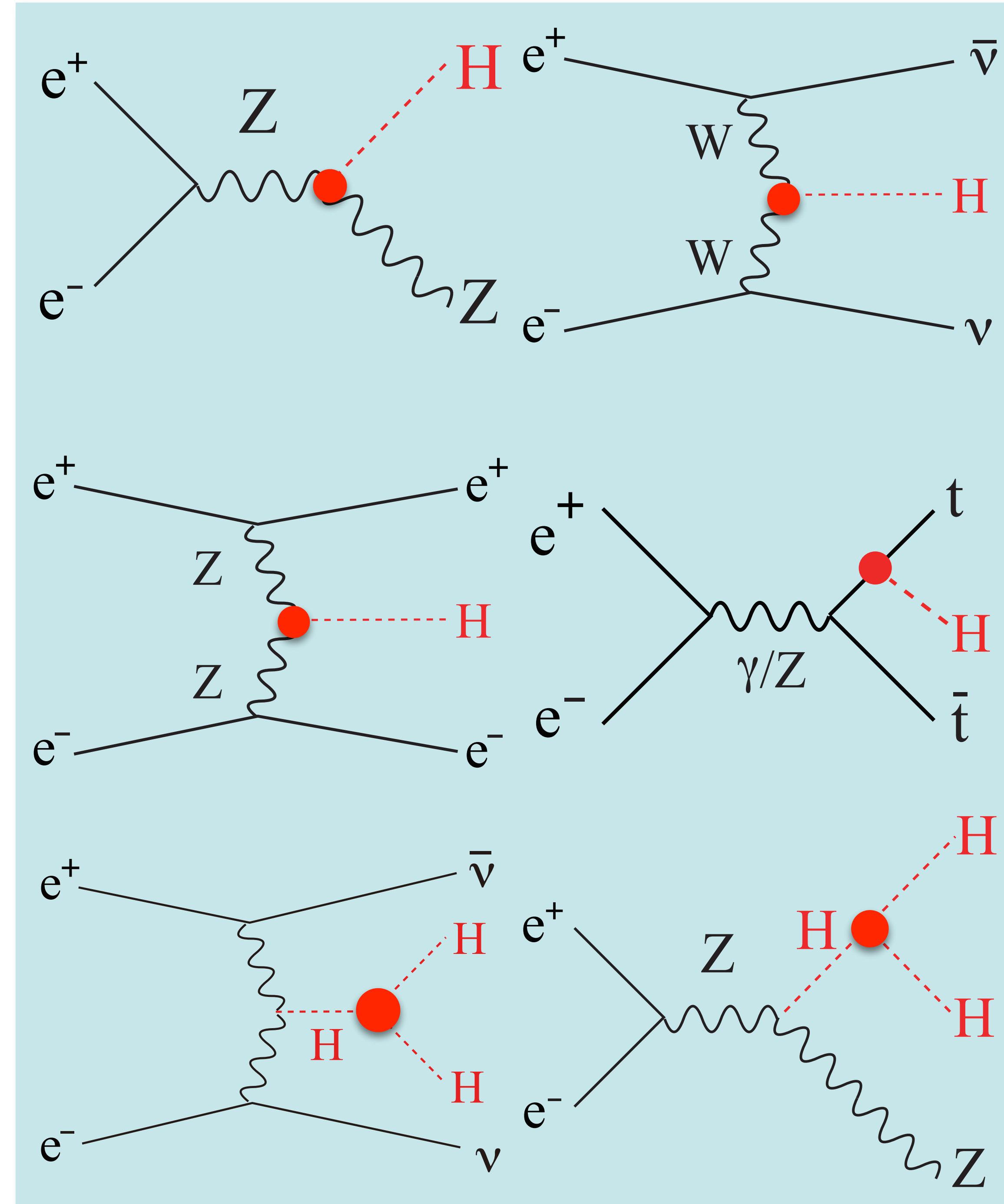
(ATLAS, 1808.08238; CMS, 1808.08242)

(Ogawa, PhD Thesis, ILD full simulation)

Higgs productions at e+e-



(unpolarized case, 1608.07538)



- two apparent important thresholds: √s ~ **250** GeV for ZH, ~**500** GeV for ZHH and ttH
- + another threshold for t t-bar, important for vacuum stability

direct experimental observables: some are unique @ e+e-

Higgs:

σ_{ZH}

$\sigma_{ZH}\times Br(H \rightarrow bb)$, $\sigma_{\nu\nu H}\times Br(H \rightarrow bb)$

$\sigma_{ZH}\times Br(H \rightarrow cc)$, $\sigma_{\nu\nu H}\times Br(H \rightarrow cc)$

$\sigma_{ZH}\times Br(H \rightarrow gg)$, $\sigma_{\nu\nu H}\times Br(H \rightarrow gg)$

$\sigma_{ZH}\times Br(H \rightarrow WW^*)$, $\sigma_{\nu\nu H}\times Br(H \rightarrow WW^*)$

$\sigma_{ZH}\times Br(H \rightarrow ZZ^*)$, $\sigma_{\nu\nu H}\times Br(H \rightarrow ZZ^*)$

$\sigma_{ZH}\times Br(H \rightarrow \tau\tau)$, $\sigma_{\nu\nu H}\times Br(H \rightarrow \tau\tau)$

$\sigma_{ZH}\times Br(H \rightarrow \gamma\gamma)$, $\sigma_{\nu\nu H}\times Br(H \rightarrow \gamma\gamma)$

$\sigma_{ZH}\times Br(H \rightarrow \mu\mu)$, $\sigma_{\nu\nu H}\times Br(H \rightarrow \mu\mu)$

$\sigma_{ZH}\times Br(H \rightarrow Invisible)$

$\sigma_{ttH}\times Br(H \rightarrow bb)$

$\sigma_{ZHH}\times Br^2(H \rightarrow bb)$, $\sigma_{\nu\nu HH}\times Br^2(H \rightarrow bb)$

EWPOs:

α, G_F, m_W, m_Z, m_h,
A_l, Γ_l, Γ_Z, Γ_W

TGCs:

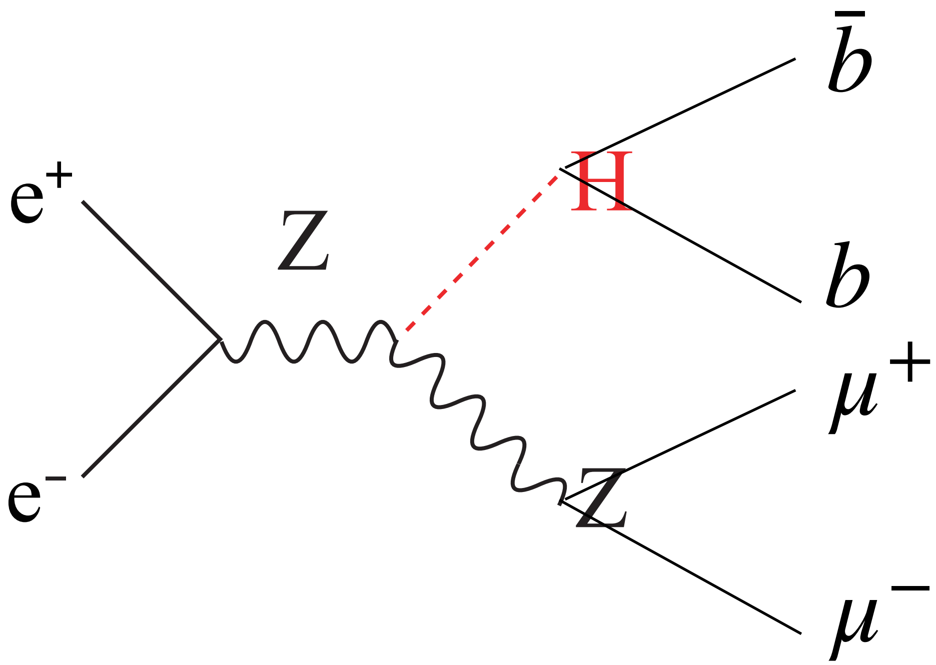
g_Z^1 κ_γ λ_γ

Global Fit: why do we need it?

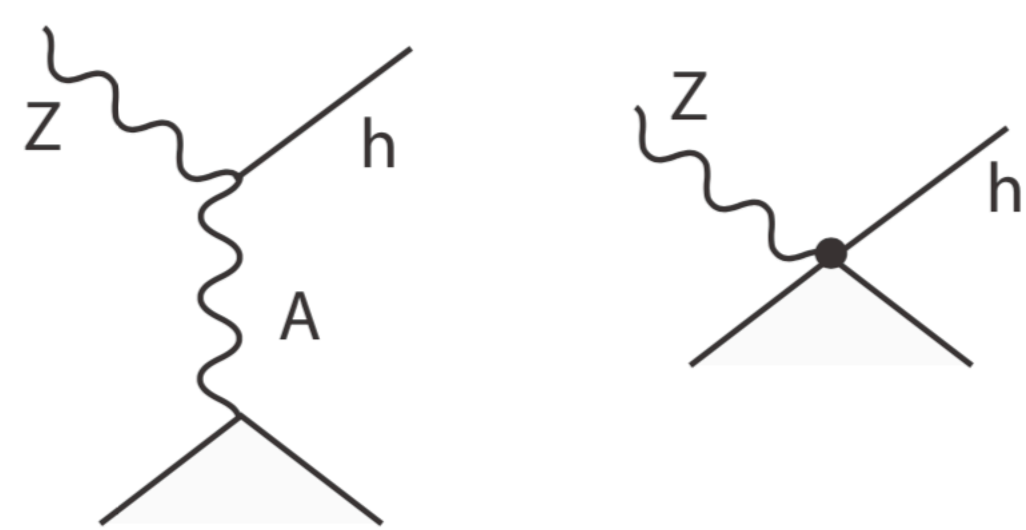
suppose we discover a deviation in, e.g. cross section of

e+e- -> ZH -> (μμ) (bb)

then we would like to know which coupling is deviated:



- hbb coupling?
- hZZ coupling?
- Zμμ coupling?
- Zee coupling?
- new diagrams?



From observables to couplings — Global Fit

$$\chi^2 = \sum_{i=1}^{n} (\frac{Y_i - Y_i'}{\Delta Y_i})^2$$

Yi: measured values by experiments

Yi': predicted values by underlying theory

ΔYi: measurement uncertainty

n: number of independent observables

- kappa formalism

$$Y_i' = F_i \cdot \frac{g^2_{HA_iA_i} \cdot g^2_{HB_iB_i}}{\Gamma_0} \qquad \begin{array}{l}(A_i = Z, W, t) \\ (B_i = b, c, \tau, \mu, g, \gamma, Z, W\ : \text{decay})\end{array}$$

$$g_{HXX} = \kappa_X \cdot g^{SM}_{HXX}$$

- SM Effective Field Theory formalism

From observables to couplings — Global Fit

in case there are correlated observables

$$\chi^2 = \sum_{i=1}^{n} (\frac{Y_i - Y_i'}{\Delta Y_i})^2 + (Y_j - Y_j')^T C_j^{-1} (Y_j - Y_j')$$

Yj: column vector of correlated observables

Cj: covariance matrix for those observables

one example: TGCs in SMEFT fit

Higgs coupling determination — kappa formalism

1) recoil mass technique —> inclusive $\boldsymbol{\sigma_{Zh}}$

2) σ_{Zh} —> $\boldsymbol{\kappa_Z}$ —> $\Gamma(h \to ZZ^*)$

3) W-fusion $\nu_e\nu_e h$ —> $\boldsymbol{\kappa_W}$ —> $\Gamma(h \to WW^*)$

4) total width $\boldsymbol{\Gamma_h} = \Gamma(h \to ZZ^*)/BR(h \to ZZ^*)$

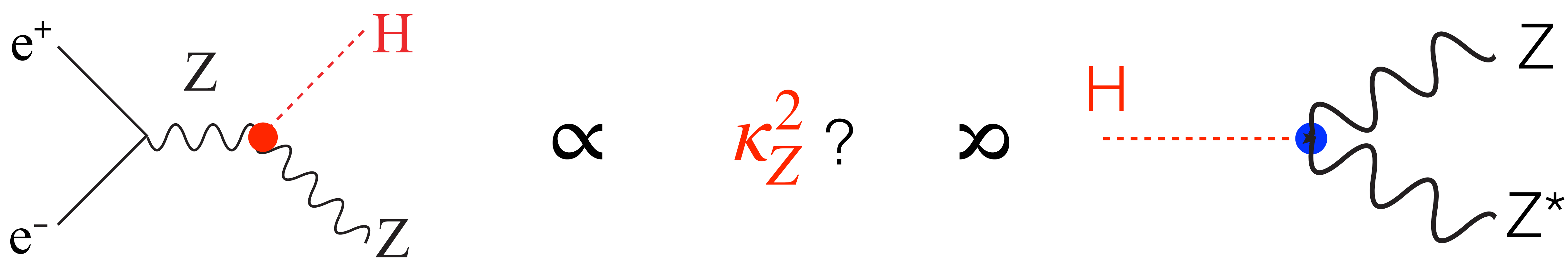
5) or $\boldsymbol{\Gamma_h} = \Gamma(h \to WW^*)/BR(h \to WW^*)$

6) then all other couplings $BR(h \to XX) * \Gamma_h$ —> $\boldsymbol{\kappa_X}$

JT, et al, PoS EPS-HEP2013 (2013) 316 Nucl.Part.Phys.Proc. 273-275 (2016) 826-833

one question in kappa formalism:

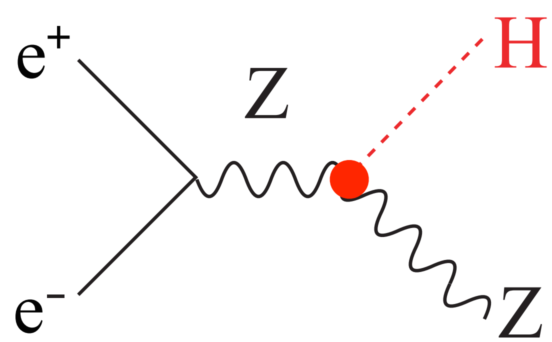
$$\frac{\sigma(e^+e^- \to Zh)}{SM} = \frac{\Gamma(h \to ZZ^*)}{SM} = \kappa_Z^2 \qquad \textbf{?}$$

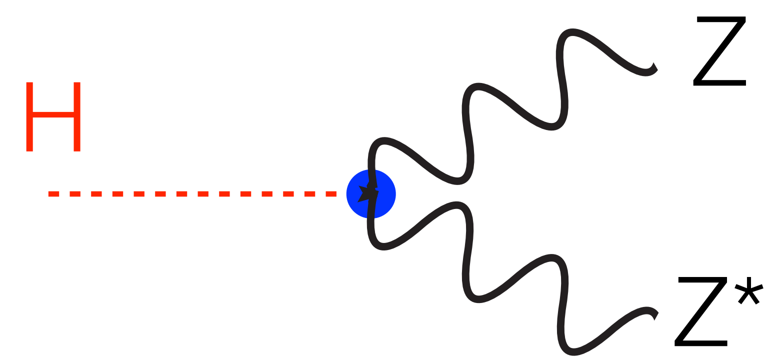


BSM territory: can deviations be represented by single κ_Z?

the answer is model dependent

$$\delta\mathcal{L} = (1+\eta_Z)\frac{m_Z^2}{v} h Z_\mu Z^\mu + \zeta_Z \frac{h}{2v} Z_{\mu\nu} Z^{\mu\nu}$$





$$\sigma(e^+e^- \to Zh) = (SM)\cdot (1 + 2\eta_Z + (5.5)\zeta_Z)$$

$$\neq$$

$$\Gamma(h \to ZZ^*) = (SM)\cdot (1 + 2\eta_Z - (0.50)\zeta_Z)$$

- BSM can induce new Lorentz structures in hZZ
- need a better, more theoretical sound framework

new strategy: SM Effective Field Theory

$$\mathcal{L}_{\rm eff} = \mathcal{L}_{\rm SM} + \Delta\mathcal{L}$$

$$= \mathcal{L}_{\rm SM} + \sum_i \frac{c_i}{\Lambda^{d_i-4}} O_i$$

- most general BSM effects represented by $d_i>4$ operators
  - more model-independent formalism
- well-defined quantum field theory respecting SM SU(3)xSU(2)xU(1) gauge symmetries
  - can include radiative corrections consistently
- unifying BSM effects in Higgs, W/Z, top, 2-fermion physics
  - global view in searching for BSM

SM Effective Field Theory: some simplifications

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \Delta\mathcal{L}$$

$$= \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i}{\Lambda^{d_i - 4}} O_i$$

the new particle searches at LHC Run 2 suggest ***Λ>500*** GeV

simply the analysis up to dimension-**6** operators

there are ***84*** of such operators for 1 fermion generation

assuming B & L number conservation, there are ***59***

- there exists a smaller but complete set relevant to Higgs coupling determination at e+e-

global SMEFT fit @ e+e-

(Barklow, Fujii, Jung, Peskin, JT, arXiv:1708.09079)

$$\Delta\mathcal{L} = \frac{c_H}{2v^2}\partial^\mu(\Phi^\dagger\Phi)\partial_\mu(\Phi^\dagger\Phi) + \frac{c_T}{2v^2}(\Phi^\dagger \overleftrightarrow{D}^\mu \Phi)(\Phi^\dagger \overleftrightarrow{D}_\mu \Phi) - \frac{c_6\lambda}{v^2}(\Phi^\dagger\Phi)^3$$
$$+\frac{g^2 c_{WW}}{m_W^2}\Phi^\dagger\Phi W^a_{\mu\nu}W^{a\mu\nu} + \frac{4gg' c_{WB}}{m_W^2}\Phi^\dagger t^a\Phi W^a_{\mu\nu}B^{\mu\nu}$$
$$+\frac{g'^2 c_{BB}}{m_W^2}\Phi^\dagger\Phi B_{\mu\nu}B^{\mu\nu} + \frac{g^3 c_{3W}}{m_W^2}\epsilon_{abc}W^a_{\mu\nu}W^{b\nu}{}_\rho W^{c\rho\mu}$$
$$+i\frac{c_{HL}}{v^2}(\Phi^\dagger \overleftrightarrow{D}^\mu \Phi)(\overline{L}\gamma_\mu L) + 4i\frac{c'_{HL}}{v^2}(\Phi^\dagger t^a \overleftrightarrow{D}^\mu \Phi)(\overline{L}\gamma_\mu t^a L)$$
$$+i\frac{c_{HE}}{v^2}(\Phi^\dagger \overleftrightarrow{D}^\mu \Phi)(\overline{e}\gamma_\mu e)\ .$$

"Warsaw" basis,
Grzadkowski et al,
arXiv:1008.4884

Φ: higgs field
W, B: SU(2), U(1) gauge
L, e: left/right electron

- 10 operators modifying couplings for h/Z/W/γ
- in total, 23 parameters (see later slides)

next: highlight a few important implications

recap 1: absolute Higgs couplings (unique role of inclusive σ_{Zh})

$$\frac{c_H}{2v^2}\partial^\mu(\Phi^\dagger\Phi)\partial_\mu(\Phi^\dagger\Phi)$$

$$\frac{c_H}{2}\partial^\mu h \partial_\mu h$$ ⟶ renormalize kinetic term of SM Higgs field

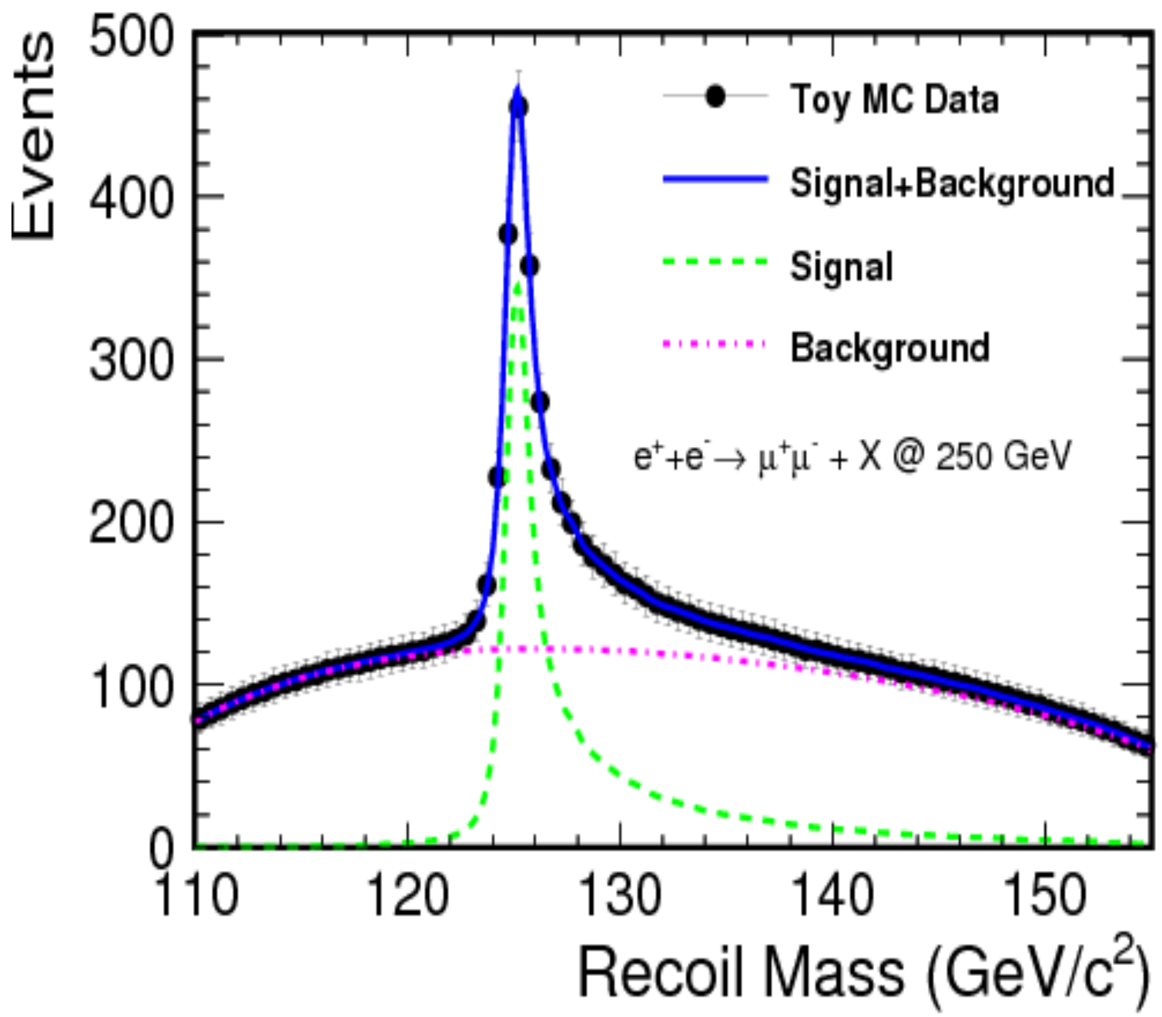
h ⟶ $(1-c_H/2)h$

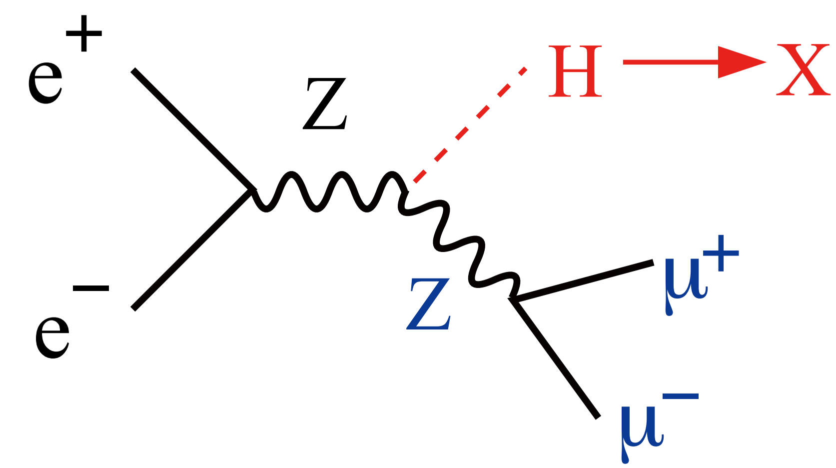
⟶ **shift all SM Higgs couplings by $-c_H/2$**

- c_H can not be determined by any BR or ratio of couplings

- c_H has to rely on inclusive cross section of $e^+e^- \rightarrow Zh$, enabled by recoil mass technique at e+e-

inclusive cross section for Higgs production: unique at e+e-





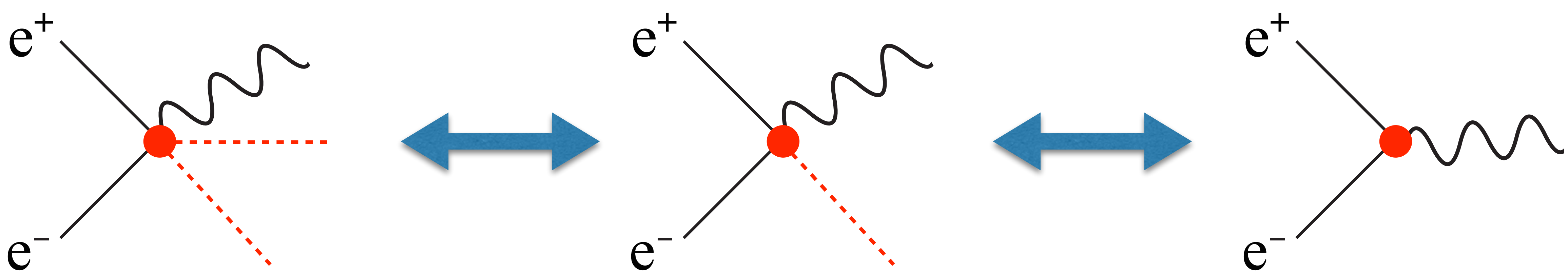
$$M_X^2 = \left(p_{CM} - (p_{\mu^+} + p_{\mu^-})\right)^2$$

for Z->ll, Yan et al, arXiv:1604.07524;
for Z->qq, Thomson, arXiv:1509.02853

- well defined initial states at e+e-
- recoil mass technique → tag Z only
- without looking into H decay
- absolute cross section of e^+e^- → ZH

recap 2: Higgs couplings are related to W-/Z- couplings (EWPOs)

$$i\frac{c_{HL}}{v^2}(\Phi^\dagger \overleftrightarrow{D}^{\mu}\Phi)(\overline{L}\gamma_\mu L) \qquad +(c'_{HL},\ c_{HE})$$

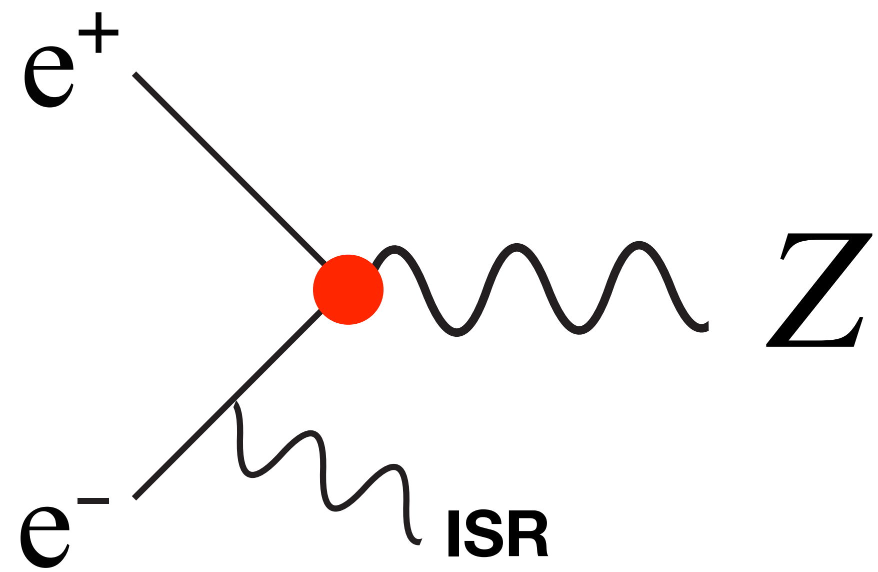


$e^+e^- \to Zhh$ $e^+e^- \to Zh$ Z-pole

- Higgs coupling encoded in EWPOs at Z-pole: $\boldsymbol{A_{LR}}$, $\boldsymbol{\Gamma_l}$
- Z coupling helped by Higgs meas. at high $\sqrt{s}$: $\boldsymbol{\delta\sigma \sim s/m^2_Z}$

new ideas: improving EWPOs @ ILC250

radiative return



- a free gift by ISR: Higgs factory is meantime a Z factory
- **~10^8** Z events by ILC250, without any change of accelerator
- more over, **polarized beams**

ILC250 = ILC250 + 100xLEP/SLC

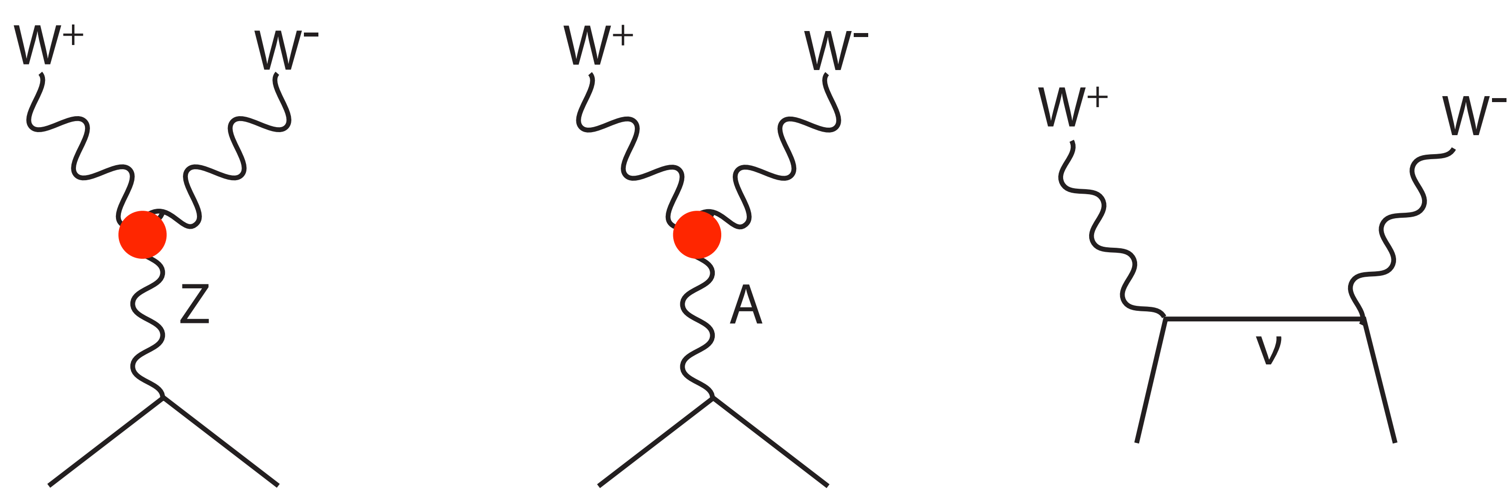
see more in arXiv:1908.11299

- expect a factor of 10 improvement on ALR

recap 2: Higgs couplings are related to W-/Z- couplings (TGCs)

$$\boxed{\frac{4gg'c_{WB}}{m_W^2}\Phi^\dagger t^a \Phi W^a_{\mu\nu}B^{\mu\nu}} \qquad +(c_{WW},\, c_{BB})$$

$e^+e^- \to WW$



$h \to ZZ$ $\qquad \zeta_Z \frac{h}{2v} Z_{\mu\nu}Z^{\mu\nu}$ $\qquad \zeta_Z = c_w^2(8c_{WW}) + 2s_w^2(8c_{WB}) + s_w^4/c_w^2(8c_{BB})$

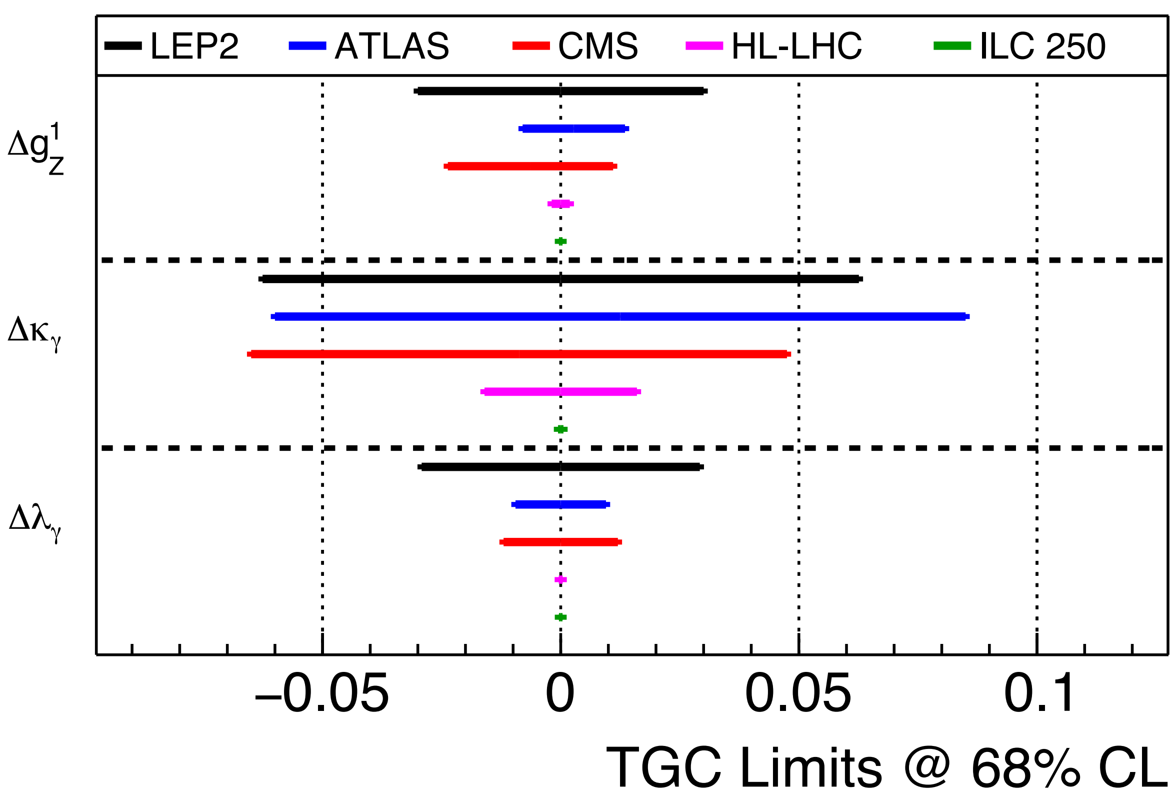
- longitudinal modes of W/Z are from Higgs fields
- higgs coupling helped by meas. of TGCs in $e^+e^- \to WW$

expected improvement on TGCs at ILC250

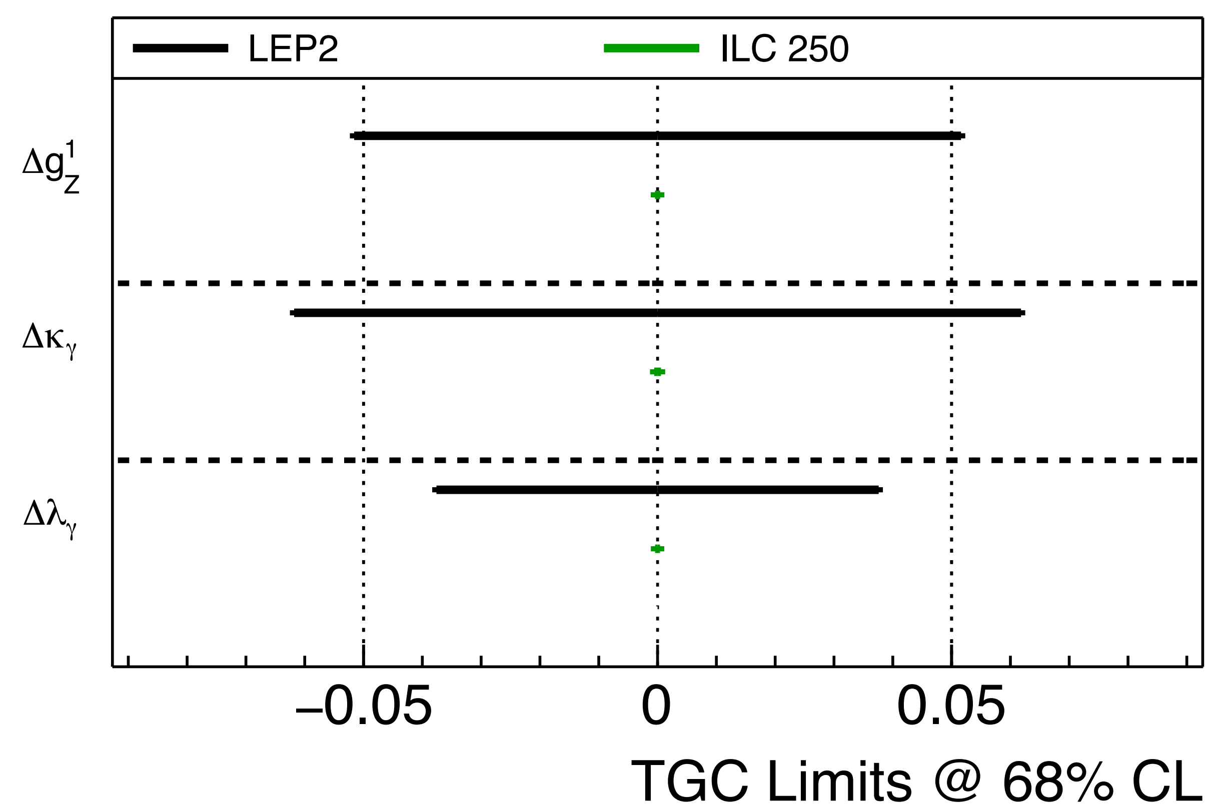
arXiv:1908.11299

$$\Delta\mathcal{L}_{TGC} = ig_V\left\{V^\mu(\hat{W}^-_{\mu\nu}W^{+\nu} - \hat{W}^+_{\mu\nu}W^{-\nu}) + \kappa_V W^+_\mu W^-_\nu \hat{V}^{\mu\nu} + \frac{\lambda_V}{m_W^2}\hat{W}^{-\rho}_{\mu}\hat{W}^+_{\rho\nu}\hat{V}^{\mu\nu}\right\}$$

1-par sensitivity



3-par sensitivity



- statistically x2000 more WW events w.r.t. LEP2

recap 3: Higgs couplings are related to themselves

$$\Delta\mathcal{L}_h = \frac{1}{2}\partial_\mu h \partial^\mu h - \frac{1}{2}m_h^2 h^2 - (1+\eta_h)\bar{\lambda} v h^3 + \frac{\theta_h}{v} h\partial_\mu h \partial^\mu h$$
$$+(1+\eta_W)\frac{2m_W^2}{v}W_\mu^+ W^{-\mu} h + (1+\eta_{WW})\frac{m_W^2}{v^2}W_\mu^+ W^{-\mu} h^2$$
$$+(1+\eta_Z)\frac{m_Z^2}{v}Z_\mu Z^\mu h + \frac{1}{2}(1+\eta_{ZZ})\frac{m_Z^2}{v^2}Z_\mu Z^\mu h^2$$
$$+\zeta_W \hat{W}_{\mu\nu}^+ \hat{W}^{-\mu\nu}\left(\frac{h}{v}+\frac{1}{2}\frac{h^2}{v^2}\right) + \frac{1}{2}\zeta_Z \hat{Z}_{\mu\nu}\hat{Z}^{\mu\nu}\left(\frac{h}{v}+\frac{1}{2}\frac{h^2}{v^2}\right)$$
$$+\frac{1}{2}\zeta_A \hat{A}_{\mu\nu}\hat{A}^{\mu\nu}\left(\frac{h}{v}+\frac{1}{2}\frac{h^2}{v^2}\right) + \zeta_{AZ}\hat{A}_{\mu\nu}\hat{Z}^{\mu\nu}\left(\frac{h}{v}+\frac{1}{2}\frac{h^2}{v^2}\right) .$$

(SM structure: kappa like)

$$\eta_h = \delta\bar{\lambda} + \delta v - \frac{3}{2}c_H + c_6$$
$$\eta_W = 2\delta m_W - \delta v - \frac{1}{2}c_H$$
$$\eta_{WW} = 2\delta m_W - 2\delta v - c_H$$
$$\eta_Z = 2\delta m_Z - \delta v - \frac{1}{2}c_H - c_T$$
$$\eta_{ZZ} = 2\delta m_Z - 2\delta v - c_H - 5c_T$$

(Anomalous: new Lorentz structure)

$$\theta_h = c_H$$
$$\zeta_W = \delta Z_W \quad = (8c_{WW})$$
$$\zeta_Z = \delta Z_Z \quad = c_w^2(8c_{WW}) + 2s_w^2(8c_{WB}) + s_w^4/c_w^2(8c_{BB})$$
$$\zeta_A = \delta Z_A \quad = s_w^2\Big((8c_{WW}) - 2(8c_{WB}) + (8c_{BB})\Big)$$
$$\zeta_{AZ} = \delta Z_{AZ} \quad = s_w c_w\Big((8c_{WW}) - (1-\frac{s_w^2}{c_w^2})(8c_{WB}) - \frac{s_w^2}{c_w^2}(8c_{BB})\Big)$$

- hZZ/hWW/hγZ/hγγ highly related: SU(2)xU(1) gauge symmetries

recap 3: Higgs couplings are related to themselves (synergy w/ LHC)

two measurements from LHC (model independent)

$$R_{\gamma\gamma} = \frac{BR(h \to \gamma\gamma)}{BR(h \to ZZ^*)} \qquad R_{\gamma Z} = \frac{BR(h \to \gamma Z)}{BR(h \to ZZ^*)}$$

$$\delta\Gamma(h \to \gamma\gamma) = \mathbf{528}\, \delta Z_A - c_H \quad + \ldots$$

$$\delta\Gamma(h \to Z\gamma) = \mathbf{290}\ \delta Z_{AZ} - c_H \quad + \ldots$$

$$\delta\Gamma(h \to ZZ^*) = -0.50\delta Z_Z \ - c_H \quad + \ldots$$

- loop induced h->γγ/γZ depend strongly on $c_{WW}/c_{WB}/c_{BB}$

- h → γγ/γZ at LHC can help higgs couplings at e+e-

recap 3: Higgs couplings are related to themselves (hWW/hZZ)

$$\Gamma(h \to ZZ^*) = (SM) \cdot (1 + 2\eta_Z - (0.50)\zeta_Z) \ ,$$

$$\Gamma(h \to WW^*) = (SM) \cdot (1 + 2\eta_W - (0.78)\zeta_W)$$

SM-like hVV

$$\eta_W = -\frac{1}{2}c_H$$

$$\eta_Z = -\frac{1}{2}c_H - c_T$$

custodial symmetry is broken by c_T -> constrained by EWPOs

$c_i \sim O(10^{-4}\text{-}10^{-3})$

anomalous hVV

$$\zeta_W = (8c_{WW})$$

$$\zeta_Z = c_w^2(8c_{WW}) + 2s_w^2(8c_{WB}) + (s_w^4/c_w^2)(8c_{BB})$$

- hWW/hZZ ratio can be determined to <0.1%

- very important for physics case of any 250 GeV e+e-
- hWW can be determined as precisely as hZZ at 250 GeV; hence precision total width & other couplings

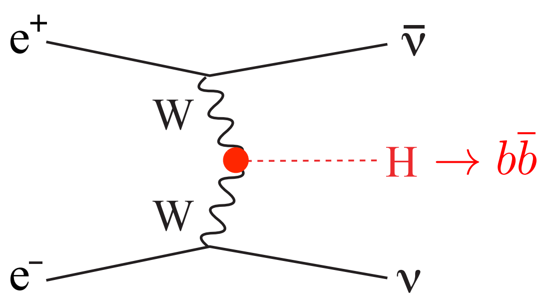
direct meas. of hWW coupling & impact of √s

$$\Gamma_H = \frac{\Gamma_{HZZ}}{\mathrm{Br}(H \to ZZ^*)} \propto \frac{g^2_{HZZ}}{\mathrm{Br}(H \to ZZ^*)}$$

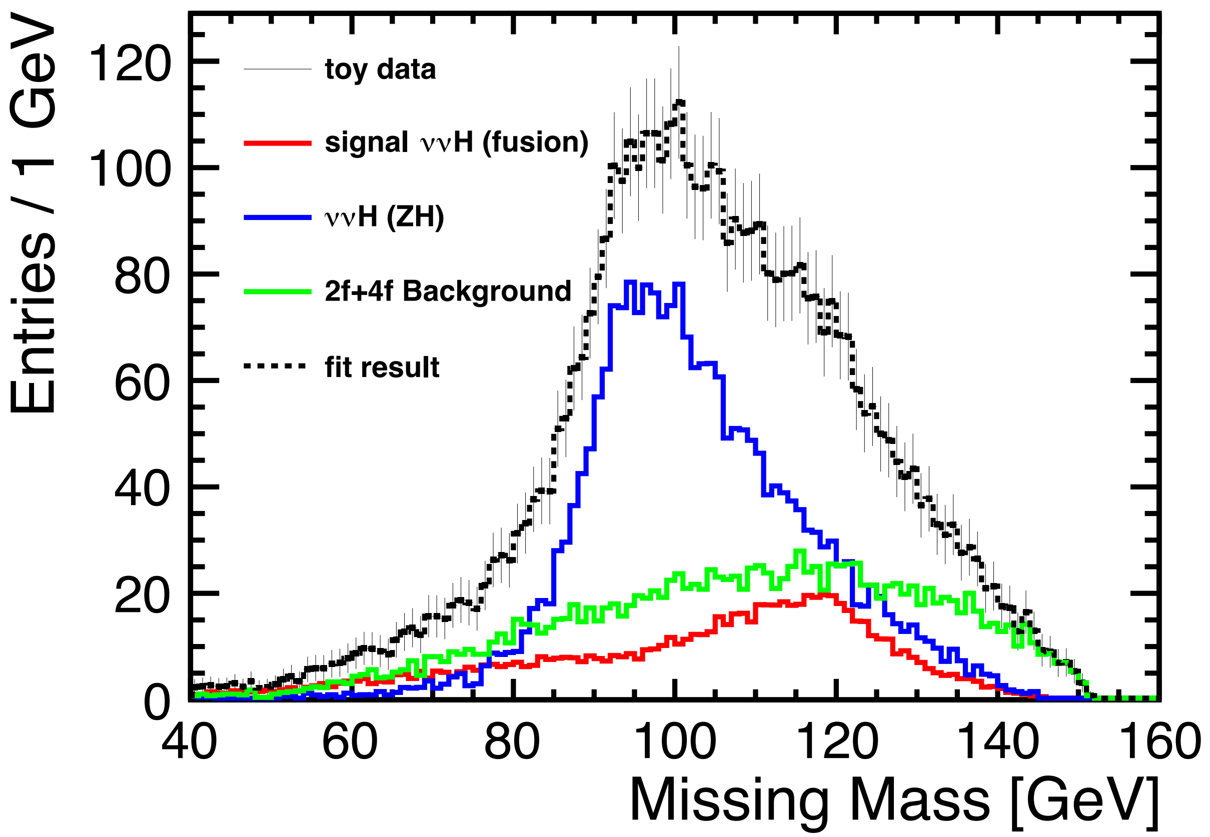
—>Br(H->ZZ*) very small

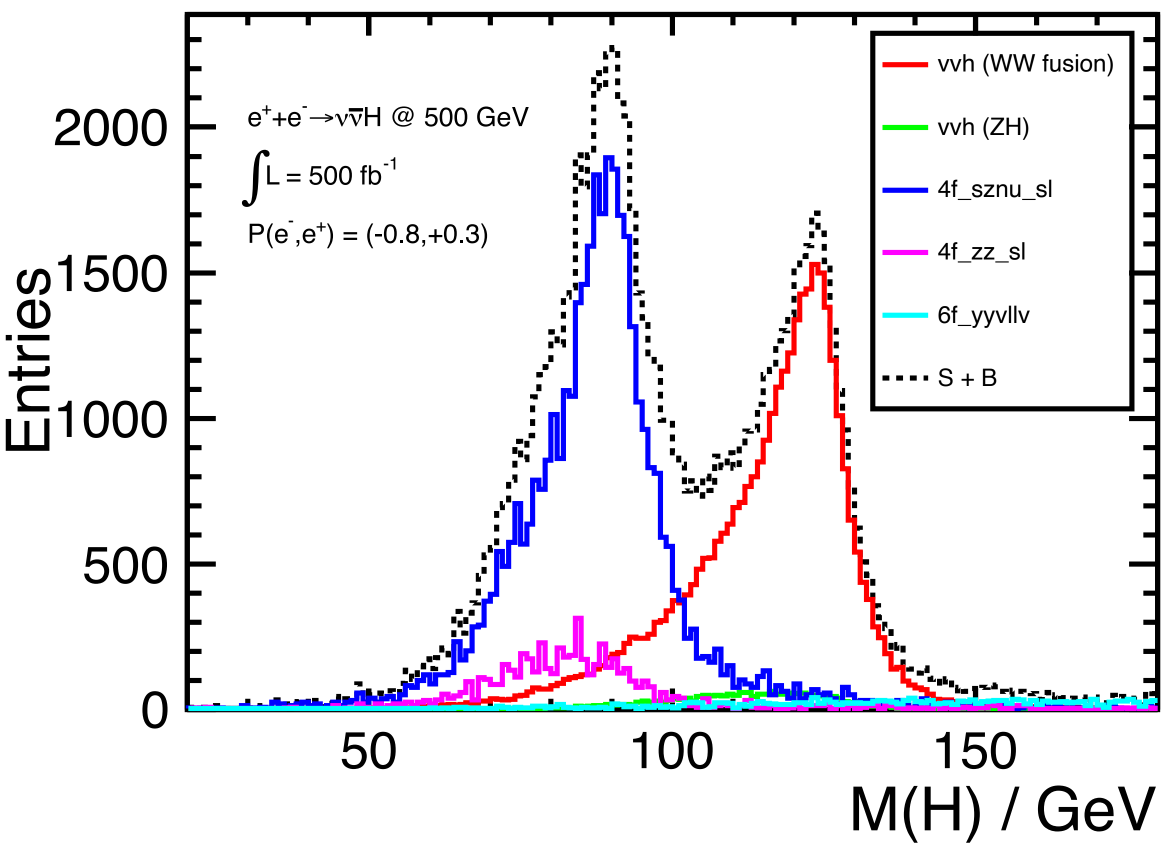
★ $$\Gamma_H = \frac{\Gamma_{HWW}}{\mathrm{Br}(H \to WW^*)} \propto \frac{g^2_{HWW}}{\mathrm{Br}(H \to WW^*)}$$

—> better option!



@250 GeV Duerig, et al., arXiv:1403.7734 **@500 GeV**





- we used to think W-fusion production is crucial…

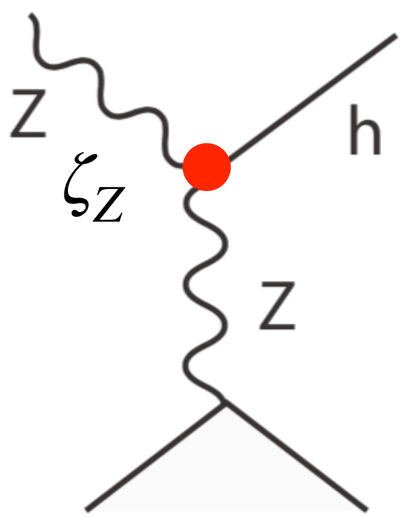
SMEFT fit: typical difference with kappa fit

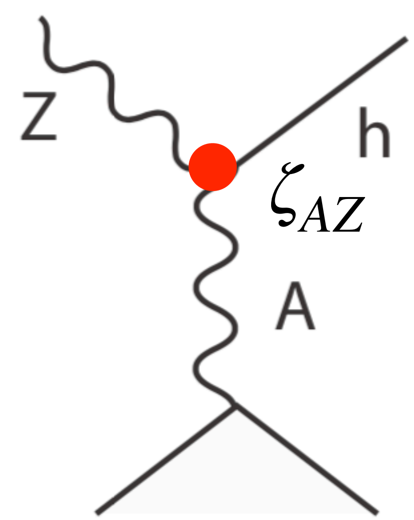
ILC250: $\int L dt$ = 2 ab^{-1} @ 250 GeV

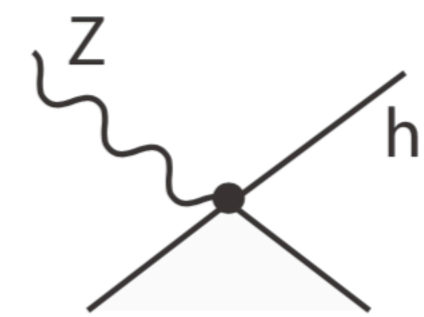
coupling $\Delta g/g$	kappa-fit	EFT-fit
hZZ	0.38%	0.50%
hWW	1.8%	0.50%
hbb	1.8%	0.99%
Γ_h	3.9%	2.3%

(definition for higgs coupling precision: 1/2 of partial width precision)

recap 4: role of beam polarizations







P(e⁻,e⁺)			
(-1,+1)	$\frac{g}{\cos\theta_w}(\frac{1}{2}-\sin^2\theta_w)$	$g\sin\theta_w$	$\frac{g}{\cos\theta_w}(c_{HL}+c'_{HL})$
(+1,-1)	$\frac{g}{\cos\theta_w}(-\sin^2\theta_w)$	$g\sin\theta_w$	$\frac{g}{\cos\theta_w}(c_{HE})$

- sensitive to different couplings -> lift degeneracy
- A_{LR} in σ_{ZH} -> improve c_{WW}, $c_{HL}+c_{HL}'$ and c_{HE}
- large cancellation in **(+1,-1)** -> weaker dependence on c_{WW}

recap 4: role of beam polarizations (e+e- -> Zh)

√s=250 GeV

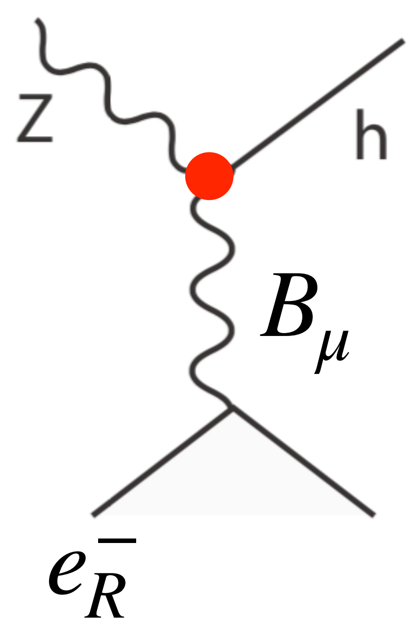
$$\delta\sigma_L = -c_H + 7.7(8c_{WW}) + \dots$$

$$\delta\sigma_R = -c_H + 0.6(8c_{WW}) + \dots$$

why?

$$\delta\sigma_0 = -c_H + 4.6(8c_{WW}) + \dots$$

($8c_{WW}$) ~ 0.16% from other meas.



contribution from

almost cancels out

$$\frac{g^2 c_{WW}}{m_W^2}\Phi^\dagger \Phi W^a_{\mu\nu} W^{a\mu\nu}$$

up to a difference in Z/γ propagator suppressed by $\frac{m_Z^2}{s}$

recap 4: role of beam polarizations (overall effects)

ILC250: 2 ab^{-1} **FCCee240: 5 ab^{-1}**

coupling	2/ab-250 pol.	+4/ab-500 pol.	5/ab-250 unpol.	+ 1.5/ab-350 unpol
HZZ	0.50	0.35	0.41	0.34
HWW	0.50	0.35	0.42	0.35
Hbb	0.99	0.59	0.72	0.62
$H\tau\tau$	1.1	0.75	0.81	0.71
Hgg	1.6	0.96	1.1	0.96
Hcc	1.8	1.2	1.2	1.1
$H\gamma\gamma$	1.1	1.0	1.0	1.0
$H\gamma Z$	9.1	6.6	9.5	8.1
$H\mu\mu$	4.0	3.8	3.8	3.7
Htt	-	6.3	-	-
HHH	-	27	-	-
Γ_{tot}	2.3	1.6	1.6	1.4
Γ_{inv}	0.36	0.32	0.34	0.30
Γ_{other}	1.6	1.2	1.1	0.94

- 250 GeV e+e-: power of 2 ab^{-1} polarized ≈ 5 ab^{-1} unpolarized

(arXiv:1903.01629)

global SMEFT fit: full formalism (23 pars.)

$$\Delta\mathcal{L} = \frac{c_H}{2v^2}\partial^\mu(\Phi^\dagger\Phi)\partial_\mu(\Phi^\dagger\Phi) + \frac{c_T}{2v^2}(\Phi^\dagger \overleftrightarrow{D}^\mu\Phi)(\Phi^\dagger \overleftrightarrow{D}_\mu \Phi) - \frac{c_6\lambda}{v^2}(\Phi^\dagger\Phi)^3$$
$$+\frac{g^2 c_{WW}}{m_W^2}\Phi^\dagger\Phi W^a_{\mu\nu}W^{a\mu\nu} + \frac{4gg' c_{WB}}{m_W^2}\Phi^\dagger t^a\Phi W^a_{\mu\nu}B^{\mu\nu}$$
$$+\frac{g'^2 c_{BB}}{m_W^2}\Phi^\dagger\Phi B_{\mu\nu}B^{\mu\nu} + \frac{g^3 c_{3W}}{m_W^2}\epsilon_{abc}W^a_{\mu\nu}W^{b\nu}{}_\rho W^{c\rho\mu}$$
$$+i\frac{c_{HL}}{v^2}(\Phi^\dagger \overleftrightarrow{D}^\mu\Phi)(\overline{L}\gamma_\mu L) + 4i\frac{c'_{HL}}{v^2}(\Phi^\dagger t^a \overleftrightarrow{D}^\mu\Phi)(\overline{L}\gamma_\mu t^a L)$$
$$+i\frac{c_{HE}}{v^2}(\Phi^\dagger \overleftrightarrow{D}^\mu\Phi)(\overline{e}\gamma_\mu e) \;.$$

10 operators (h,W,Z,γ): c_H, c_T, c_6, c_{WW}, c_{WB}, c_{BB}, c_{3W}, c_{HL}, c'_{HL}, c_{HE}

+ 4 SM parameters: g, g’, v, λ
+ 5 operators modifying h couplings to b, c, τ, μ, g
+ 2 operators for contact interactions with quarks
+ 2 parameters for h->invisible and exotic

strategy to determine all the 23 parameters at e+e-

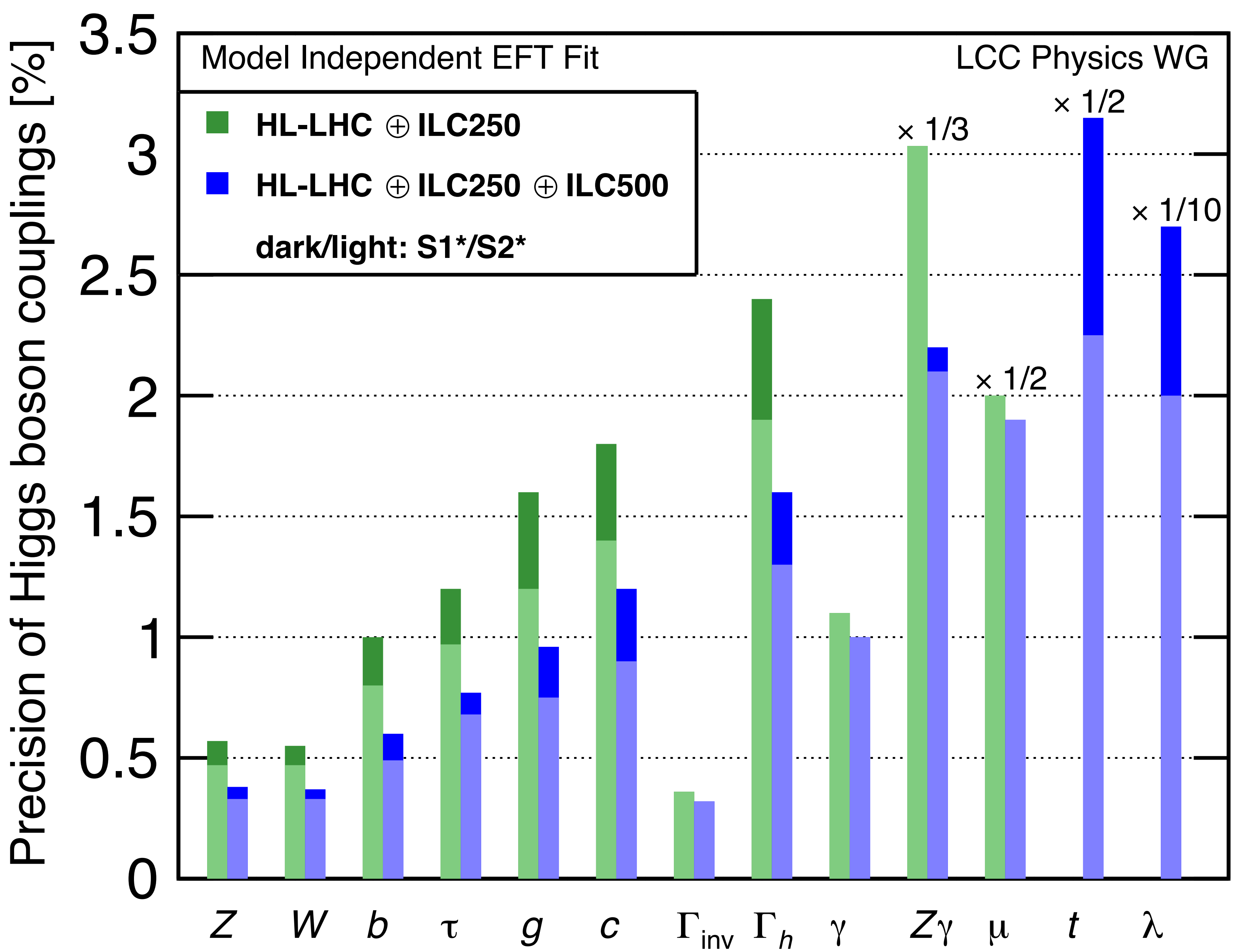
Electroweak Precision Observables	(9)
+	
Triple Gauge boson Couplings	(3)
+	
Higgs observables at LHC & e+e-	(3+12x2)

↑ 2 for polarized

- all the 23 parameters can be determined ***simultaneously***

(details in backup)

precisions at Higgs factories: complementarity with LHC



(arXiv:1903.01629)

#qualitative:

model independence, hcc coupling

#quantitative (<~1%):

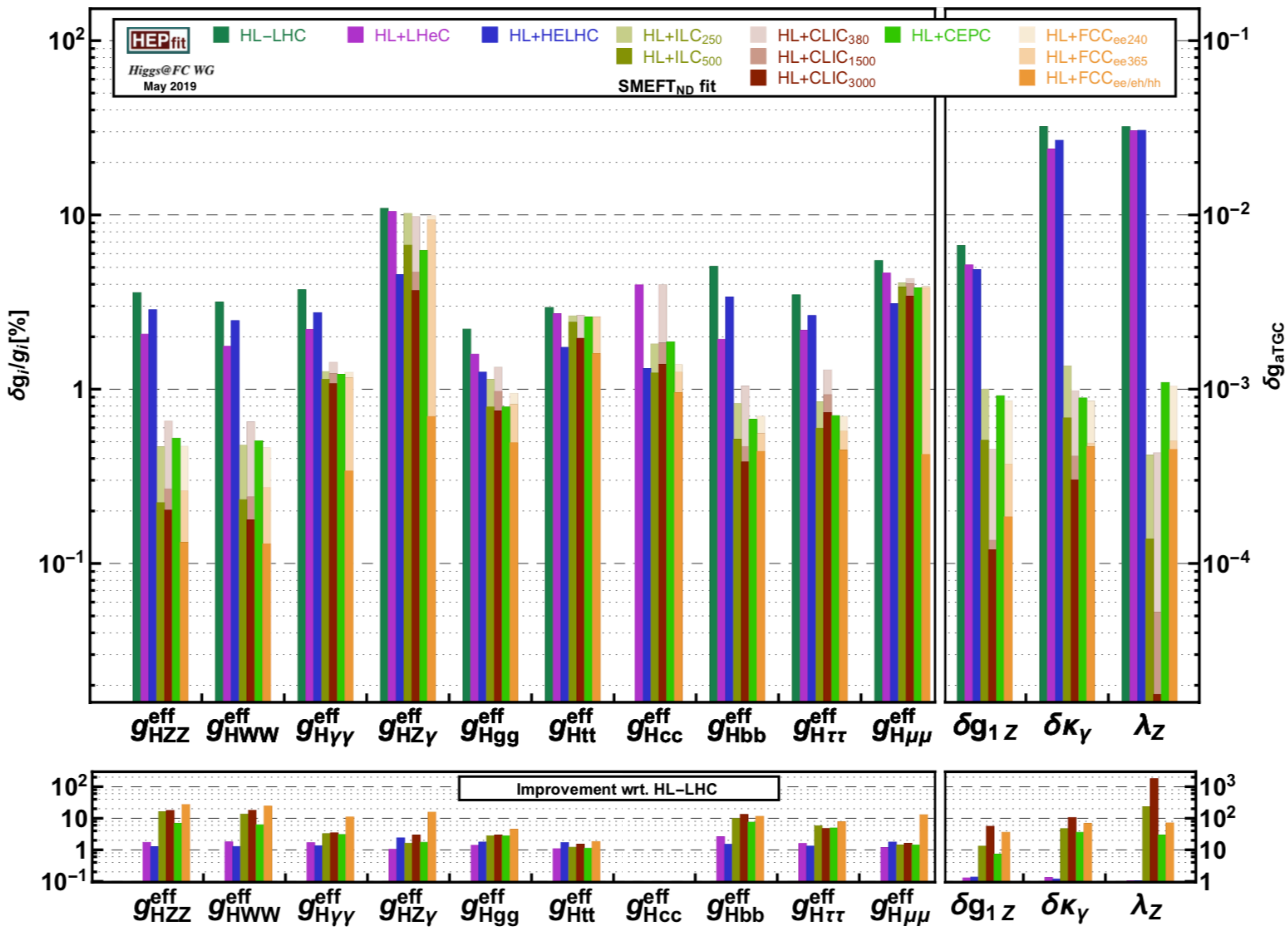
hZZ, hWW, hbb, h$\tau\tau$

h->invisible/exotic

#synergy:

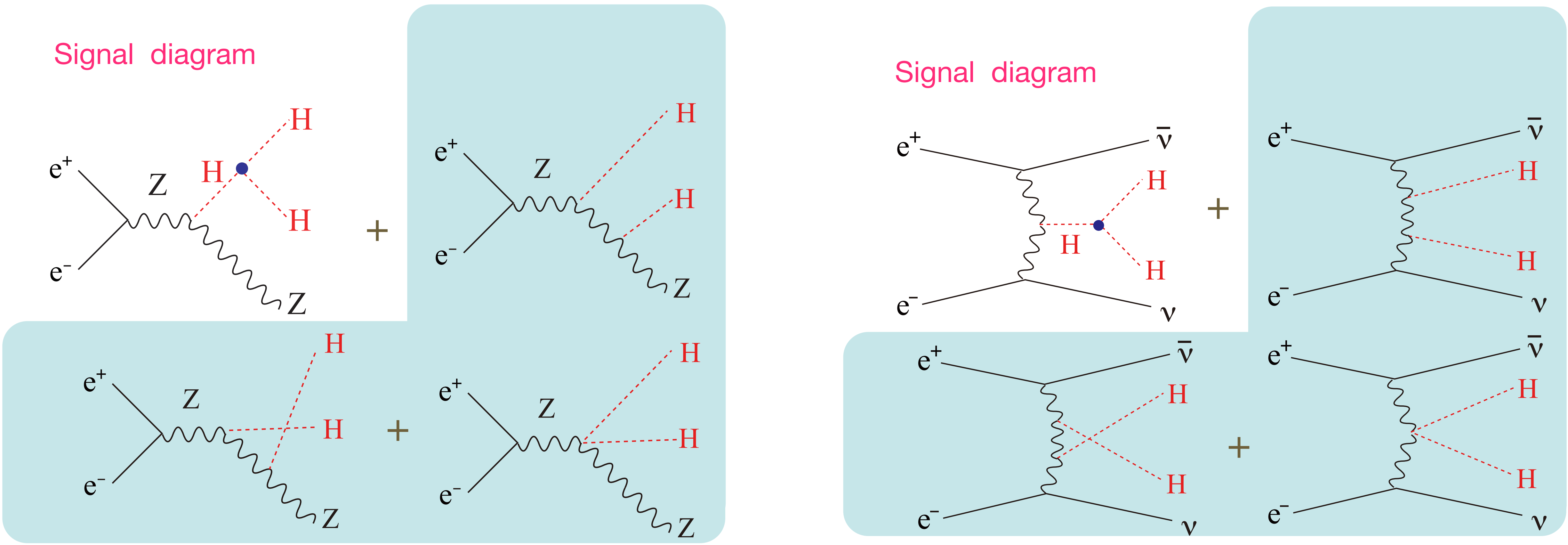
h$\gamma\gamma$, hγZ, h$\mu\mu$, htt, λ

precision at Higgs factories: European Strategy Update



(Physics Briefing Book, arXiv:1910.11775)

Higgs self-coupling determination in HH processes

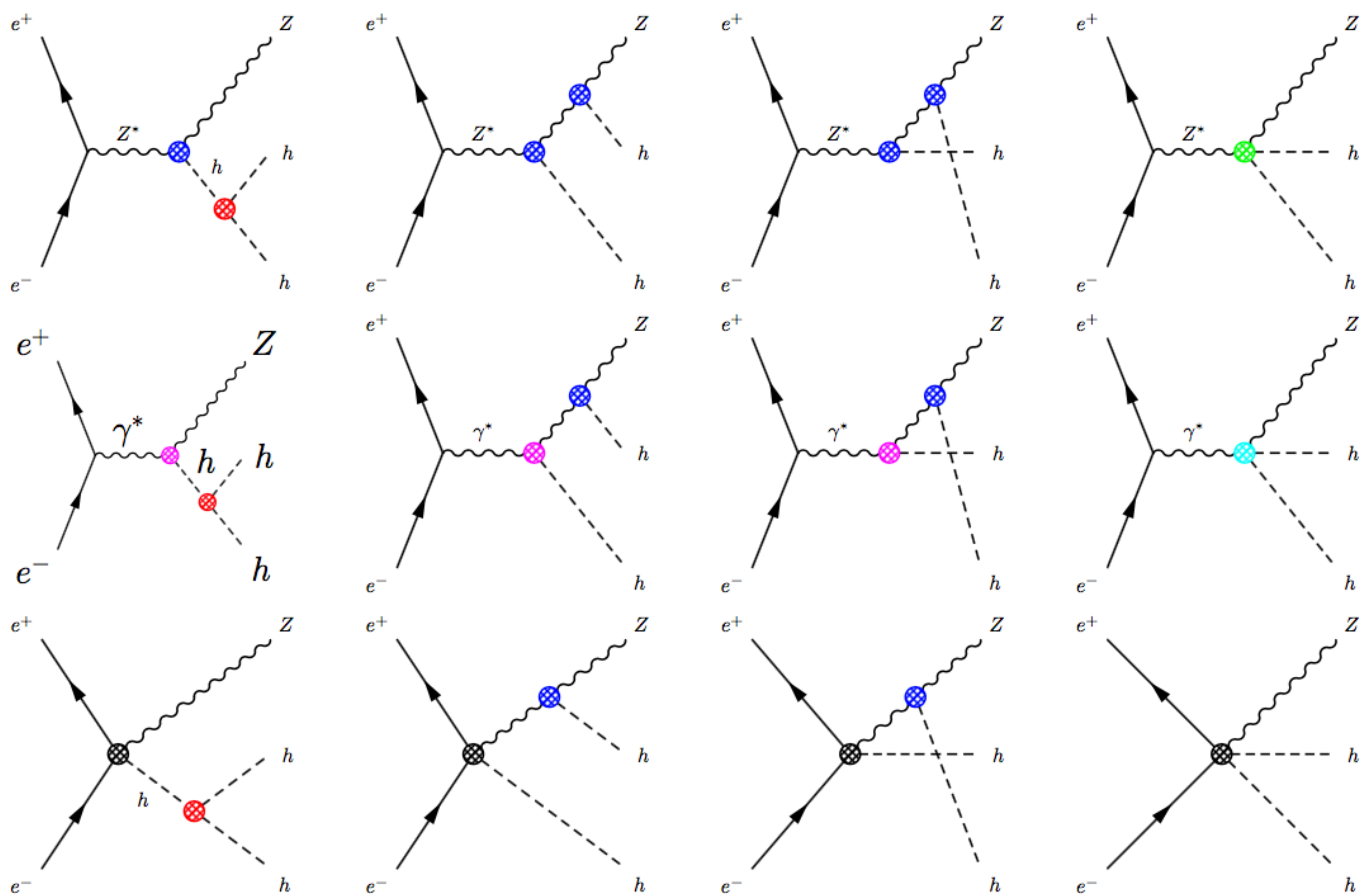


- classic studies always assume all the coupling except λ_{hhh} in these processes are fixed
- might be OK for many of the couplings, but definitely not obvious for ZZHH / WWHH couplings

λ_{hhh} model-independent determination in SMEFT (c_6)

$$\Delta\mathcal{L}_h = \; -(1+\eta_h)\bar{\lambda} v h^3 + \frac{\theta_h}{v} h\partial_\mu h \partial^\mu h$$

$$\eta_h = \delta\bar{\lambda} + \delta v - \frac{3}{2} c_H + c_6$$



λ_{hhh} model-independent determination in SMEFT (c_6)

(arXiv:1708.09079)

$$\frac{\sigma_{Zhh}}{\sigma_{SM}} - 1 = 0.565 c_6 - 3.58 c_H + 16.0(8c_{WW}) + 8.40(8c_{WB}) + 1.26(8c_{BB}) \\ -6.48 c_T - 65.1 c'_{HL} + 61.1 c_{HL} + 52.6 c_{HE},$$

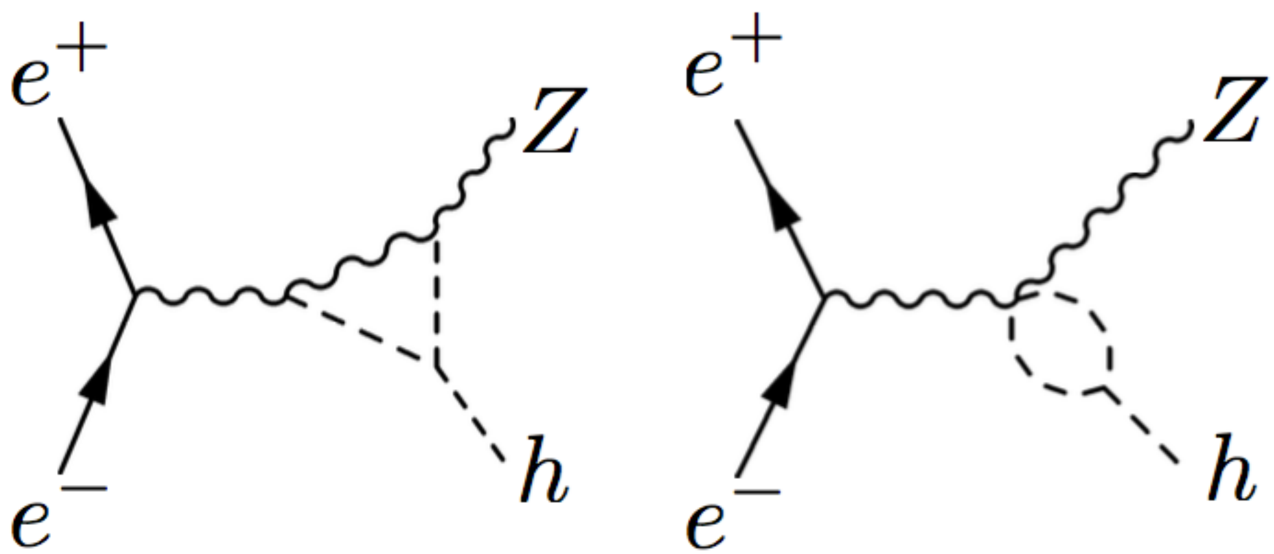
$$\Delta c_6 = \frac{1}{0.565}\left[\left(\frac{\Delta\sigma_{Zhh}}{\sigma_{SM}}\right)^2 + \sum_{i,j} a_i a_j (V_c)_{ij}\right]^{\frac{1}{2}}$$

(statistical error) (systematic error)

16.8% >> 2.0%

- interesting to prove this in e+e- → ννHH as well: still open
- another crucial question: can we do the same analysis to HH processes at hadron collider? can we still measure λ_{hhh} to 5% at FCC-hh?

λ_{hhh} determination in single-Higgs process



McCullough, arXiv:1312.3322

$$\delta_\sigma^{240} = 100\,(2\delta_Z + 0.014\delta_h)\,\%$$

- $\delta\sigma$ could receive contributions from many other sources

—> **δh ~ 500%** at 250GeV only; Gu, et al, arXiv:1711.03978

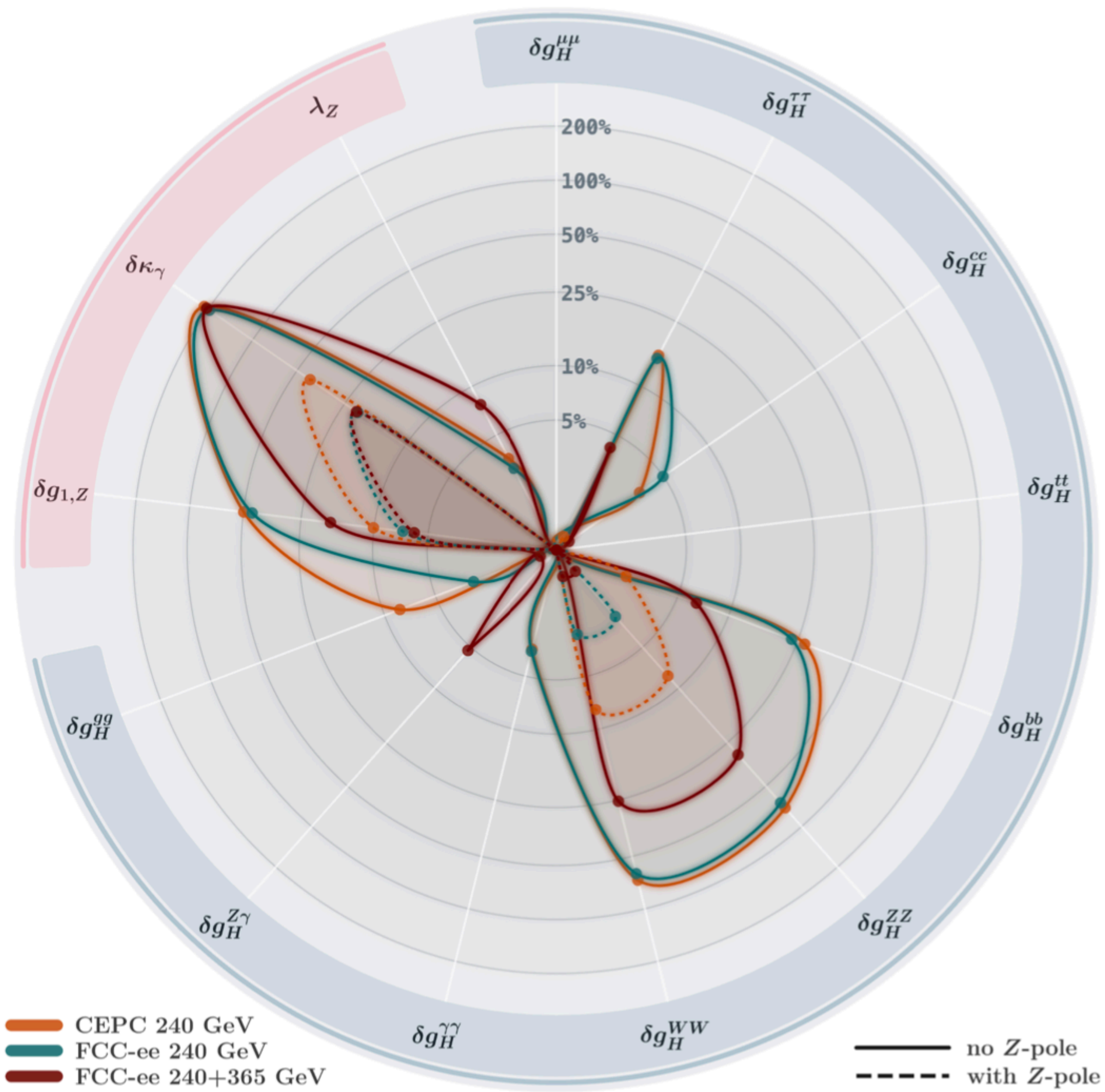
—> **δh ~ 50%** + 350/500GeV; Jung, Peskin, JT, paper in preparation

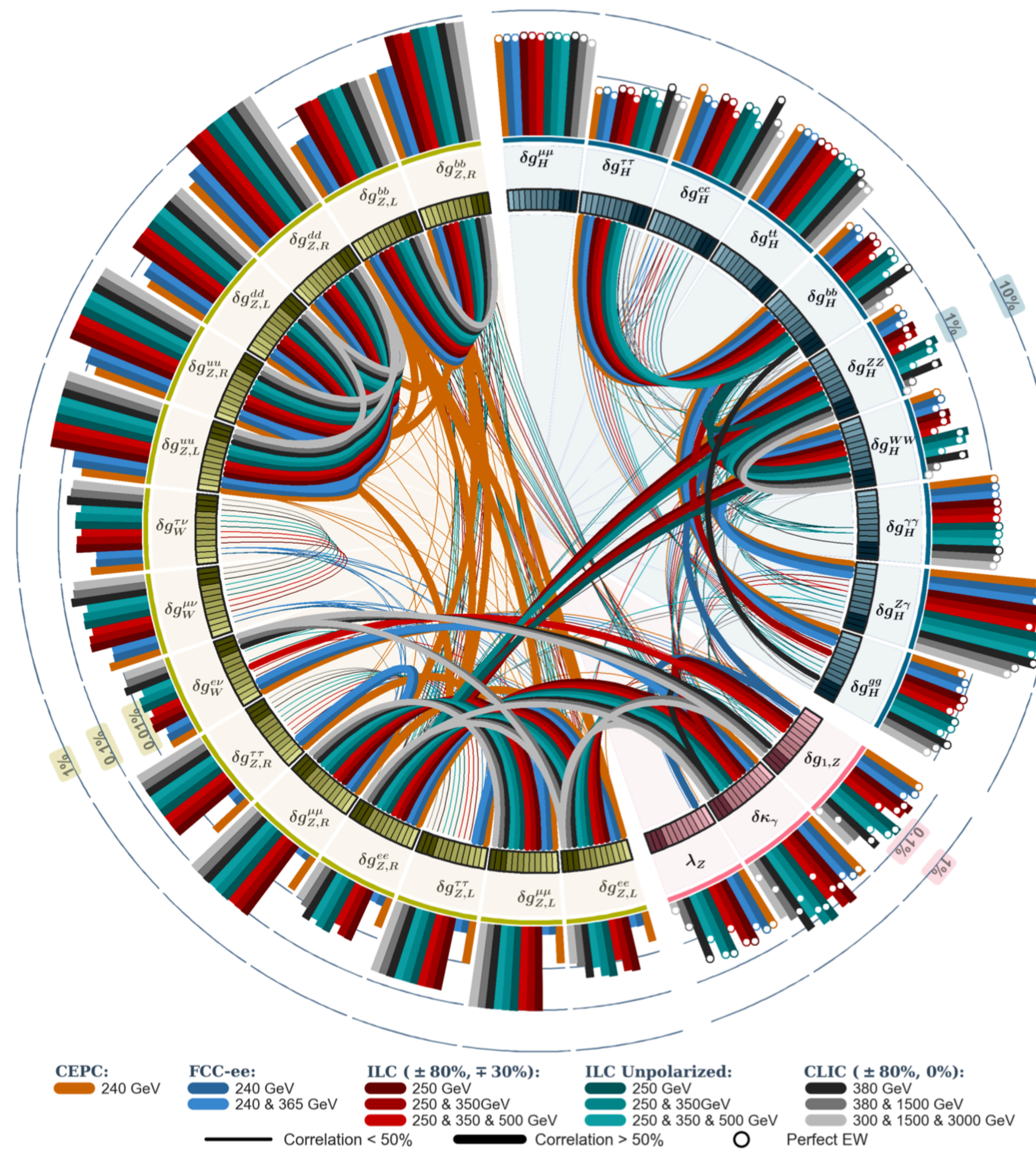
- open: what if we include other NLO effects as well?

ongoing work / open questions, biased by my own interests

(i) role of each measurement

(e.g. Grojean et al, arXiv:1907.04311)

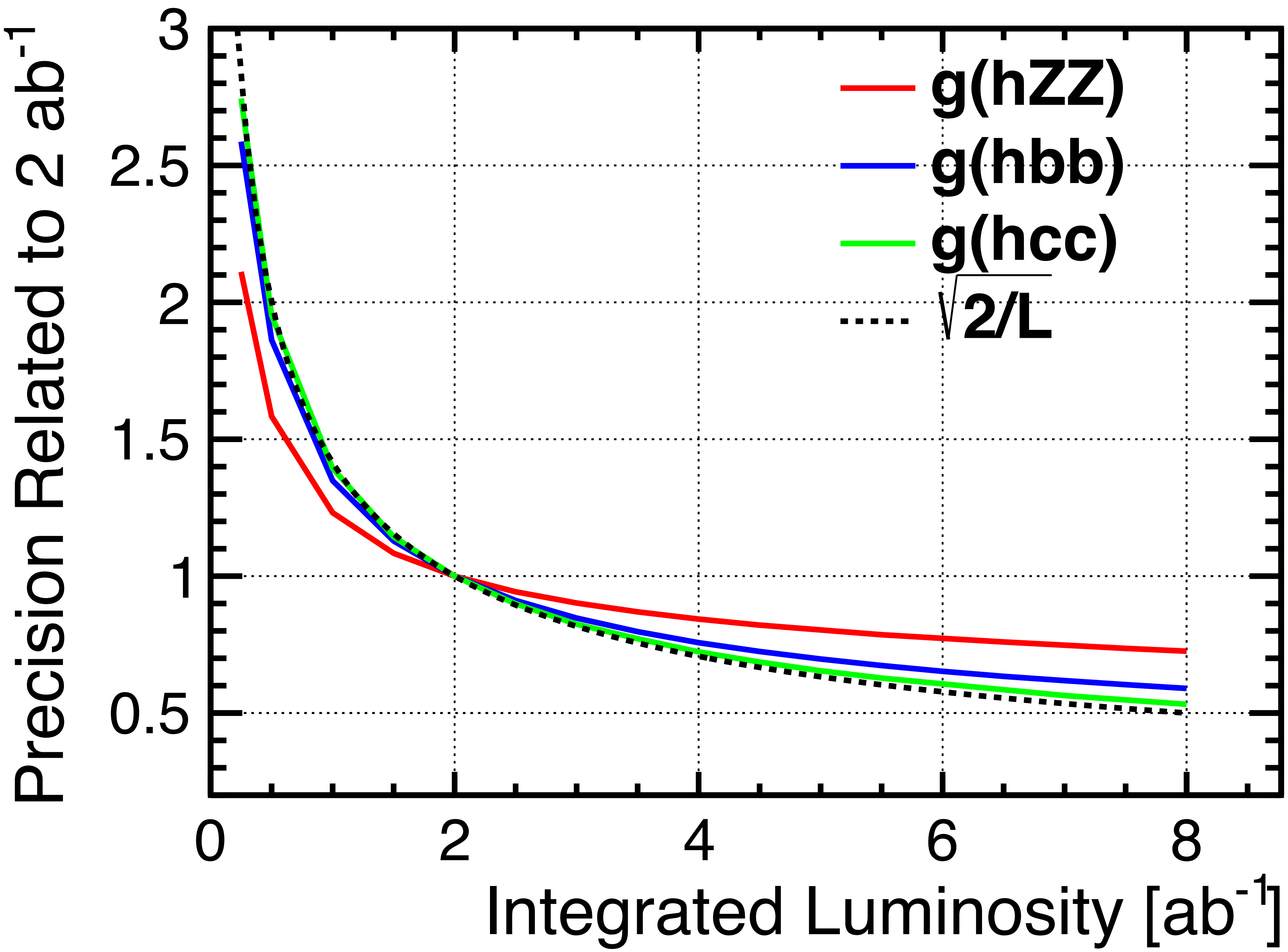




Is there an easier way?

role of each measurement: more transparent understanding

(Fujii, Peskin, JT, paper in preparation)



why not following $1/\sqrt{L}$? why so different for hZZ/hbb/hcc?

role of each measurement: more transparent understanding

New idea: express analytically uncertainty of every EFT coefficient or Higgs coupling directly by a set of input observables

for example: unpolarized e+e- at 250 GeV

$$\delta g_{hZZ} = \frac{1}{2}\delta\sigma_{Zh} + 6.4\delta\Gamma_l + 5.3\delta g_{Z,eff} - 0.015\delta R_{\gamma Z} - 2.4\delta\kappa_{A,eff} + 8.9\delta m_h + 0.098\delta A_l + \cdots$$

$$\delta X = \frac{\Delta X}{X}$$

σ_{Zh}	:	cross section of e+e- -> Zh
A_l, Γ_l	:	A_{LR} and Γ(Z->ll) at Z-pole
g_{Zeff}, κ_{Aeff}	:	Triple Gauge Couplings
$R_{\gamma Z}$	:	BR(h->γZ) / BR(h->ZZ*)
m_h	:	Higgs mass

role of each measurement: more transparent understanding

for example: unpolarized e+e- at 250 GeV

plug in measurement precisions for current EWPOs + 2 ab-1

$$\delta g_{hZZ} = \frac{1}{2}\delta\sigma_{Zh} + 6.4\delta\Gamma_l + 5.3\delta g_{Z,eff} - 0.015\delta R_{\gamma Z} - 2.4\delta\kappa_{A,eff} + 8.9\delta m_h + 0.098\delta A_l + \cdots$$

$$= 41 \oplus 66 \oplus 30 \oplus 23 \oplus 14 \oplus 11 \oplus 8.7 \oplus \cdots \times 10^{-4}$$

σ_{Zh} (41) | **EWPOs** (66) | **TGCs** (30) | **BR(h->γZ)** (23) | **Higgs mass** (11)

importance hierarchy

role of each measurement: more transparent understanding

for example: unpolarized e+e- at 250 GeV

plug in measurement precisions for current EWPOs + 2 ab-1

$$\delta g_{hbb} = \frac{1}{2}\delta B_{bb} - \frac{1}{2}\delta B_{WW} + \frac{1}{2}\delta\sigma_{Zh} - 5.79\delta\Gamma_l - 0.016\delta\Gamma_{\gamma Z} + \cdots$$

$$= 28 \oplus 91 \oplus 41 \oplus 59 \oplus 32 \oplus \cdots \times 10^{-4}$$

BR(h->bb) | **BR(h->WW)** | **σ_{Zh}** | **EWPOs** | **BR(h->γZ)**

role of each measurement: more transparent understanding

for example: unpolarized e+e- at 250 GeV

plug in measurement precisions for current EWPOs + 2 ab-1

$$\delta g_{hcc} = \frac{1}{2}\delta B_{cc} - \frac{1}{2}\delta B_{WW} + \frac{1}{2}\delta\sigma_{Zh} - 5.79\delta\Gamma_l - 0.016\delta\Gamma_{\gamma Z} + \cdots$$

$$= 160 \oplus 91 \oplus 41 \oplus 59 \oplus 32 \oplus \cdots \times 10^{-4}$$

BR(h->cc)

BR(h->WW)

σ_{Zh}

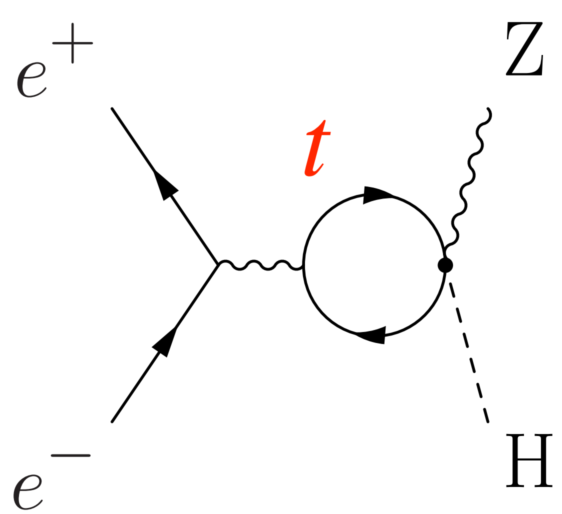
EWPOs

BR(h->γZ)

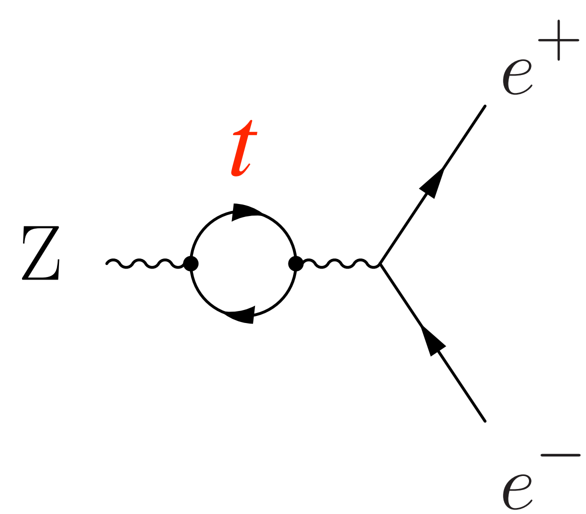
stay tuned

(ii) what happens at next leading order for SMEFT fit

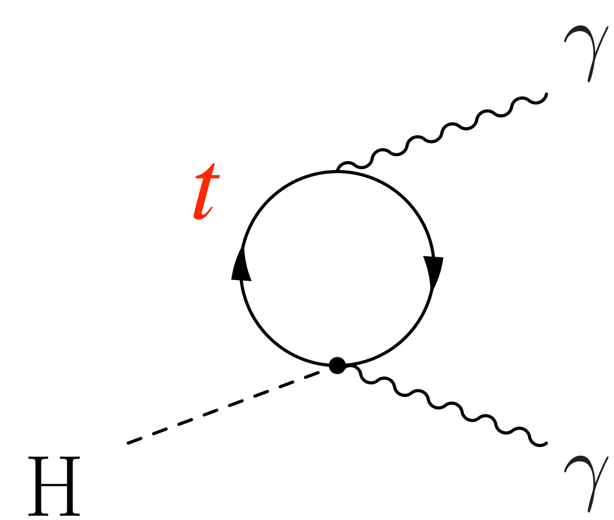
- at e+e-, NLO ~ O(α), 1% level
- for NLO from W/Z/γ/H operators overall effect will be < 0.1%
- for NLO from top, operators would be much less constrained, currently ~ O(1) -> overall effect 1% -> potential impact in global fit



$\mathcal{O}_{Ht} = (\Phi^\dagger i \overleftrightarrow{D}_\mu \Phi)(\bar{t}\gamma^\mu t)$



$\mathcal{O}_{Hq}^{(3)} = (\Phi^\dagger i \overleftrightarrow{D}^a_\mu \Phi)(\bar{Q}\gamma^\mu \tau^a Q)$



$\mathcal{O}_{tB} = (\bar{Q}\sigma^{\mu\nu} t)\tilde{\Phi} B_{\mu\nu}$

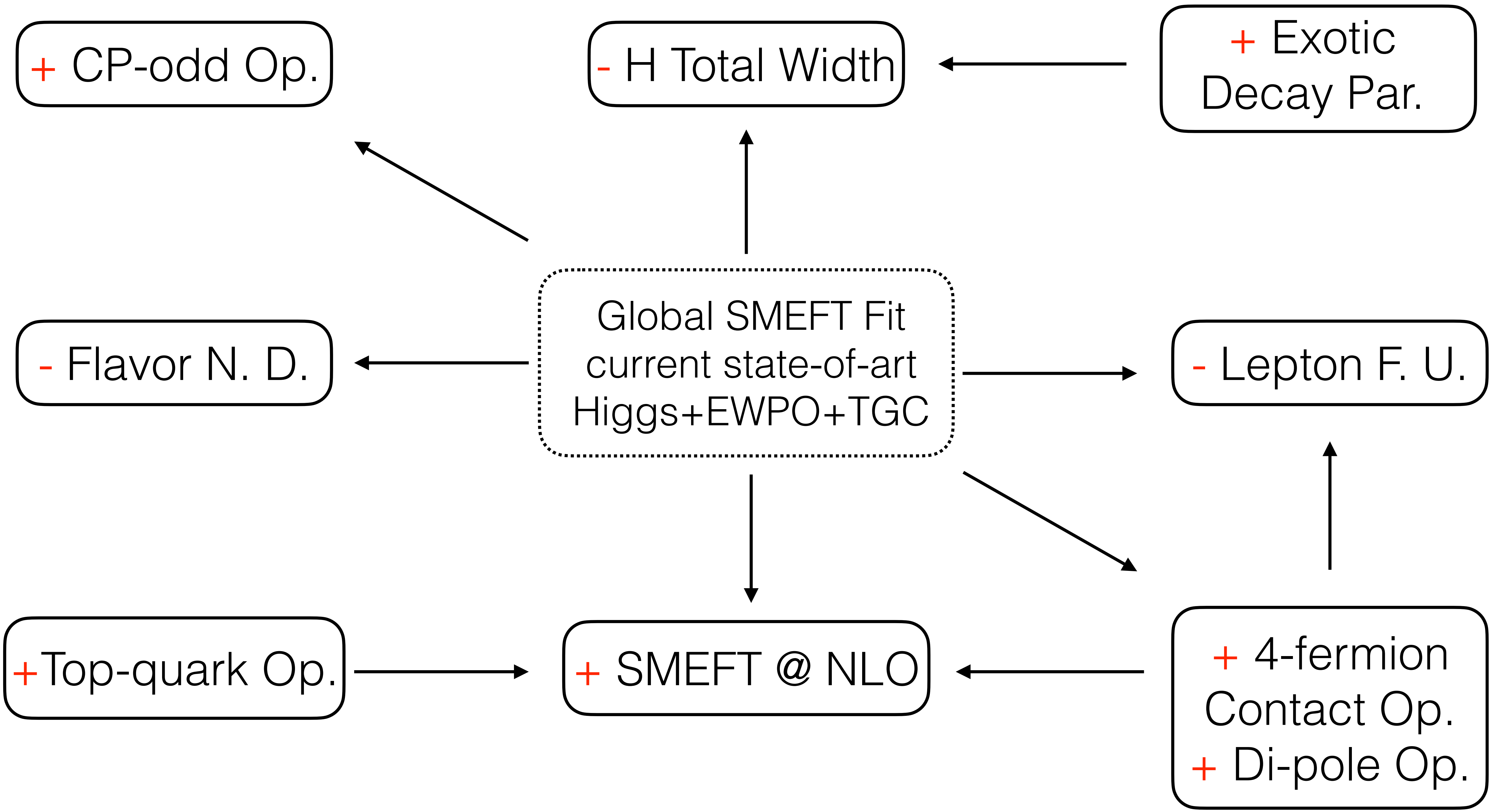
Higgs, top and electro-weak precision measurements at future e^+e^- colliders; a combined effective field theory analysis with renormalization mixing

arXiv:2020.XXXX

Sunghoon Jung,[a] Junghwan Lee,[a] Martin Perelló,[b] Junping Tian,[c] Marcel Vos[b]

- with the same set of observables, at 250 GeV running only, the global fit will not converge at any of the Higgs factories
- e.g. Higgs couplings could not be determined unambiguously
- unless (luckily) we can use top-quark measurements at LHC/HL-LHC
- Higgs coupling precisions will not fully restored unless we have e+e- →t t-bar data (Energy Upgrade is really desirable)

(iii) SMEFT fit: go even more model-independently

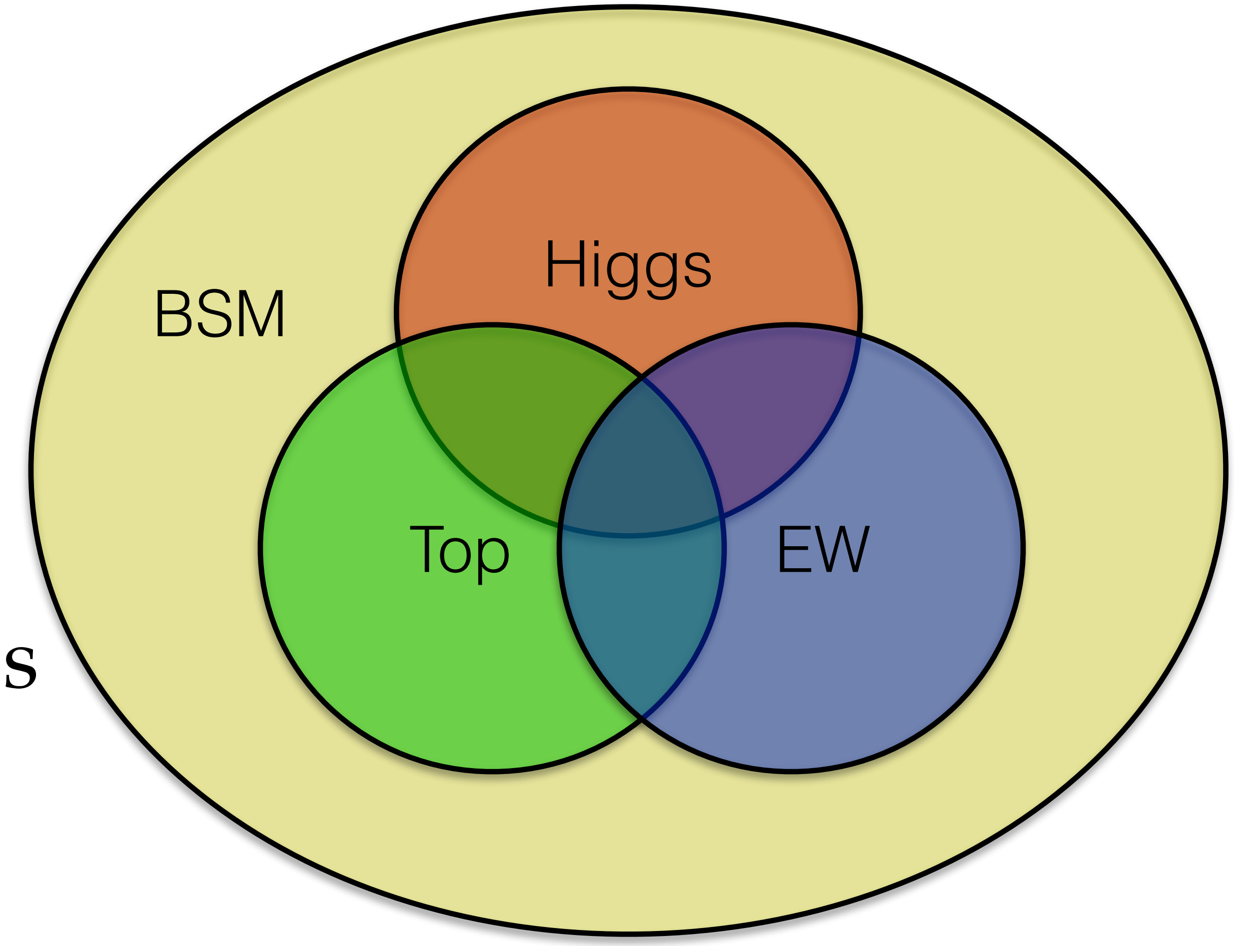


welcome to join Snowmass EF04 Topical Group (conveners: A.Belloni, A.Freitas, JT)

summary

- The capabilities of future Higgs factories are best represented in SMEFT formalism

- EWPO/TGC/Top/Beam polarization all play important roles in model-independent determination of Higgs couplings



- SMEFT provides a global view in searching for BSM, and is able to bring together consistently measurements from not only at LHC & future e+e-, but essentially all HEP experiments

- Proposed Higgs factories can deliver 1% or below precision for many Higgs couplings already at $\sqrt{s} = 250$ GeV $\rightarrow$ go ahead!

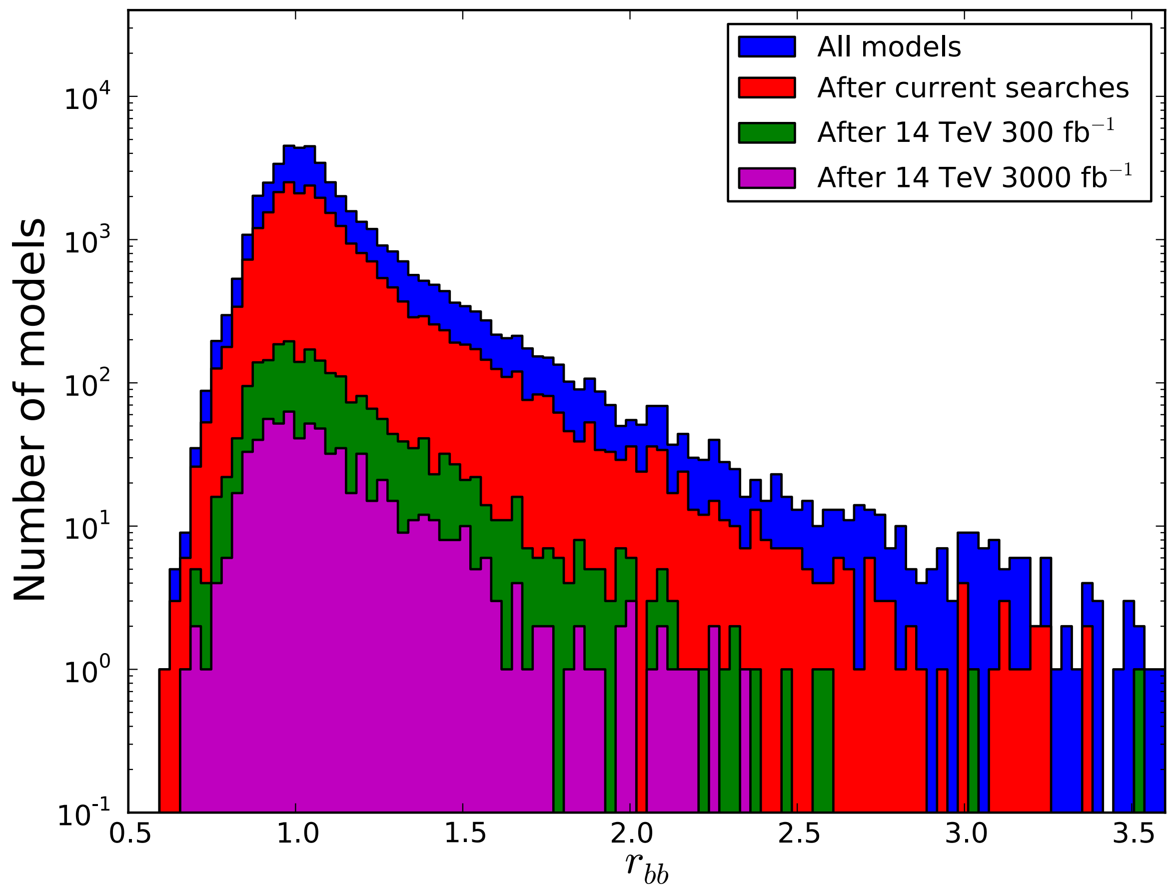
backup

Brief update on the ILC status and transition

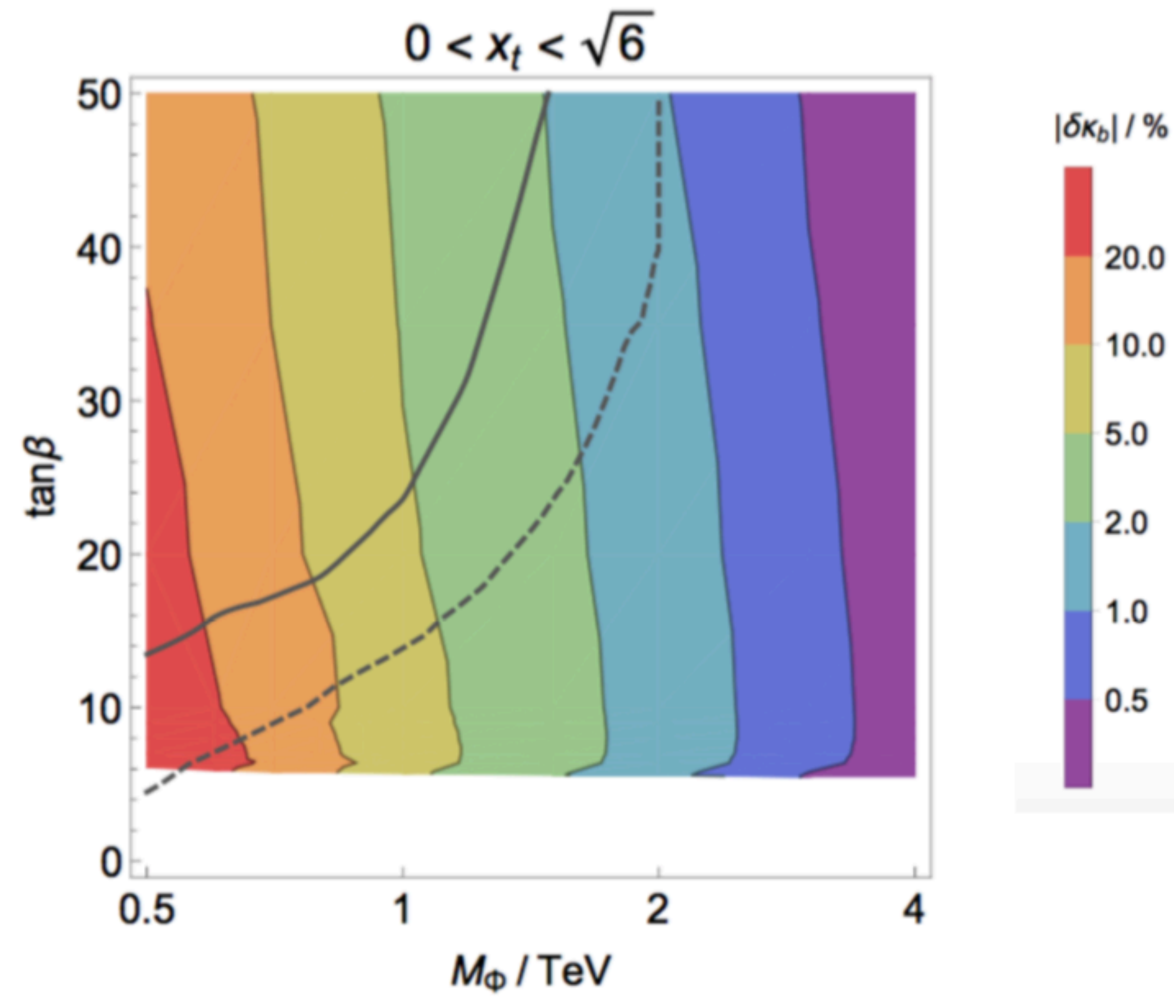
courtesy of Jim Brau/Keisuke Fujii

- October/Ncvember, 2019 — LCWS in Sendai
  - Strong statements supporting ILC (Diet, ICFA, etc.)
  - including expression of interest by Melinda Pavek representing US State Department
- Science Council of Japan (SCJ) Master Plan concluded in January.
  - ILC selected as project for hearing, **recognizing scientific merit,** although not on list limited to smaller projects.
  - This **recognition** moves project to next level of consideration.
- ICFA meeting in February. *ICFA statement on ILC*
  - **H. Masuko**, Deputy-Director General, MEXT.
  - **T. Kawamura**, Chairperson of the Federation of Diet Members for the ILC.
  - **Chris Fall,** Director of US DOE Office of Science
- Transition from LCC to Pre-laboratory soon. Being planned.

direct and indirect discoveries: complementarity



Cahill-Rowley, et al, arXiv:1308.0297



Wells, Zhang, arXiv:1711.04774

an orthogonal way to discoveries w.r.t. direct search:

precision Higgs couplings

strategy to determine all the 23 parameters

- m_W and $\alpha(m_Z)$ -> g, g';
- G_F -> v; m_h -> λ; m_Z -> c_T;
- A_l and Γ_l -> $c_{HL}+c_{HL}'$, c_{HE};
- Γ_W and Γ_Z -> c_W, c_Z;

- g_{1Z} -> c_{HL}'; κ_γ -> c_{WB}; κ_λ -> c_{3W};

- $BR(h\to\gamma\gamma)$ and $BR(h\to\gamma Z)$ -> c_{BB}, c_{WW};
- σ_{ZH} -> c_H; σ_{ZHH} -> c_6;
- $BR(h\to bb/cc/gg/\mu\mu/\tau\tau)$ -> y_b, y_c, c_g, y_μ, y_τ;
- *BR(h->invisible)* and *BR(h->other)*;
- c_{WW} is helped by A_{LR} in σ_{ZH}, angular meas., W-fusion;
- $c_{HL}/c_{HL}'/c_{HE}$ are helped by A_{LR} in σ_{ZH}

(iv) Higgs CP measurement

- find CP-violating source in Higgs sector —> EW baryongenesis
- essential to understand structures of all Higgs couplings

through H—>$\tau^+\tau^-$
(or ttH)

$$L_{Hff} = -\frac{m_f}{v} H \bar{f} (\cos\Phi_{CP} + \underline{i\gamma^5 \sin\Phi_{CP}}) f$$

$$\Delta\Phi_{CP} \sim 4.3^\circ$$

Jeans et al, 1804.01241

through HZZ/HWW

$$L_{HVV} = 2C_V M_V^2 (\frac{1}{v} + \frac{a}{\Lambda}) H V_\mu V^\mu + C_V \frac{b}{\Lambda} H V_{\mu\nu} V^{\mu\nu} + \underline{C_V \frac{\tilde{b}}{\Lambda} H V_{\mu\nu} \tilde{V}_{\mu\nu}}$$

(CP-odd)

$\Delta\tilde{b} \sim 0.016$ (for Λ=1TeV)

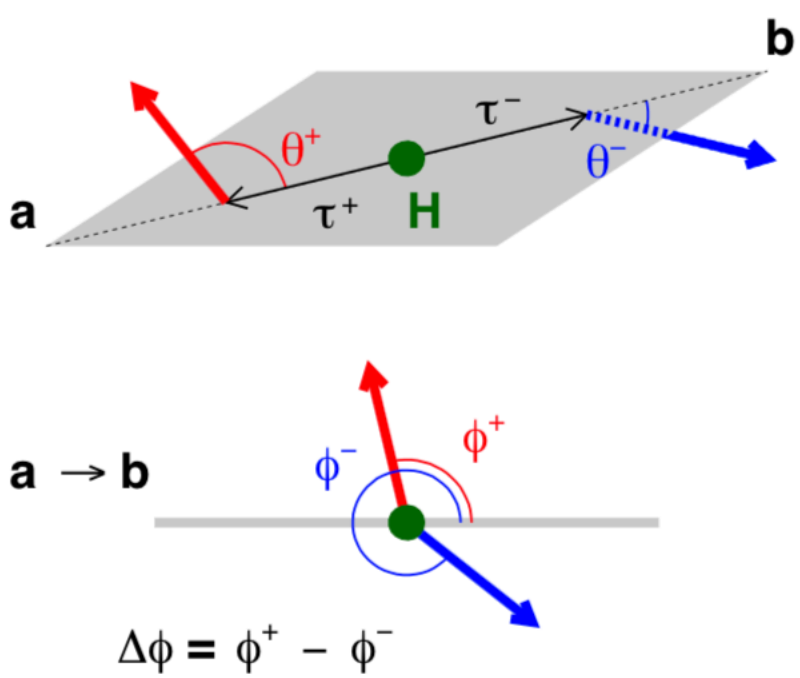
Ogawa, 1712.09772

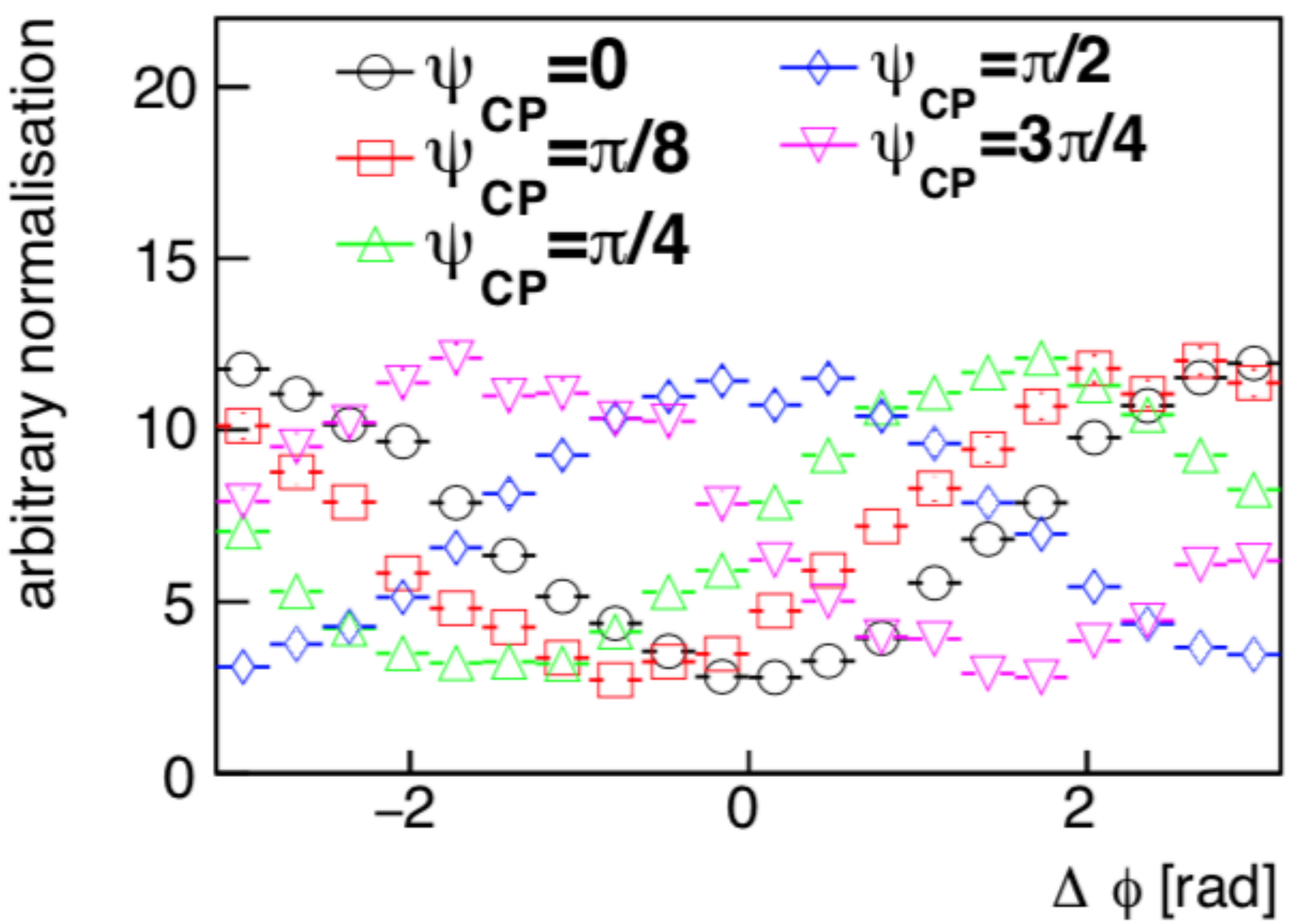
open: how can we combine the sensitivities? (need to do in concrete models)

(ii-4) Higgs CP in $H \to \tau^+\tau^-$

- CP is essential to understand structures of all Higgs couplings

$$L_{Hff} = -\frac{m_f}{v} H \bar{f} (\cos \Phi_{CP} + i\gamma^5 \sin \Phi_{CP}) f$$





$$\Delta\Phi_{CP} \sim 4.3^\circ$$

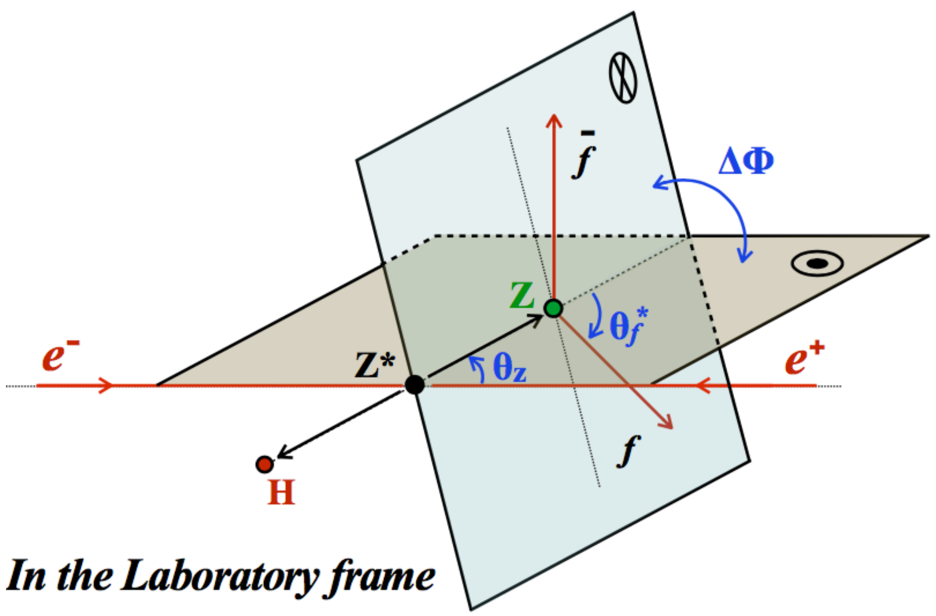
Jeans et al, arXiv:1804.01241

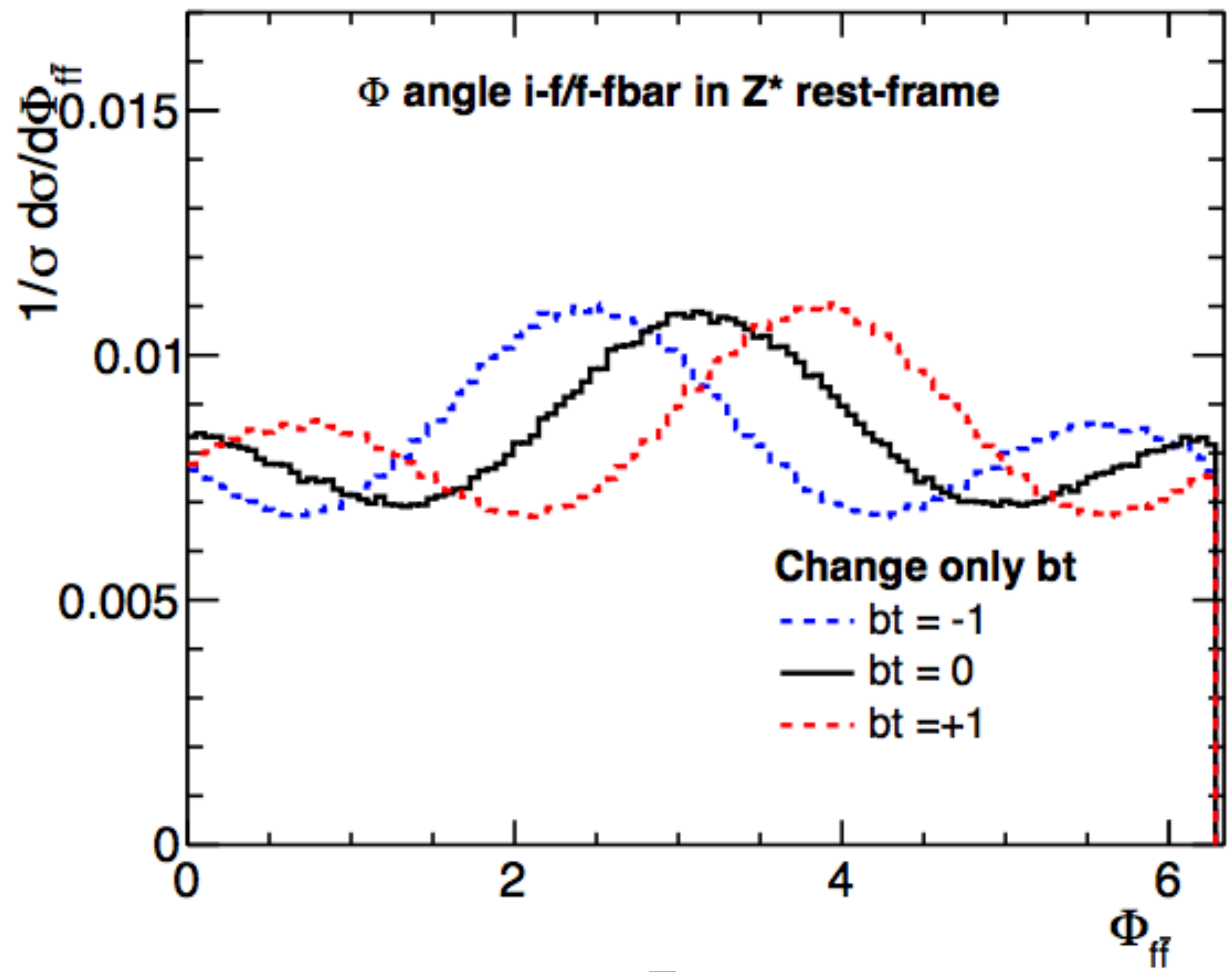
(ii-4) Higgs CP in HZZ coupling

$$L_{hZZ} = M_Z^2(\frac{1}{v} + \frac{a}{\Lambda})hZ_\mu Z^\mu + \frac{b}{2\Lambda}hZ_{\mu\nu}Z^{\mu\nu} + \frac{\tilde{b}}{2\Lambda}hZ_{\mu\nu}\tilde{Z}_{\mu\nu}$$

(CP-odd)

$$e^+ + e^- \to Zh \to f\bar{f}h$$





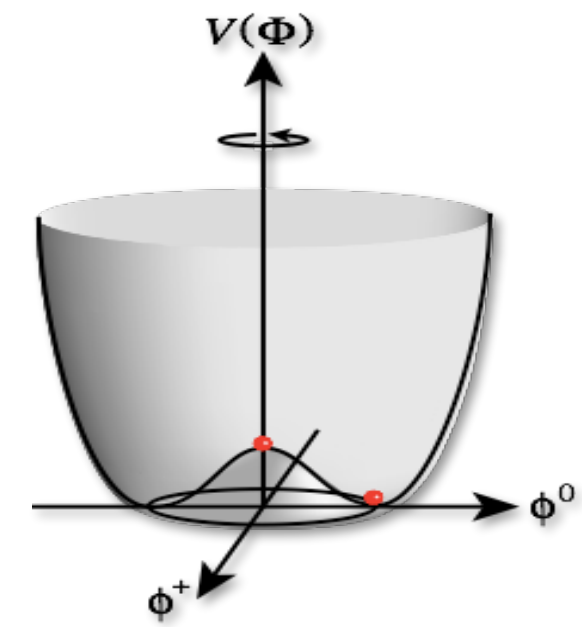
@ $\sqrt{s} = 250\text{GeV}$

$\Delta\tilde{b} \sim 0.016$ (for Λ=1TeV)

Ogawa et al, arXiv:1712.09772

(vi) Higgs self-coupling

- direct probe of the Higgs potential
- large deviation (> 20%) motivated by electroweak baryongenesis, could be ~100%
- √s>=500 GeV, e+e- —> ZHH
- √s>=1 TeV, e+e- —> vvHH (WW-fusion)

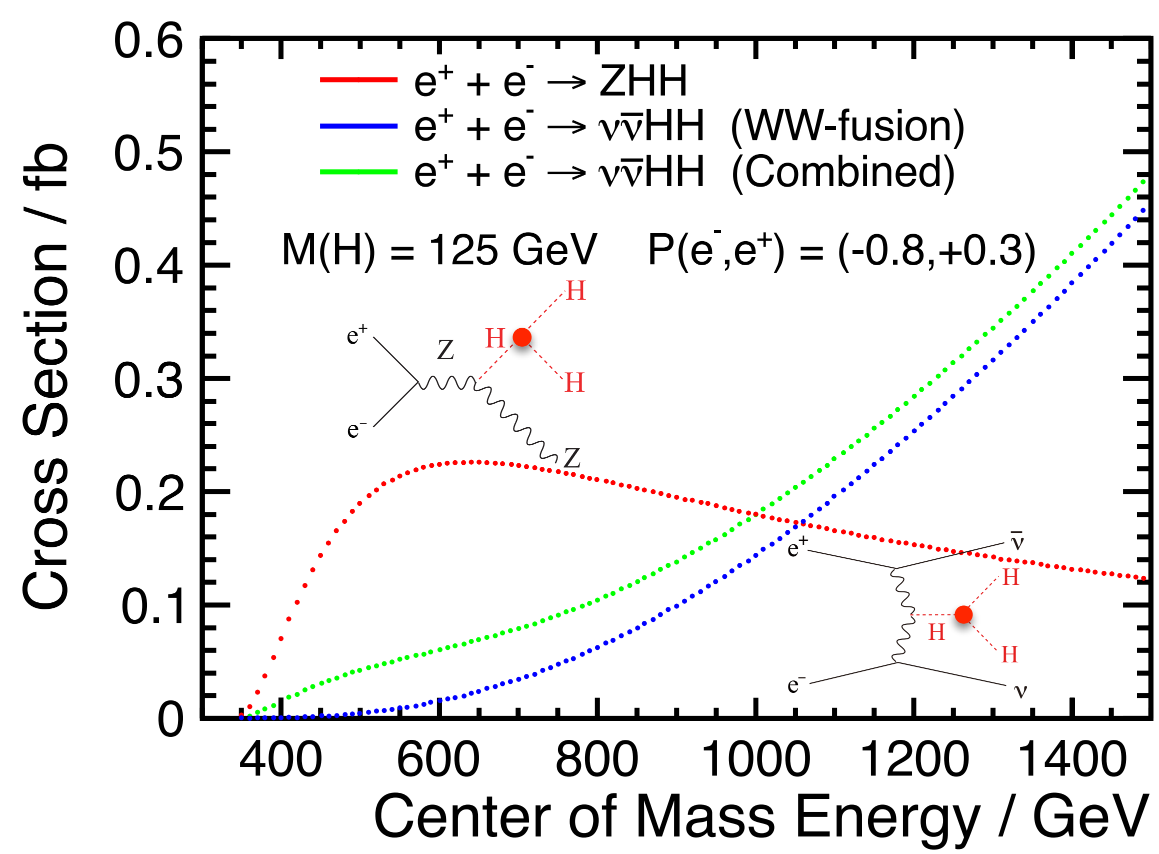


ILC

$\Delta\lambda_{HHH}/\lambda_{HHH}$	500 GeV	+ 1 TeV
H20	27%	10%

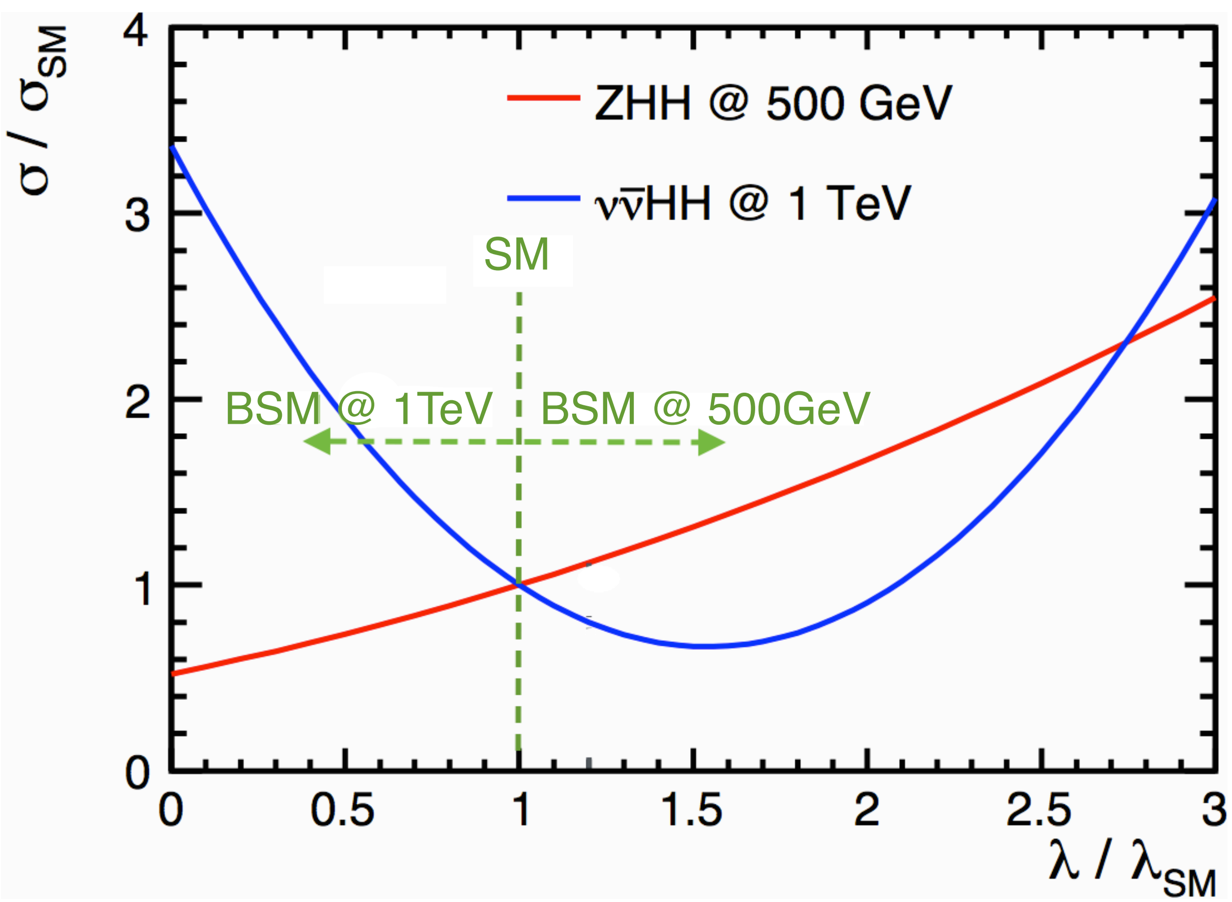
CLIC

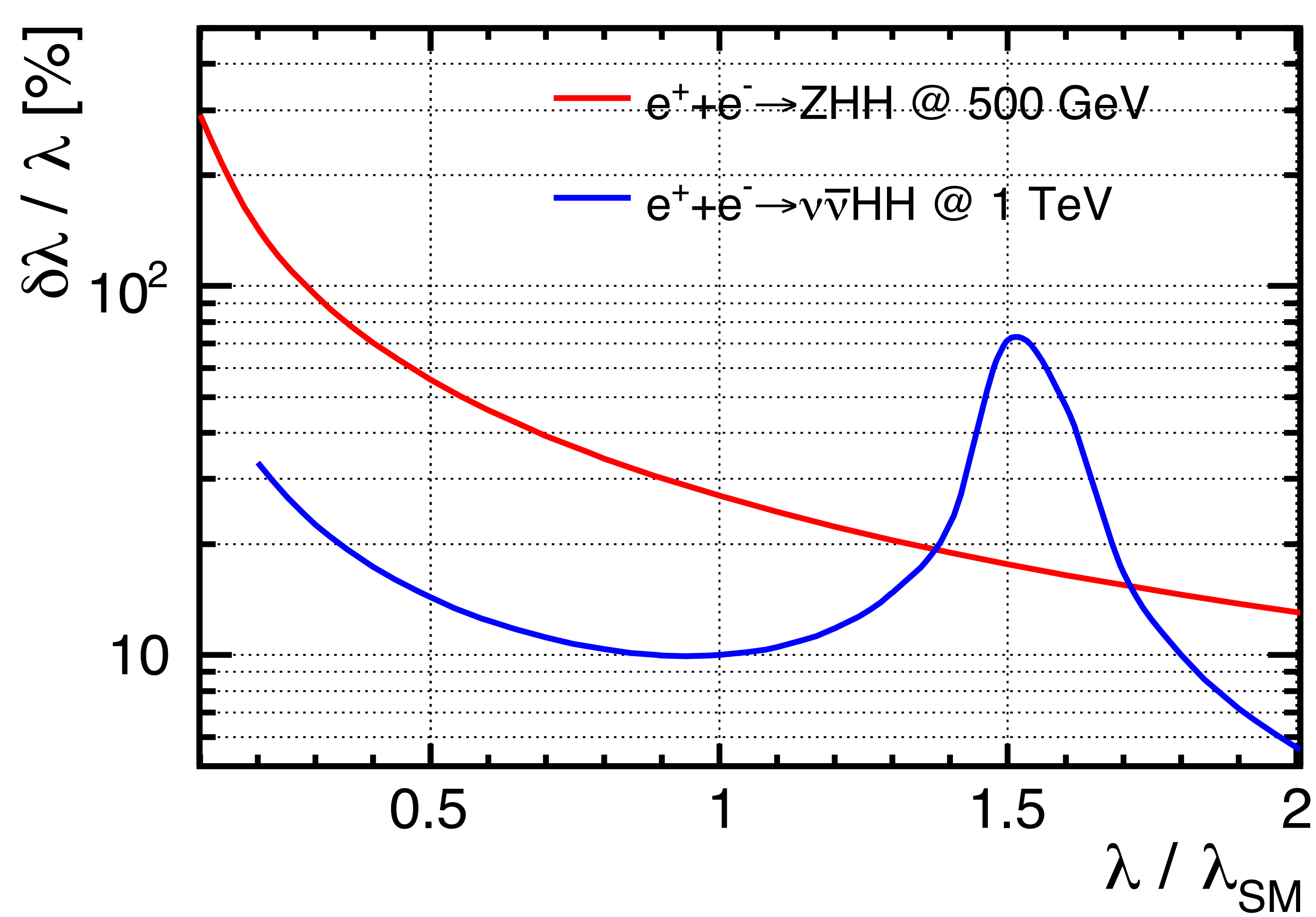
1.5 TeV	+3 TeV
36%	10%



Higgs self-coupling: when $\lambda_{HHH} \neq \lambda_{SM}$?

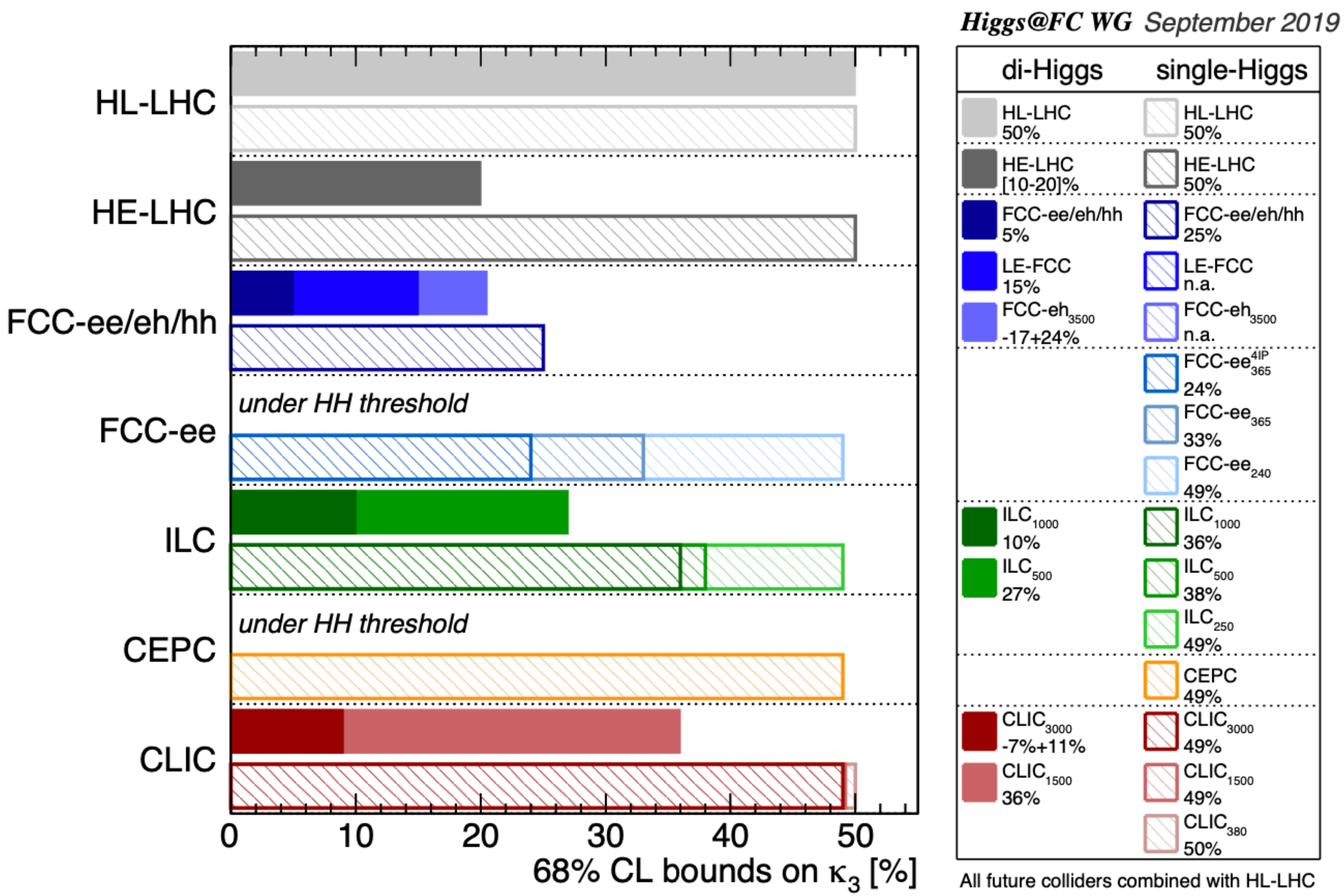
- constructive interference in ZHH, while destructive in vvHH (& LHC) —> complementarity between ILC & LHC, between √s ~500 GeV and >1TeV
- if $\lambda_{HHH} / \lambda_{SM} = 2$, Higgs self-coupling can be measured to ~15% using ZHH at 500 GeV e+e-





Duerig, Tian, et al, paper in preparation

λ_{hhh} by double / single Higgs processes



(Physics Briefing Book, arXiv:1910.11775)

role of each measurement: more transparent understanding

for example: **polarized** e+e- at 250 GeV

plug in measurement precisions for current EWPOs + 2 ab-1

$$\delta g_{hZZ} = \frac{1}{2}\delta\sigma_{Zh}^{R} + 0.35\delta A_l + 3.6\delta\kappa_{A,eff} - 4.0\delta g_{Z,eff} - 1.8\delta\Gamma_l + 8.9\delta m_h + \cdots$$

$$= 51 \oplus 31 \oplus 20 \oplus 17 \oplus 18 \oplus 11 \oplus \cdots \times 10^{-4}$$

σ_{Zh}

A_{LR}

TGCs

TGCs

Γ_l

Higgs mass

importance hierarchy

benchmark BSM models

	Model	$b\bar{b}$	$c\bar{c}$	gg	WW	$\tau\tau$	ZZ	$\gamma\gamma$	$\mu\mu$
1	MSSM [34]	+4.8	-0.8	- 0.8	-0.2	+0.4	-0.5	+0.1	+0.3
2	Type II 2HD [36]	+10.1	-0.2	-0.2	0.0	+9.8	0.0	+0.1	+9.8
3	Type X 2HD [36]	-0.2	-0.2	-0.2	0.0	+7.8	0.0	0.0	+7.8
4	Type Y 2HD [36]	+10.1	-0.2	-0.2	0.0	-0.2	0.0	0.1	-0.2
5	Composite Higgs [38]	-6.4	-6.4	-6.4	-2.1	-6.4	-2.1	-2.1	-6.4
6	Little Higgs w. T-parity [39]	0.0	0.0	-6.1	-2.5	0.0	-2.5	-1.5	0.0
7	Little Higgs w. T-parity [40]	-7.8	-4.6	-3.5	-1.5	-7.8	-1.5	-1.0	-7.8
8	Higgs-Radion [41]	-1.5	- 1.5	10.	-1.5	-1.5	-1.5	-1.0	-1.5
9	Higgs Singlet [42]	-3.5	-3.5	-3.5	-3.5	-3.5	-3.5	-3.5	-3.5

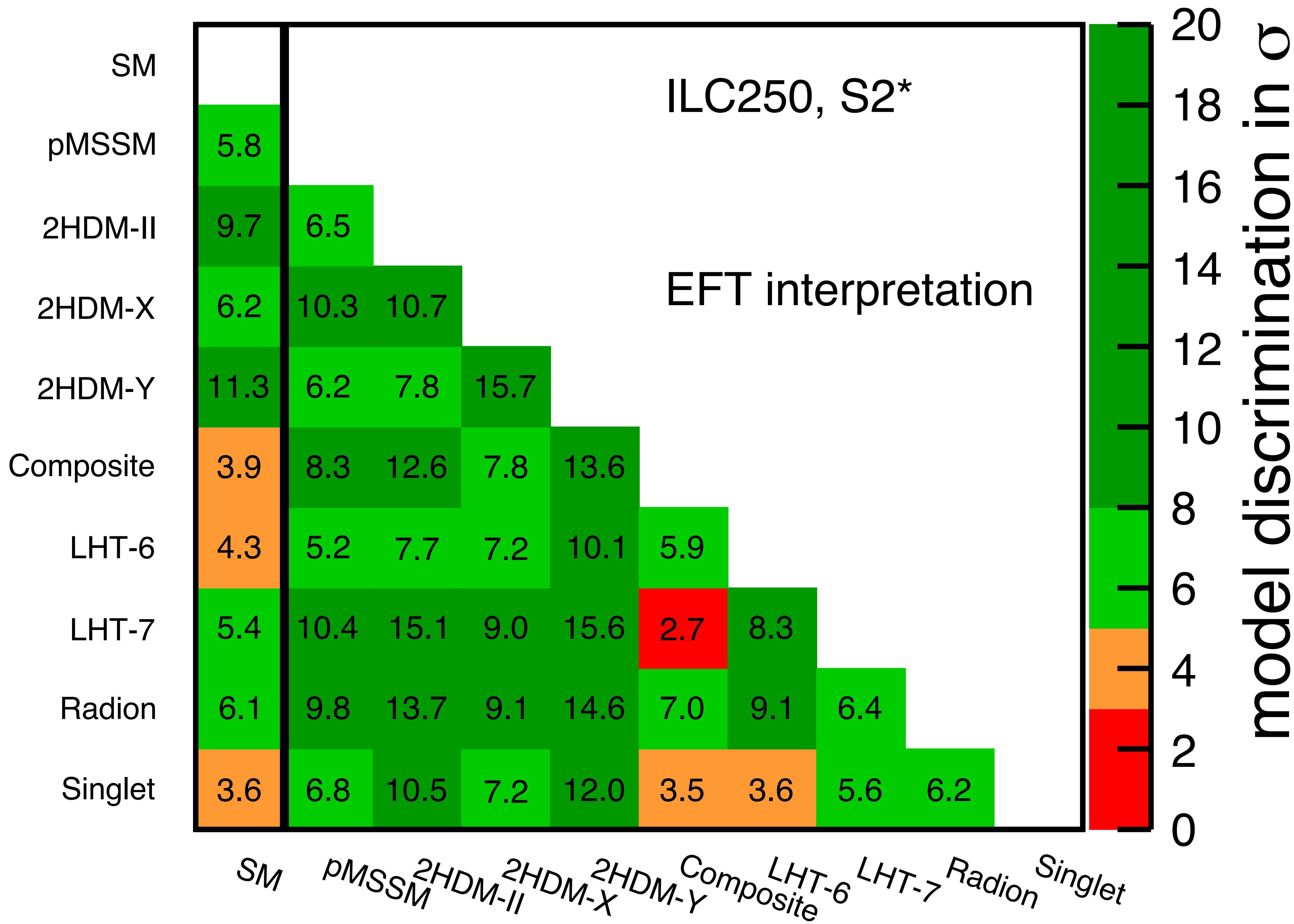
Table 4: Deviations from the Standard Model predictions for the Higgs boson couplings, in %, for the set of new physics models described in the text. As in Table 1, the effective couplings $g(hWW)$ and $g(hZZ)$ are defined as proportional to the square roots of the corresponding partial widths.

—> quantitative assessment for models discrimination

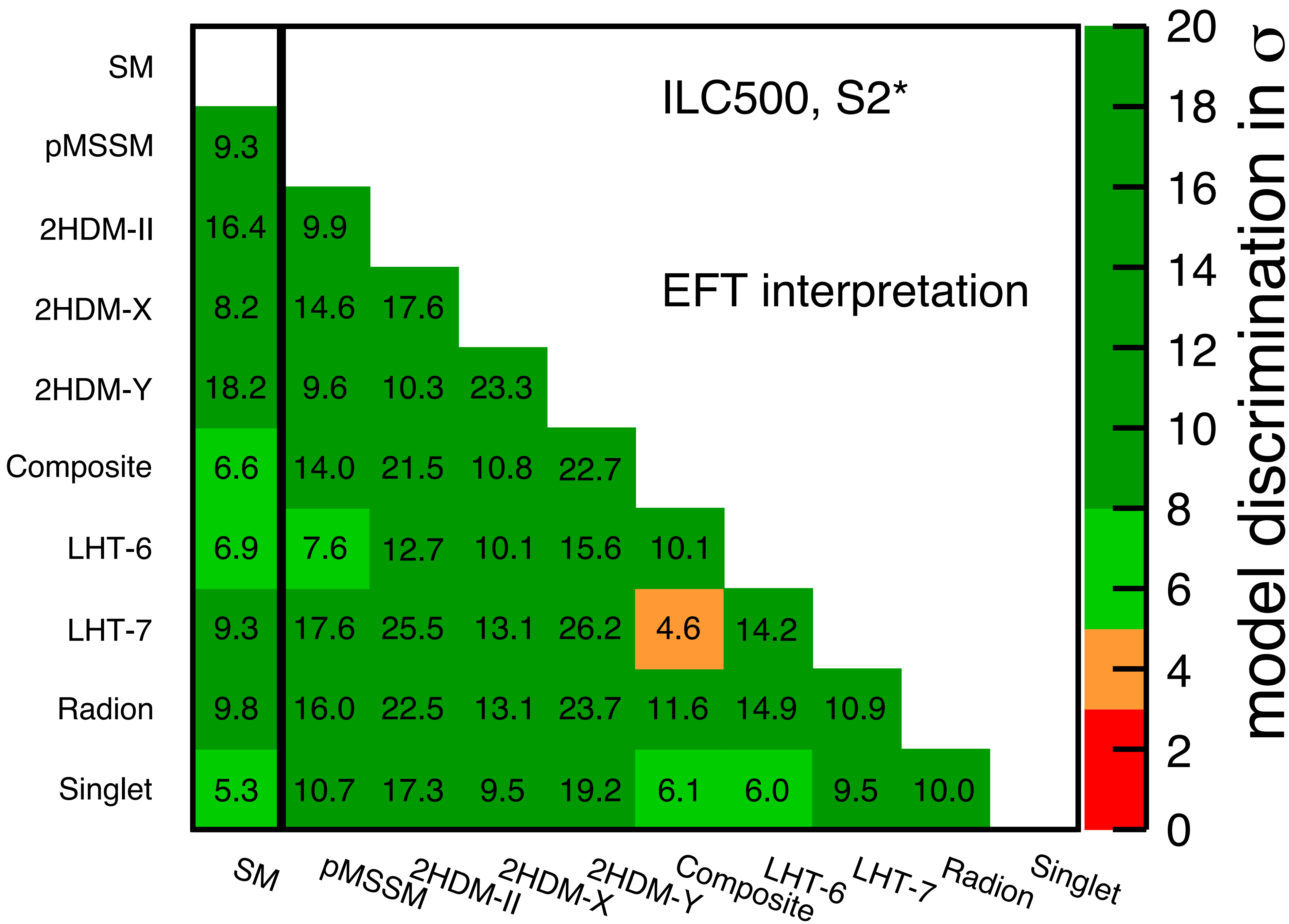
model parameters (chosen as escaping direct search at HL-LHC)

- a PMSSM model with b squarks at 3.4 TeV, gluino at 4 TeV
- a Type II 2 Higgs doublet model with $m_A = 600 \text{ GeV}, \tan\beta = 7$
- a Type X 2 Higgs doublet model with $m_A = 450 \text{ GeV}, \tan\beta = 6$
- a Type Y 2 Higgs doublet model with $m_A = 600 \text{ GeV}, \tan\beta = 7$
- a composite Higgs model MCHM5 with $f = 1.2 \text{ TeV}, m_T = 1.7 \text{ TeV}$
- a Little Higgs model with T-parity with $f = 785 \text{ GeV}, m_T = 2 \text{ TeV}$
- A Little Higgs model with couplings to 1st and 2nd generation with $f = 1.2 \text{ TeV}, m_T = 1.7 \text{ TeV}$
- A Higgs-radion mixing model with $m_r = 500 \text{ GeV}$
- a model with a Higgs singlet at 2.8 TeV creating a Higgs portal to dark matter and large λ for electroweak baryogenesis

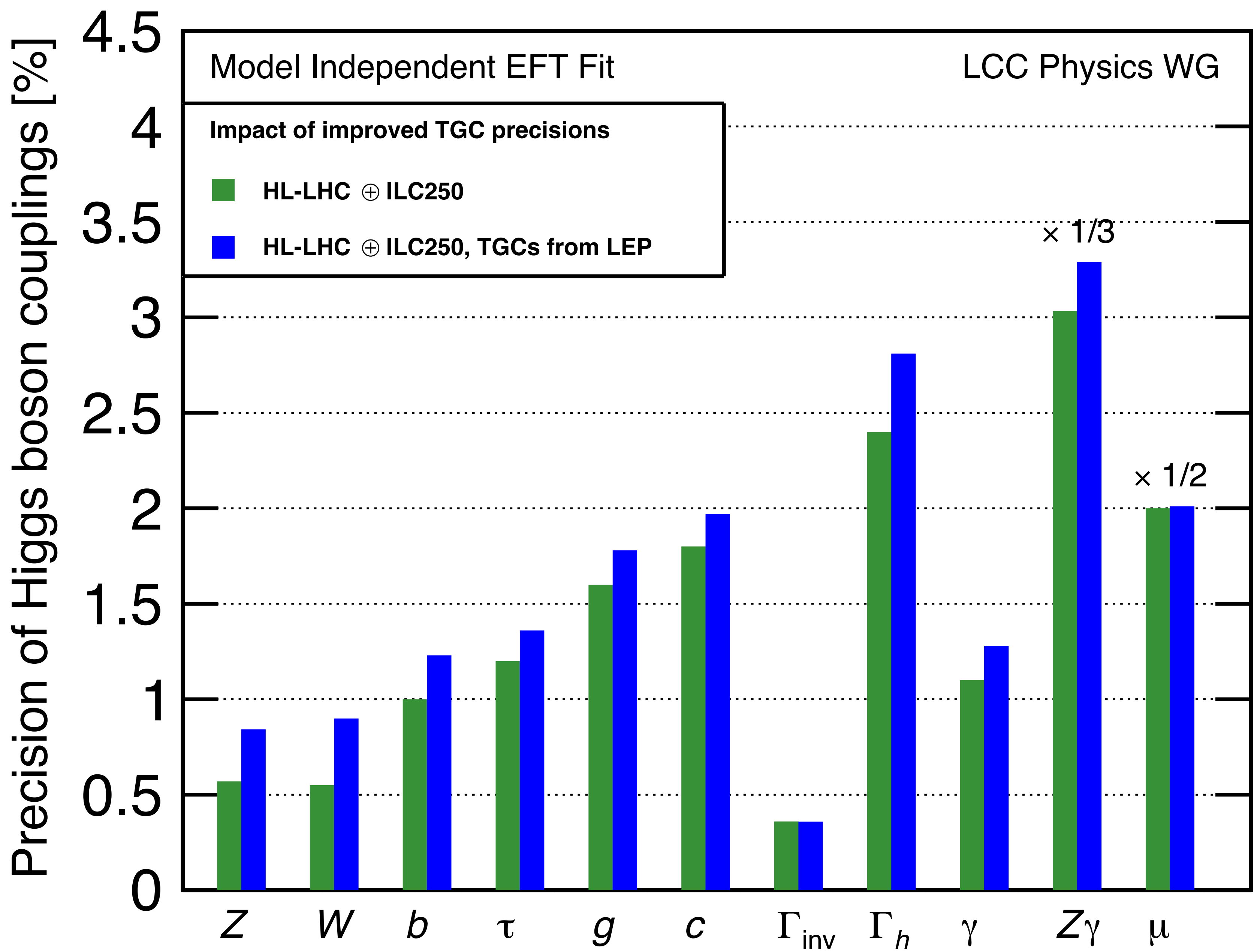
BSM benchmark models discrimination at ILC250

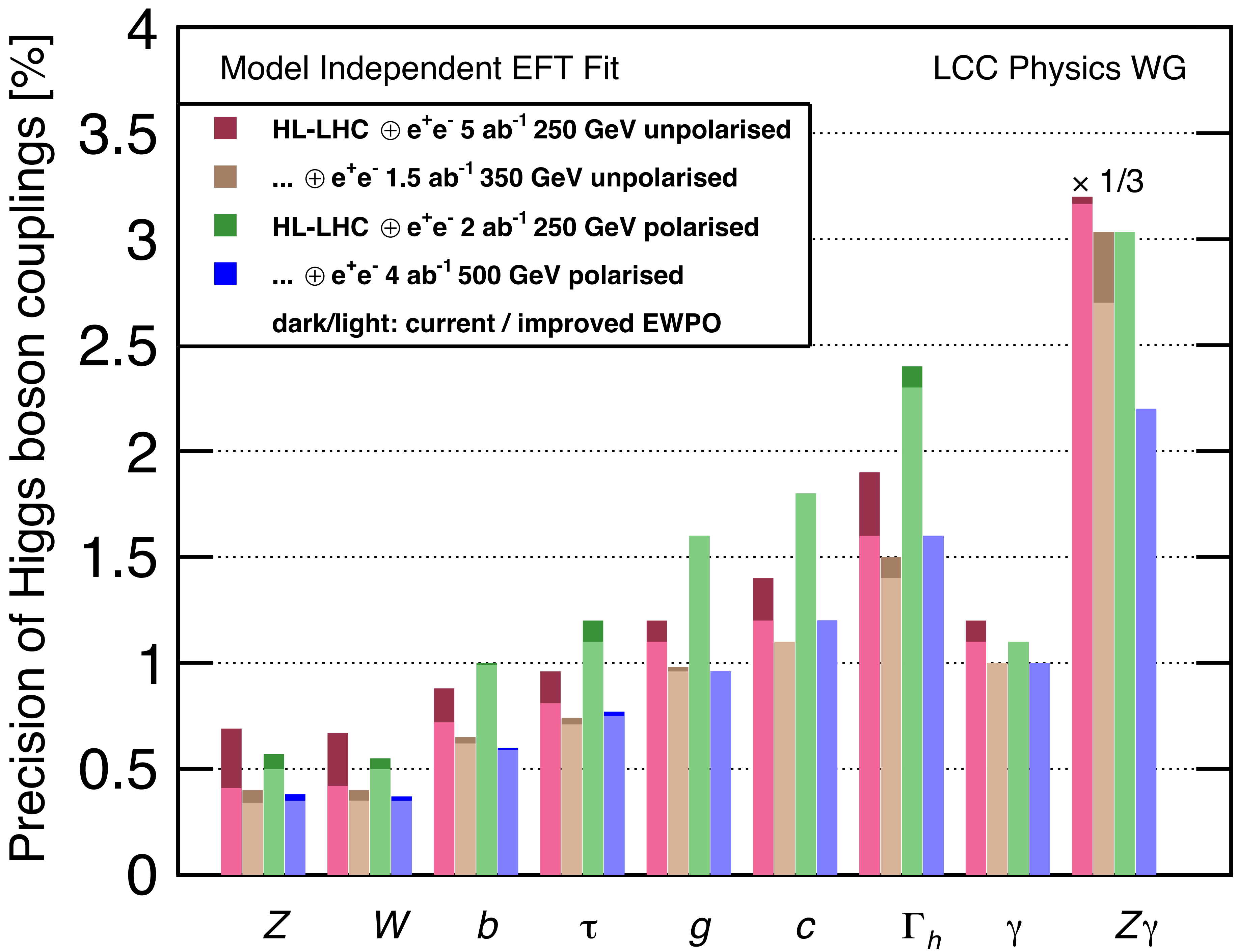


effect of improvement from TGC, ννH, ZH at 500GeV



impact of TGCs





Model Independent EFT Fit
LCC Physics WG
HL-LHC ⊕ e+e- 5 ab-1 250 GeV unpolarised
... ⊕ e+e- 1.5 ab-1 350 GeV unpolarised
HL-LHC ⊕ e+e- 2 ab-1 250 GeV polarised
... ⊕ e+e- 4 ab-1 500 GeV polarised
dark/light: current / improved EWPO
× 1/3
Precision of Higgs boson couplings [%]
0
0.5
1
1.5
2
2.5
3
3.5
4
Z
W
b
τ
g
c
Γh
γ
Zγ

simplifications of our analysis

- at tree level, and to linear order in D-6 coefficients
- ignore some possible D-6 corrections involving light leptons, e.g. 4-fermion operators
- avoid using observables that involve contact interactions that include quark currents (see more later)
- ignore the effects of CP-violating operators

$$\Delta\mathcal{L}_{CP} = +\frac{g^2\tilde{c}_{WW}}{m_W^2}\Phi^\dagger\Phi W^a_{\mu\nu}\widetilde{W}^{a\mu\nu} + \frac{4gg'\tilde{c}_{WB}}{m_W^2}\Phi^\dagger t^a\Phi W^a_{\mu\nu}\widetilde{B}^{\mu\nu}$$
$$+\frac{g'^2\tilde{c}_{BB}}{m_W^2}\Phi^\dagger\Phi B_{\mu\nu}\widetilde{B}^{\mu\nu} + \frac{g^3\tilde{c}_{3W}}{m_W^2}\epsilon_{abc}W^a_{\mu\nu}W^{b\nu}{}_\rho\widetilde{W}^{c\rho\mu}$$

on-shell renormalization

- D-6 operators modify the SM expressions for precision electroweak observables, thus shift the appropriate values for the SM couplings —> g, g', v, λ free parameters
- D-6 operators also renormalize the kinetic terms of the SM fields —> rescale the boson fields

$$\mathcal{L} = -\frac{1}{2} W^+_{\mu\nu} W^{-\mu\nu} \cdot (1 - \delta Z_W) - \frac{1}{4} Z_{\mu\nu} Z^{\mu\nu} \cdot (1 - \delta Z_Z)$$
$$- \frac{1}{4} A_{\mu\nu} A^{\mu\nu} \cdot (1 - \delta Z_A) + \frac{1}{2} (\partial_\mu h)(\partial^\mu h) \cdot (1 - \delta Z_h) \ ,$$

with

$$\begin{aligned} \delta Z_W &= (8c_{WW}) \\ \delta Z_Z &= c_w^2 (8c_{WW}) + 2 s_w^2 (8c_{WB}) + s_w^4 / c_w^2 (8c_{BB}) \\ \delta Z_A &= s_w^2 \Big((8c_{WW}) - 2(8c_{WB}) + (8c_{BB}) \Big) \\ \delta Z_h &= -c_H \quad . \end{aligned}$$

$$\Delta\mathcal{L} = \frac{1}{2} \delta Z_{AZ} \, A_{\mu\nu} Z^{\mu\nu} \ , \qquad \delta Z_{AZ} = s_w c_w \Big((8c_{WW}) - (1 - \frac{s_w^2}{c_w^2})(8c_{WB}) - \frac{s_w^2}{c_w^2}(8c_{BB}) \Big)$$

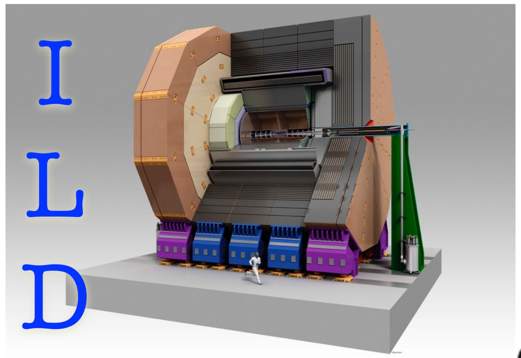
systematic errors included in the global fit

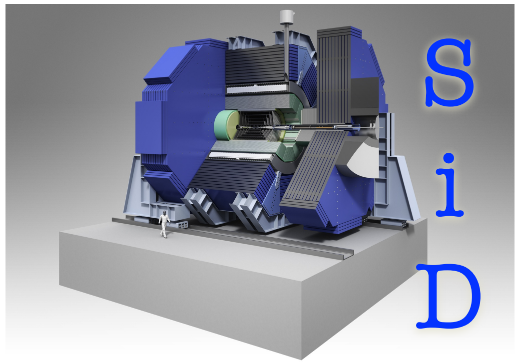
- 0.1% from theory computations
- 0.1% from luminosity
- 0.1% from beam polarizations
- 0.1%$\oplus$0.3%/sqrt(L/250) from b-tagging and analysis

improvement factors in S2

- 10% from better jet-clustering algorithm
- 20% from better flavor-tagging algorithm
- 20% from including more signal channels in h->WW*
- x10 better for A_{LR} using e+e- -> γ Z at ILC250

expected meas. for direct observables





estimates at ILC by full simulation

-80% e^-, +30% e^+ polarization:

	250 GeV		350 GeV		500 GeV	
	Zh	$\nu\bar{\nu}h$	Zh	$\nu\bar{\nu}h$	Zh	$\nu\bar{\nu}h$
σ [50–53]	2.0		1.8		4.2	
$h \to invis.$ [54, 55]	0.86		1.4		3.4	
$h \to b\bar{b}$ [56–59]	1.3	8.1	1.5	1.8	2.5	0.93
$h \to c\bar{c}$ [56, 57]	8.3		11	19	18	8.8
$h \to gg$ [56, 57]	7.0		8.4	7.7	15	5.8
$h \to WW$ [59–61]	4.6		5.6 *	5.7 *	7.7	3.4
$h \to \tau\tau$ [63]	3.2		4.0 *	16 *	6.1	9.8
$h \to ZZ$ [2]	18		25 *	20 *	35 *	12 *
$h \to \gamma\gamma$ [64]	34 *		39 *	45 *	47	27
$h \to \mu\mu$ [65, 66]	72 *		87 *	160 *	120 *	100 *
a [27]	7.6		2.7 *		4.0	
b	2.7		0.69 *		0.70	
$\rho(a, b)$	-99.17		-95.6 *		-84.8	

(arXiv: 1708.08912; numbers are in %, for nominal ∫Ldt = 250 fb^{-1})

EFT input from TGCs in e+e- -> W^+W^-

	250 GeV W^+W^-	350 GeV W^+W^-	500 GeV W^+W^-
g_{1Z}	0 .062 *	0.033 *	0.025
κ_A	0.096 *	0.049 *	0.034
λ_A	0.077 *	0.047 *	0.037
$\rho(g_{1Z}, \kappa_A)$	63.4 *	63.4 *	63.4
$\rho(g_{1Z}, \lambda_A)$	47.7 *	47.7 *	47.7
$\rho(\kappa_A, \lambda_A)$	35.4 *	35.4 *	35.4

(arXiv: 1708.08912; numbers are in %, for nominal $\int L dt$ = 500 fb^{-1} shared equally by left-/right- polarized data)

EFT input: EWPOs

Observable	current value	current σ	future σ	SM best fit value
$\alpha^{-1}(m_Z^2)$	128.9220	0.0178		(same)
G_F (10^{-10} GeV^{-2})	1166378.7	0.6		(same)
m_W (MeV)	80385	15	5	80361
m_Z (MeV)	91187.6	2.1		91188.0
m_h (MeV)	125090	240	15	125110
A_ℓ	0.14696	0.0013		0.147937
Γ_ℓ (MeV)	83.984	0.086		83.995
Γ_Z (MeV)	2495.2	2.3		2494.3
Γ_W (MeV)	2085	42	2	2088.8

EFT input: EWPOs (7)

$$\underline{\alpha(m_Z), G_F, m_W, m_Z, m_h,} A_{LR}(\ell), \Gamma(Z \to \ell^+\ell^-)$$

$$\delta e = \delta(4\pi\alpha(m_Z^2))^{1/2} = s_w^2 \delta g + c_w^2 \delta g' + \frac{1}{2}\delta Z_A$$

$$\delta G_F = \ -2\delta v + 2c'_{HL}$$

$$\delta m_W = \delta g + \delta v + \frac{1}{2}\delta Z_W$$

$$\delta m_Z = c_w^2 \delta g + s_w^2 \delta g' + \delta v - \frac{1}{2}c_T + \frac{1}{2}\delta Z_Z$$

$$\delta m_h = \frac{1}{2}\delta\overline{\lambda} + \delta v + \frac{1}{2}\delta Z_h$$

($\delta X = \Delta X / X$)

$$\overline{\lambda} = \lambda(1 + \frac{3}{2}c_6)$$

$$s_w^2 = \sin^2\theta_w = \frac{g'^2}{g^2 + g'^2}$$

$$c_w^2 = \cos^2\theta_w = \frac{g^2}{g^2 + g'^2}$$

⟶ δg, $\delta g'$, δv, $\delta \lambda$, c_T

EFT input: EWPOs (7)

$$\alpha(m_Z), G_F, m_W, m_Z, m_h, \underline{A_{LR}(\ell), \Gamma(Z \to \ell^+ \ell^-)}$$

$$\delta\Gamma_\ell = \delta m_Z + 2\frac{g_L^2 \delta g_L + g_R^2 \delta g_R}{g_L^2 + g_R^2}$$

$$\delta A_\ell = \frac{4 g_L^2 g_R^2 (\delta g_L - \delta g_R)}{g_L^4 - g_R^4}$$

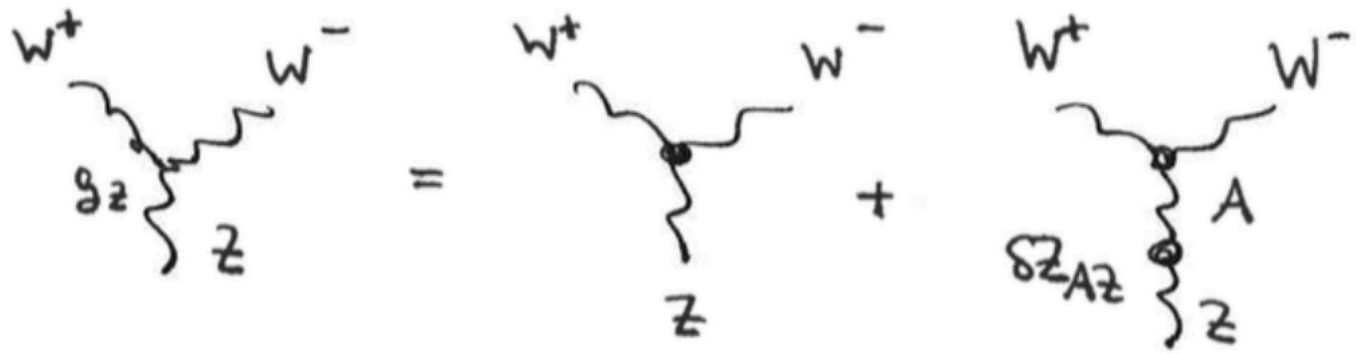
$$g_L = \frac{g}{c_w}\left[(-\frac{1}{2} + s_w^2)(1 + \frac{1}{2}\delta Z_Z) - \frac{1}{2}(c_{HL} + c'_{HL}) - s_w c_w \delta Z_{AZ}\right]$$

$$g_R = \frac{g}{c_w}\left[(+s_w^2)(1 + \frac{1}{2}\delta Z_Z) - \frac{1}{2} c_{HE} - s_w c_w \delta Z_{AZ}\right]$$

$\longrightarrow$ c_{HL}+c'_{HL}, c_{HE}

EFT input: TGC (3)

$$\Delta\mathcal{L}_{TGC} = ig_V\Big\{V^\mu(\hat{W}^-_{\mu\nu}W^{+\nu} - \hat{W}^+_{\mu\nu}W^{-\nu}) + \kappa_V W^+_\mu W^-_\nu \hat{V}^{\mu\nu} + \frac{\lambda_V}{m_W^2}\hat{W}^{-\rho}_\mu \hat{W}^+_{\rho\nu}\hat{V}^{\mu\nu}\Big\}$$

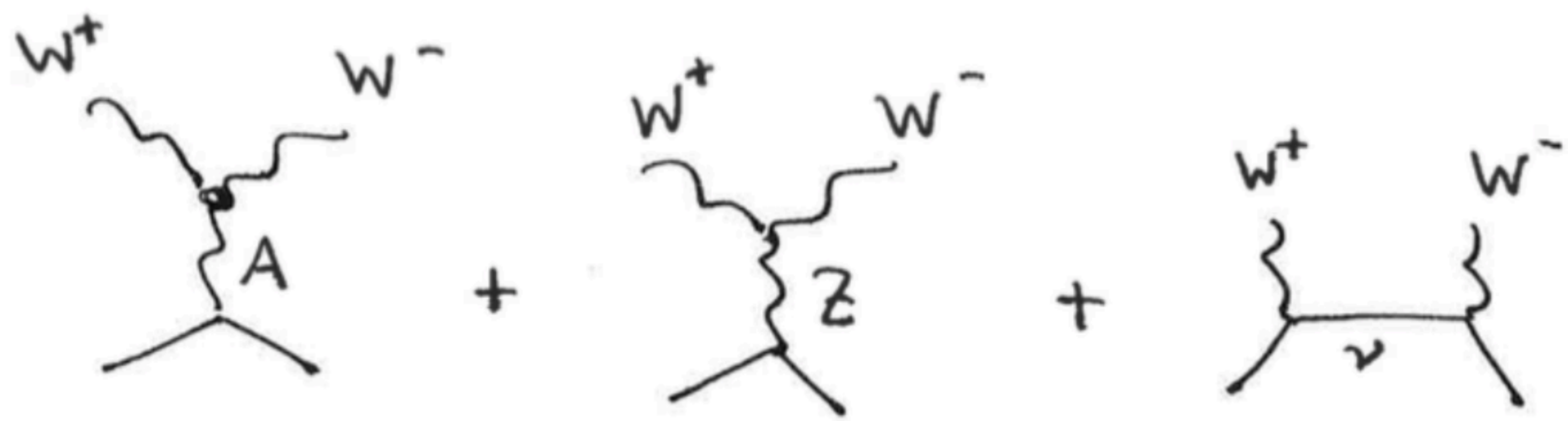


$$g_Z = gc_w(1 + \frac{1}{2}\delta Z_Z + \frac{s_w}{c_w}\delta Z_{AZ})$$

$$\kappa_A = 1 + (8c_{WB})$$

$$\lambda_A = -6g^2c_{3W}$$

EFT input: TGC (3)



$$\delta g_{Z,eff} = \delta g_Z + \frac{1}{c_w^2}((c_w^2 - s_w^2)\delta g_L + s_w^2 \delta g_R - 2\delta g_W)$$
$$\delta\kappa_{A,eff} = (c_w^2 - s_w^2)(\delta g_L - \delta g_R) + 2(\delta e - \delta g_W) + (8c_{WB})$$
$$\delta\lambda_{A,eff} = -6g^2 c_{3W}$$

$$g_W = g\ (1 + c'_{HL} + \frac{1}{2}\delta Z_W)$$

EFT input: BR(h->γγ)/BR(h->ZZ*), BR(h->γZ)/BR(h->ZZ*)

(2: HL-LHC)

$$\delta\Gamma(h \to \gamma\gamma) = 528\,\delta Z_A - c_H + 4\delta e + 4.2\,\delta m_h - 1.3\,\delta m_W - 2\delta v$$

$$\delta\Gamma(h \to Z\gamma) = 290\,\delta Z_{AZ} - c_H - 2(1 - 3s_W^2)\delta g + 6c_w^2\delta g' + \delta Z_A + \delta Z_Z$$
$$+9.6\,\delta m_h - 6.5\,\delta m_Z - 2\delta v$$

$$\delta\Gamma(h \to ZZ^*) = 2\eta_Z - 2\delta v - 13.8\delta m_Z + 15.6\delta m_h - 0.50\delta Z_Z - 1.02 C_Z + 1.18\delta\Gamma_Z$$

$$\delta Z_A = s_w^2\Big((8c_{WW}) - 2(8c_{WB}) + (8c_{BB})\Big) \qquad \delta Z_{AZ} = s_w c_w\Big((8c_{WW}) - (1 - \frac{s_w^2}{c_w^2})(8c_{WB}) - \frac{s_w^2}{c_w^2}(8c_{BB})\Big)$$

EFT coefficients

10: c_H, c_T, c_6, c_{WW}, c_{WB}, c_{BB}, c_{3W}, c_{HL}, c'_{HL}, c_{HE}

+ 4: g, g', v, λ

can already be determined,
except c_6, c_H

—> Higgs observables @ e+e-

EFT input: σ(e+e- —>Zh), σ(e+e- —> Zhh)

- c_H has to be determined by inclusive σ_{Zh} measurement
- c_6 has to be determined by double Higgs measurement

EFT input: BR(h—>XX)

$$\Delta\mathcal{L} = -c_{\tau\Phi}\frac{y_\tau}{v^2}(\Phi^\dagger\Phi)\overline{L}_3\cdot\Phi\tau_R + h.c.$$

- h couplings to b, c, τ, μ, g

$$\delta\mathcal{L} = \mathcal{A}\frac{h}{v}G_{\mu\nu}G^{\mu\nu}$$

- Γ(h->invisible), total decay width

note: beam polarizations provide several independent (redundant) set of σ,σxBR input, which are powerful to test EFT validity two more parameters: C_W, C_Z for $\Gamma(h\to WW^*)$ and $\Gamma(h\to ZZ^*)$

$$\Gamma/(SM) = 1 + 2\eta_W - 2\delta v - 11.7\delta m_W + 13.6\delta m_h$$
$$-0.75\zeta_W - 0.88C_W + 1.06\delta\Gamma_W \ ,$$

$$C_W = \sum_X c'_X \mathcal{N}_X \ / \ \sum_X \mathcal{N}_X \ ,$$

(c'$_X$: contact interactions)

EFT input: $$\Gamma_W = \frac{g^2 m_W}{48\pi}(\sum_X \mathcal{N}_X)\cdot(1 + 2\delta g + \delta m_W + \delta Z_W + 2C_W)$$

(similar for Z)