

# Measurement of Higgs couplings at the ILC



From Design to Reality

Technical Design Report

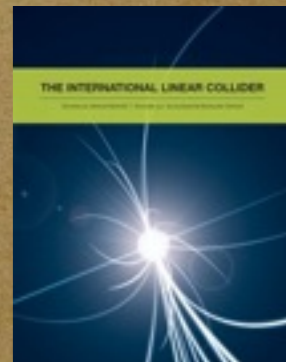
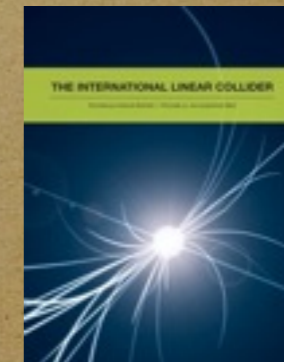
1 - Executive Summary

2 - Physics

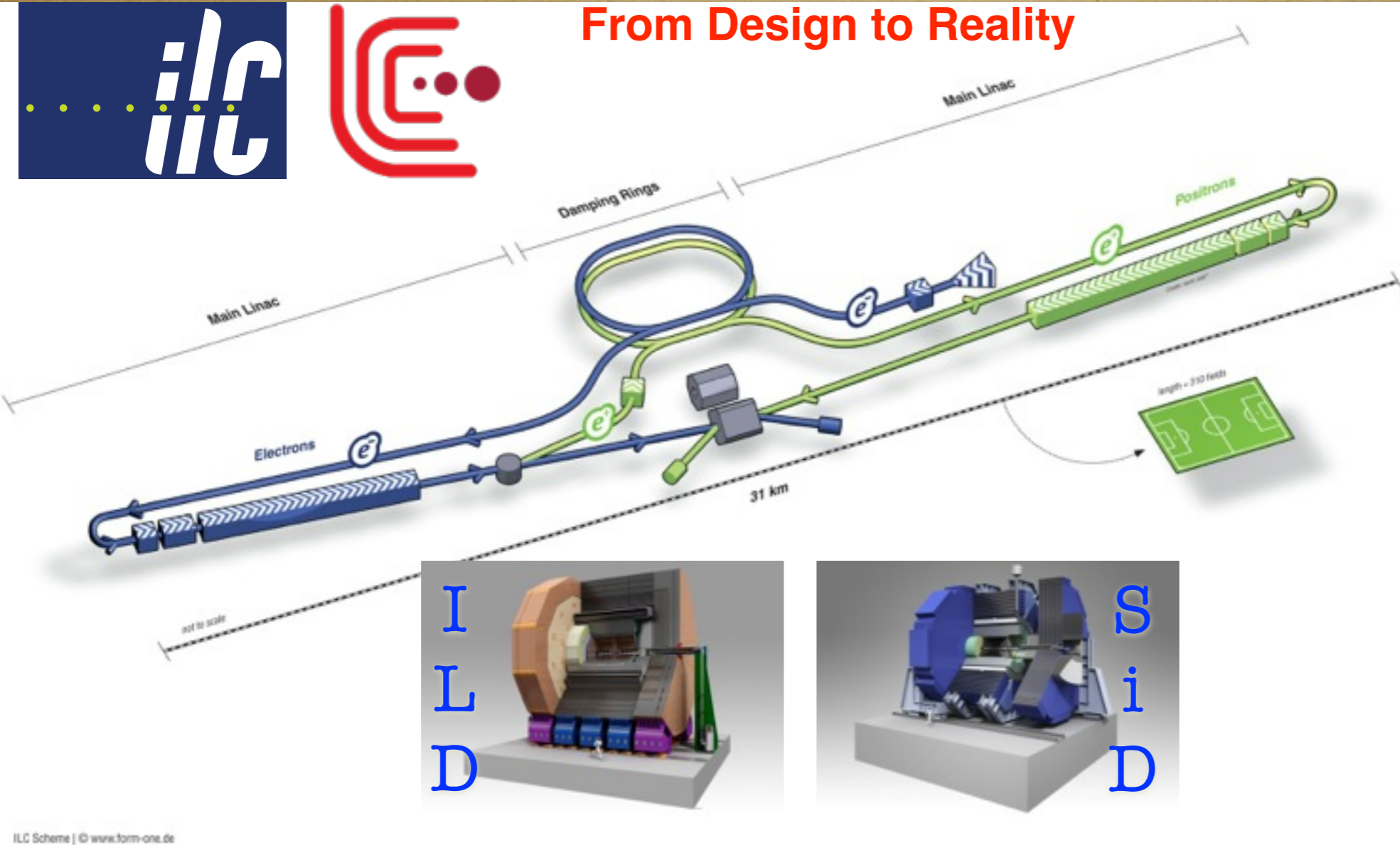


3 - Accelerator I

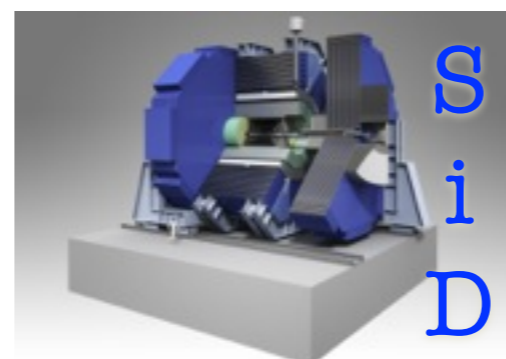
3 - Accelerator II



4 - Detector



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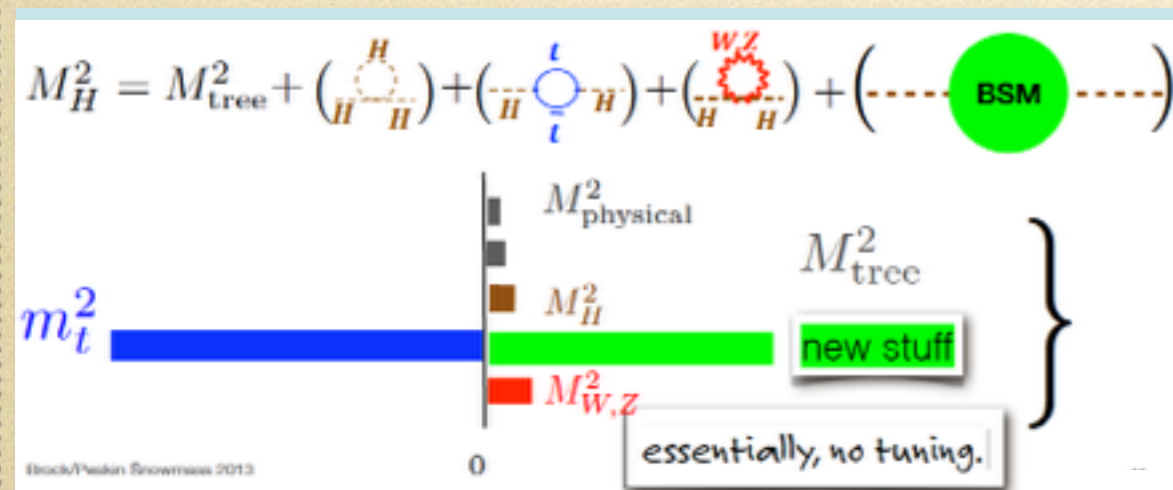
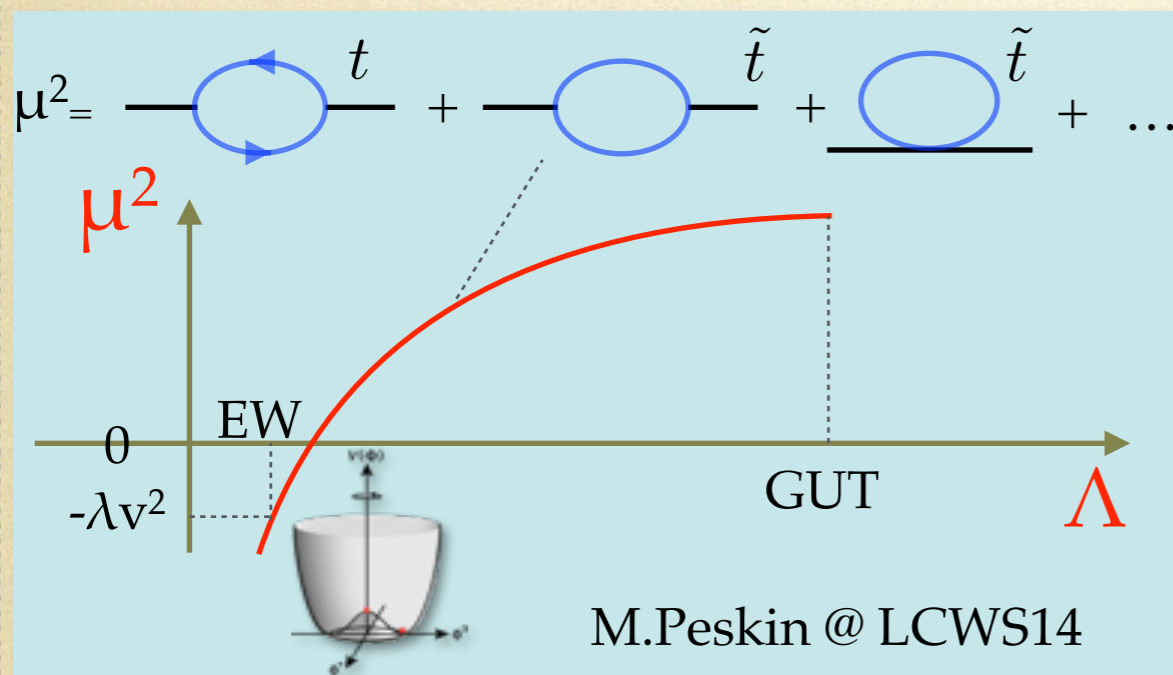
Junping Tian (KEK)

---on behalf of the ILC Physics & Detector Study

ICHEP 2014, Jul. 2-9 @ Valencia

For ILC Higgs Physics — TDR vol. 2 & vol. 4; ILC Higgs White Paper

# Post discovery of a Higgs boson — What we want to know



C.Brock @ Snowmass 2013

1.  $H(125) = H_{\text{SM}}$ ?
2. Why is  $\mu^2$  negative?
3. Is the cancelation in  $M_H$  radiative corrections natural?
4. What is the dynamics responsible for EWSB?

learn as much as possible about H(125)!

ILC is built to reveal the nature of H(125)

# Why Precisions?

- **Multiplet structure :**
  - Additional singlet? ( $\phi + S$ )
  - Additional doublet? ( $\phi + \phi'$ )
  - Additional triplet? ( $\phi + \Delta$ )
- **Underlying dynamics :**
  - Why did the Higgs condense?
  - Weakly interacting or strongly interacting?  
= elementary or composite ?
- **Relations to other questions of HEP :**
  - $\phi + S \rightarrow$  (B-L) gauge, DM, ...
  - $\phi + \phi' \rightarrow$  Type I :  $m_\nu$  from small vev, ...
    - $\rightarrow$  Type II : SUSY, DM, ...
    - $\rightarrow$  Type X:  $m_\nu$  (rad.seesaw), ...
  - $\phi + \Delta \rightarrow m_\nu$  (Type II seesaw), ...
  - $\lambda > \lambda_{SM} \rightarrow$  EW baryogenesis ?
  - $\lambda \downarrow 0 \rightarrow$  inflation ?

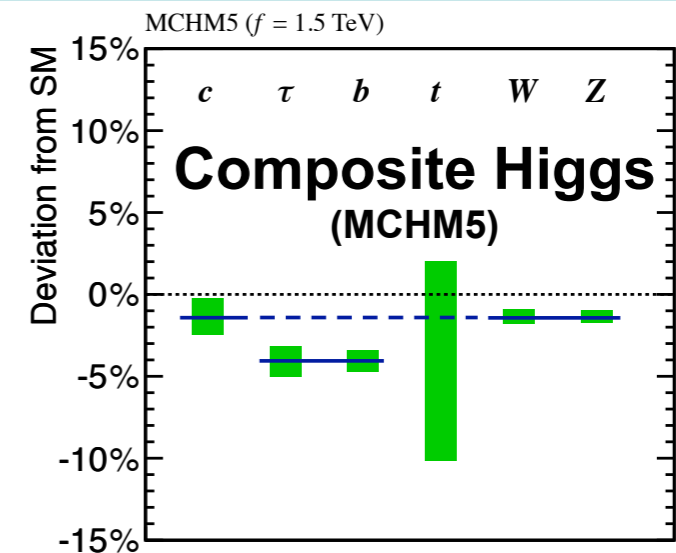
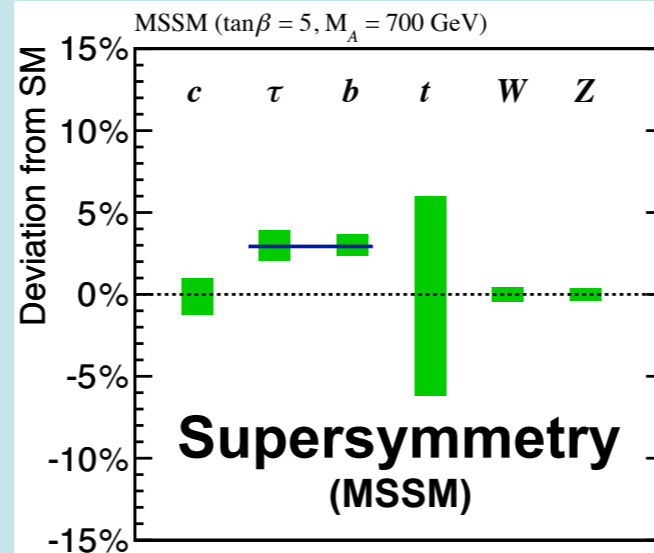
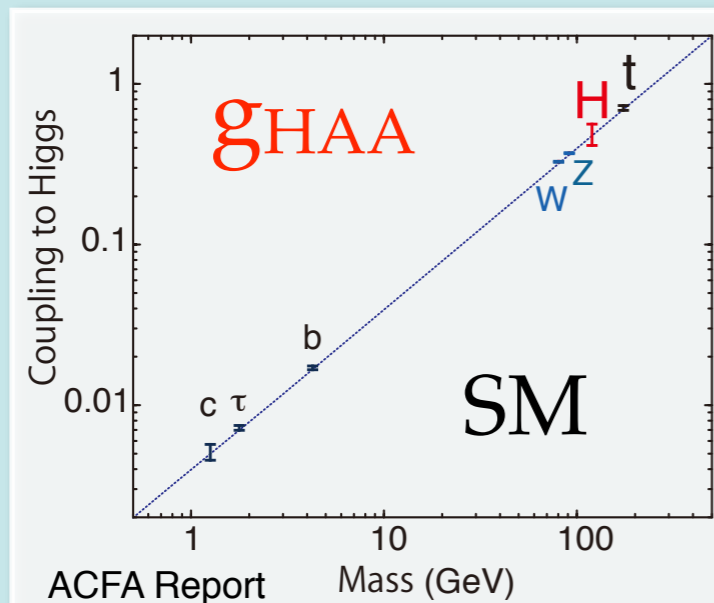
K. Fuji @ Pheno2014

- \* SM is a minimal solution, there are many other possibilities! TeV scale new physics is strongly motivated.
- \* deviations on various Higgs couplings are window to see new physics.
- \* Haber's decoupling limit, deviation  $\sim m_h^2/M^2$ .

$$\Delta g/g \sim O(1\%) @ 1 \text{ TeV}$$



ILC comprehensive Higgs program, key is to measure mass coupling relation model independently



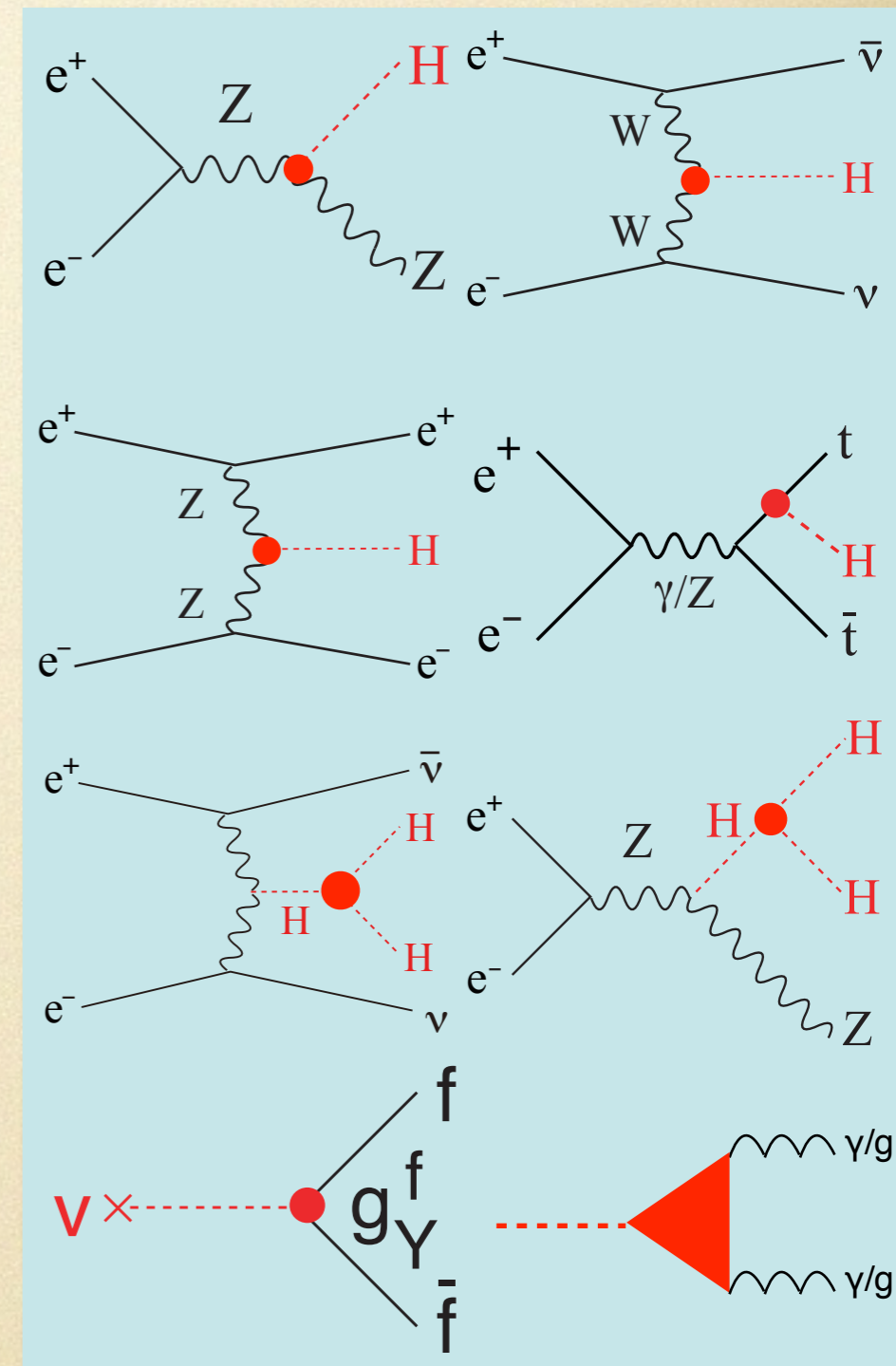
TDR Vol.2; T.Tomohiko

# A staged running program (Why 250—500 GeV?)

three well-known thresholds, a choice of physics

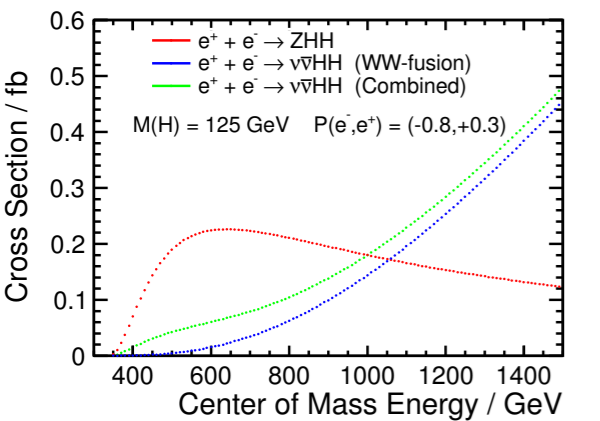
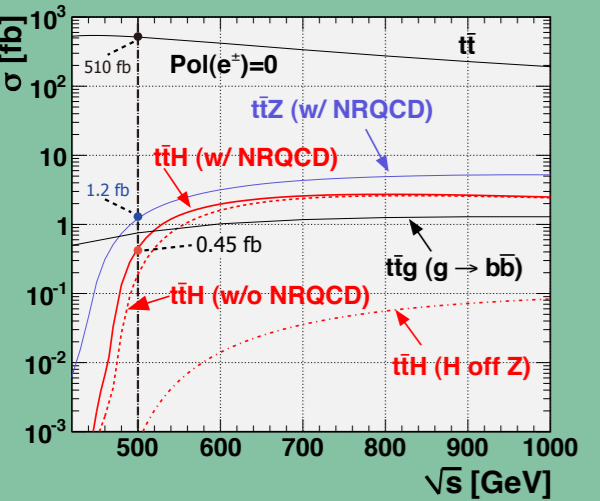
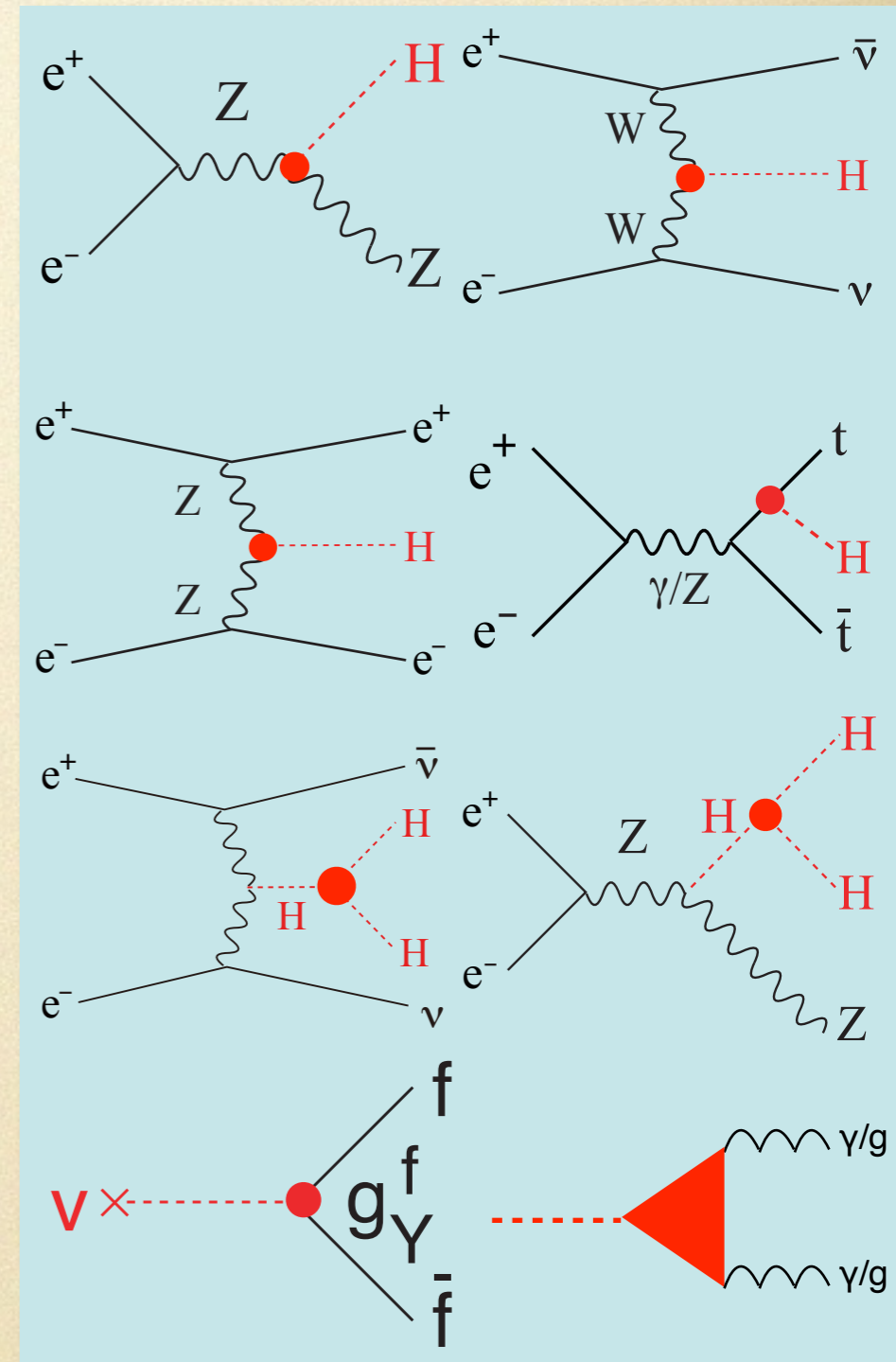
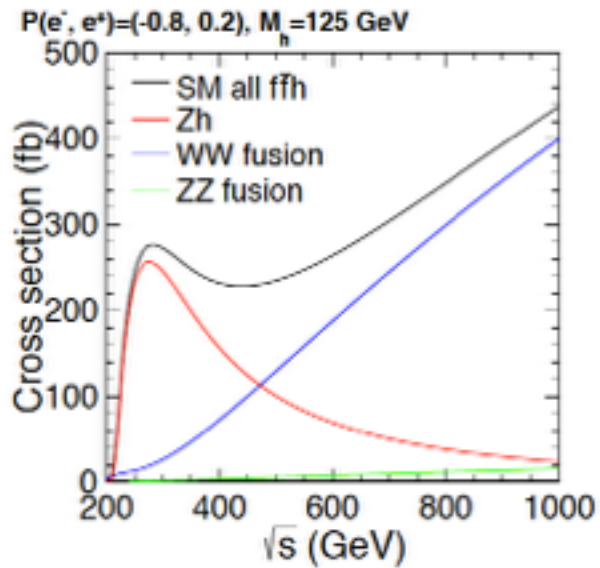
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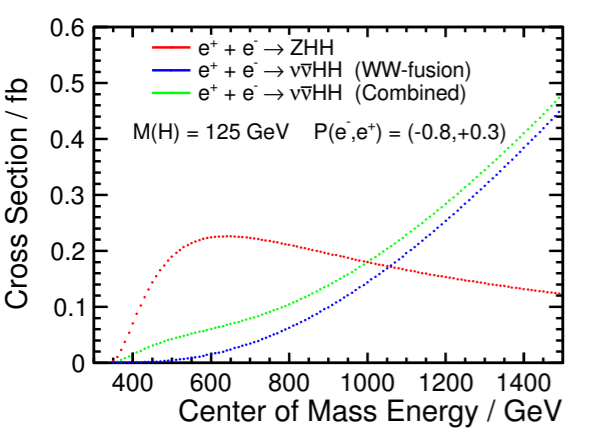
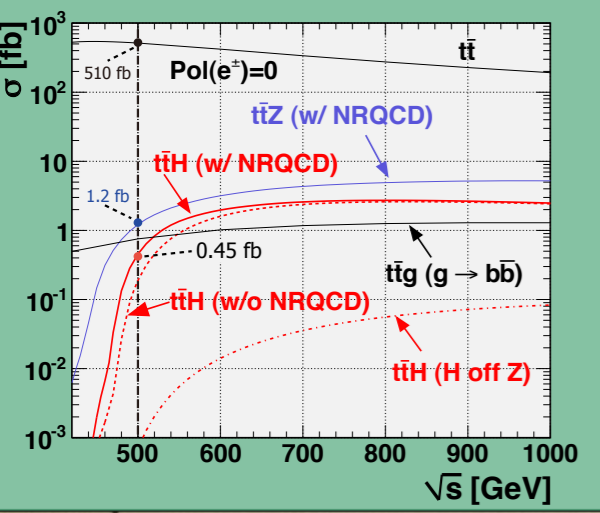
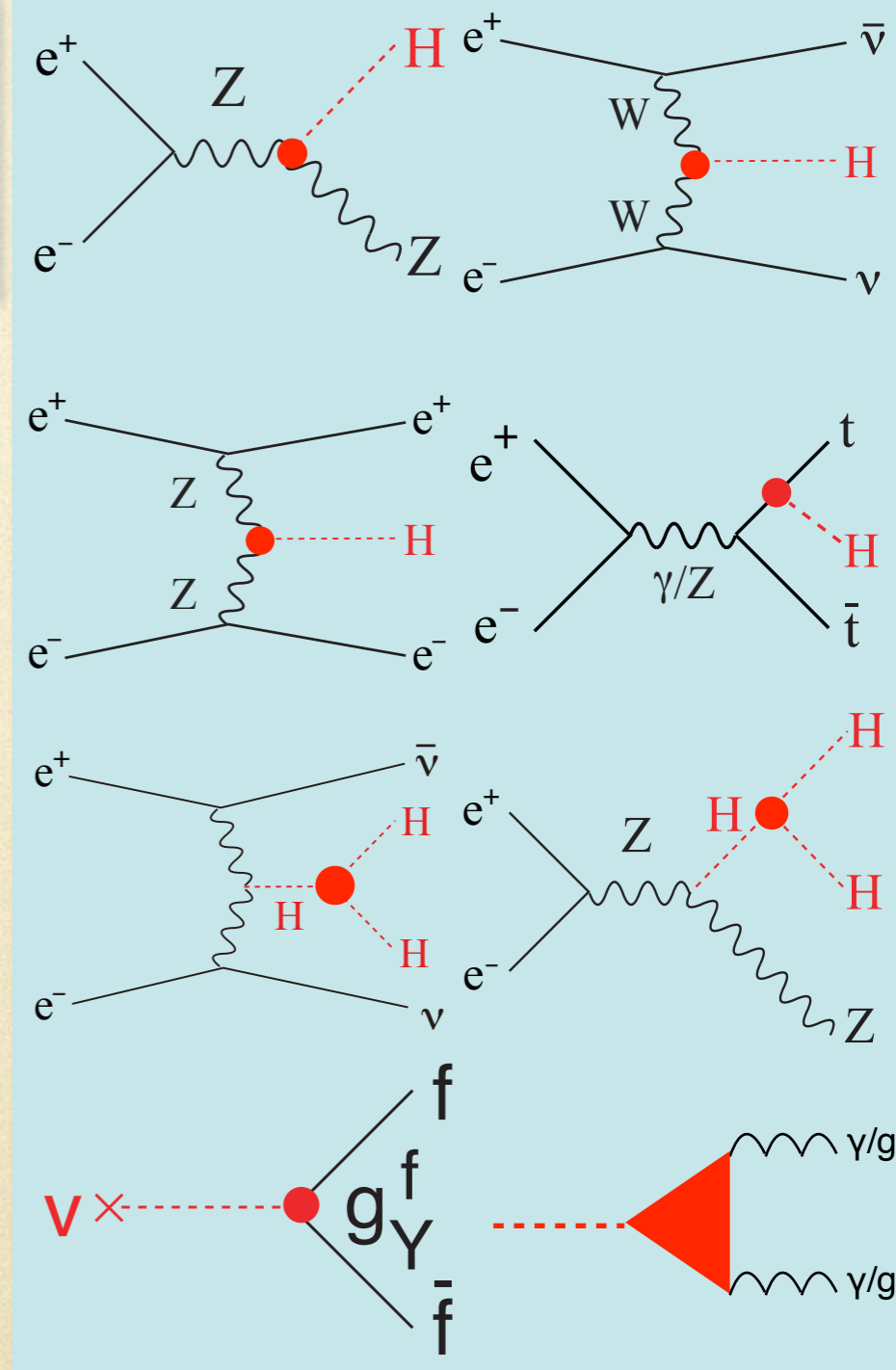
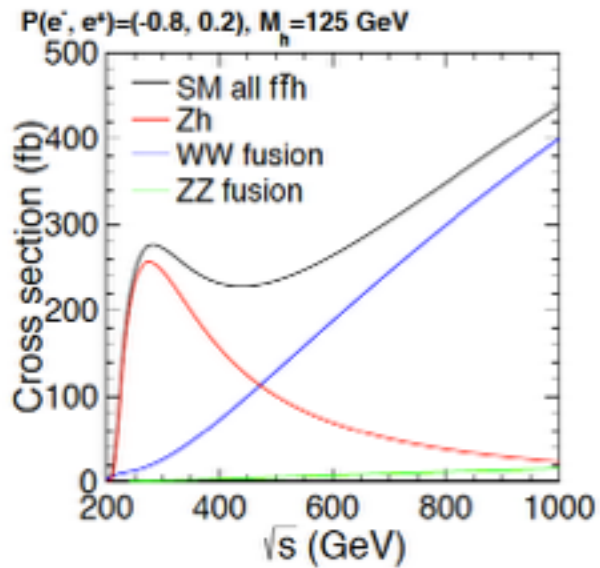


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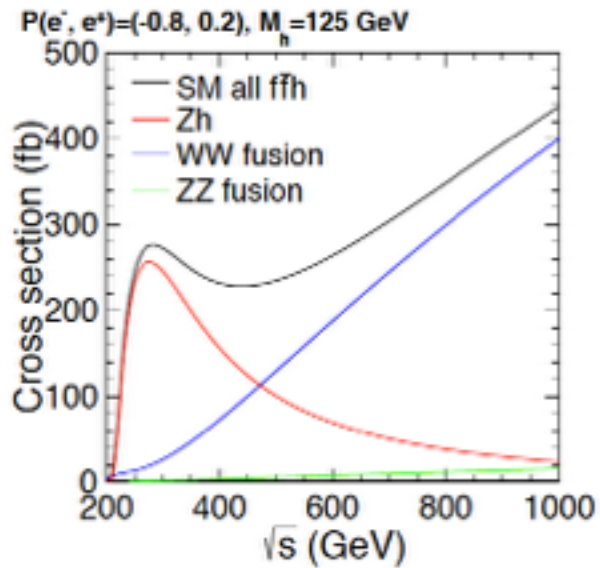
## ZH @ 250 GeV

- ▶ Higgs mass, spin, CP
- ▶ Absolute HZZ coupling
- ▶  $\text{Br}(H \rightarrow bb, cc, gg, \tau\tau, WW^*, ZZ^*, \gamma\gamma, \gamma Z)$



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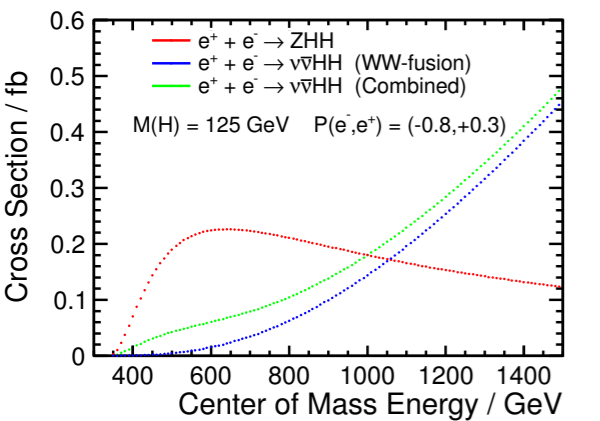
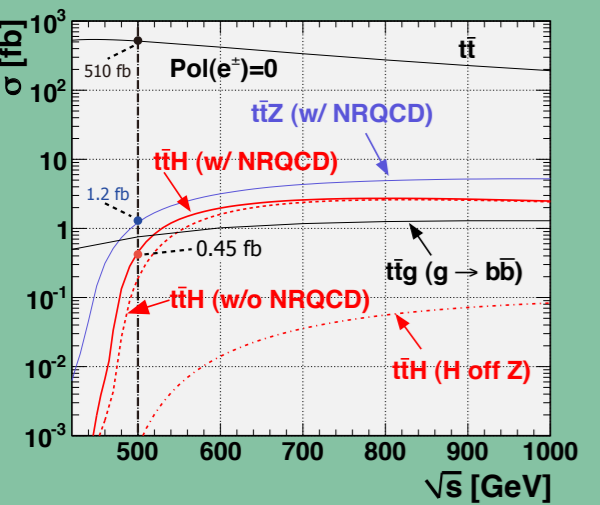
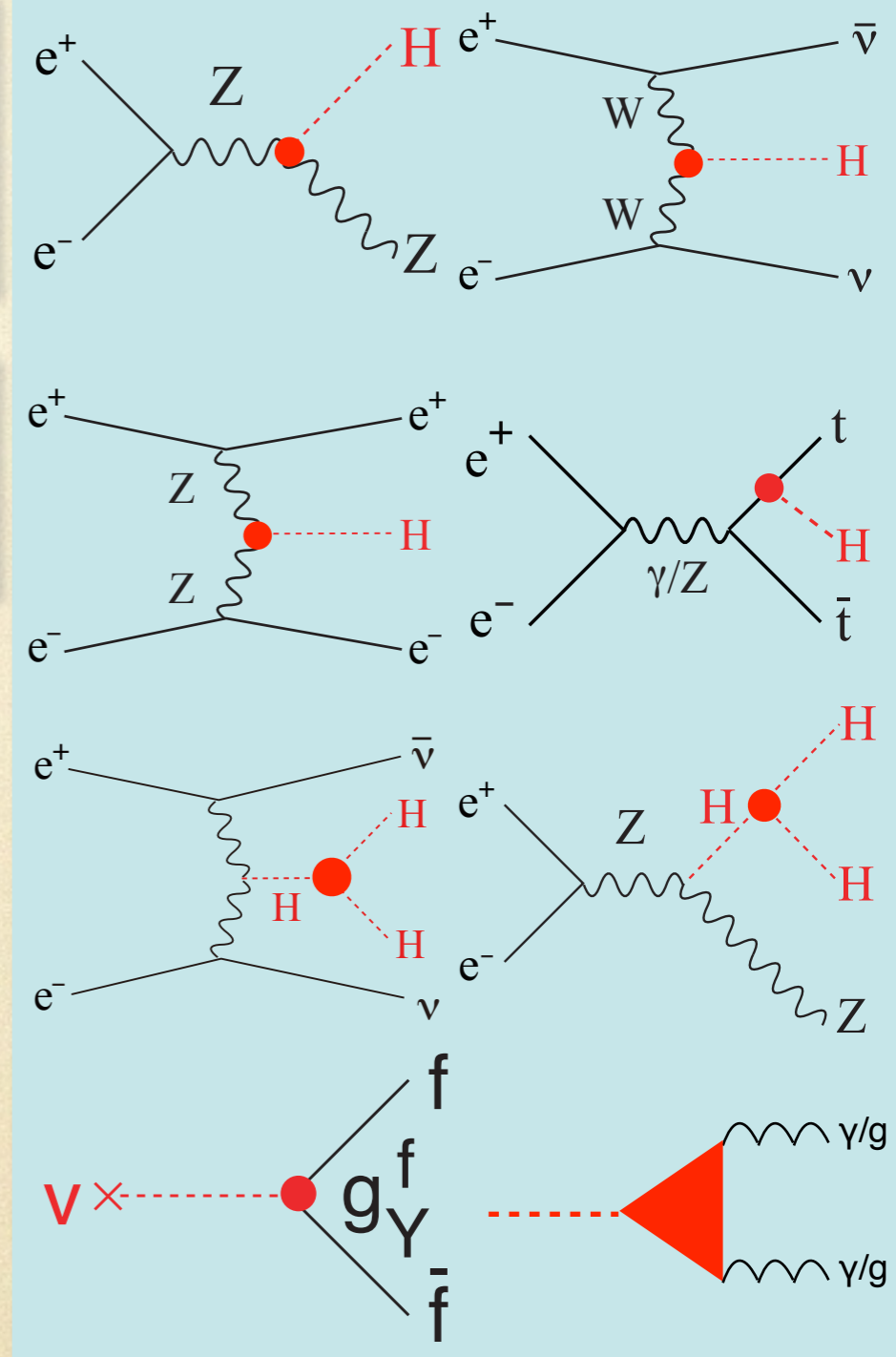


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## tt, $\nu\nu H$ @ 350 GeV (talk by I.Garcia)

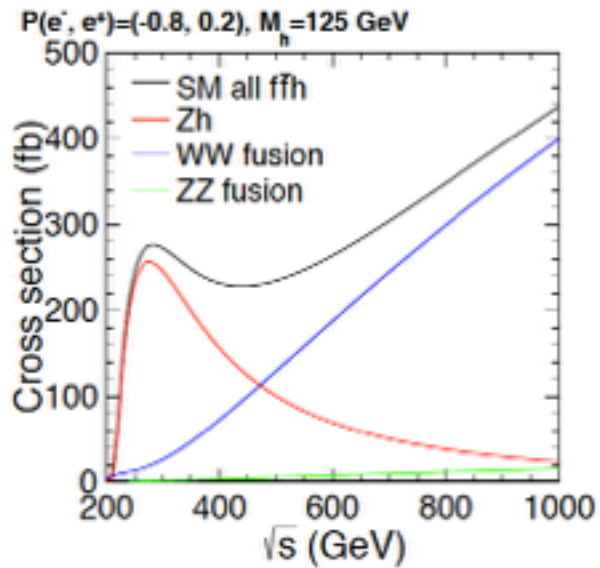
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- ▶ HWW, Total width





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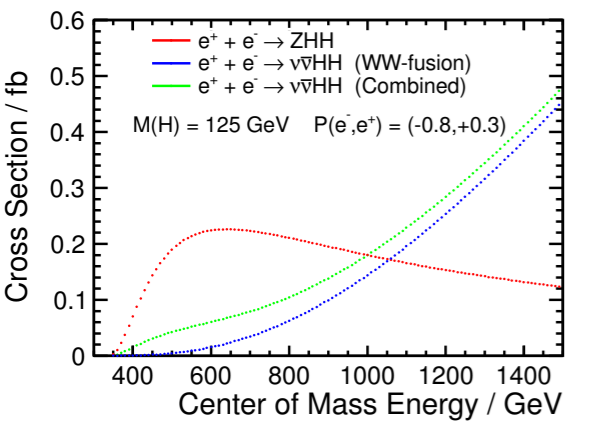
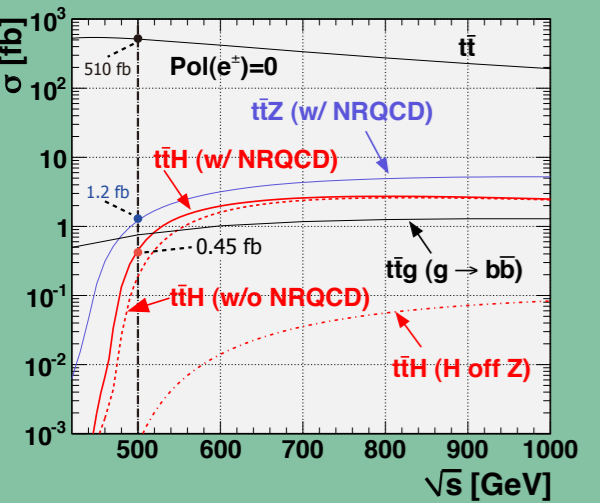
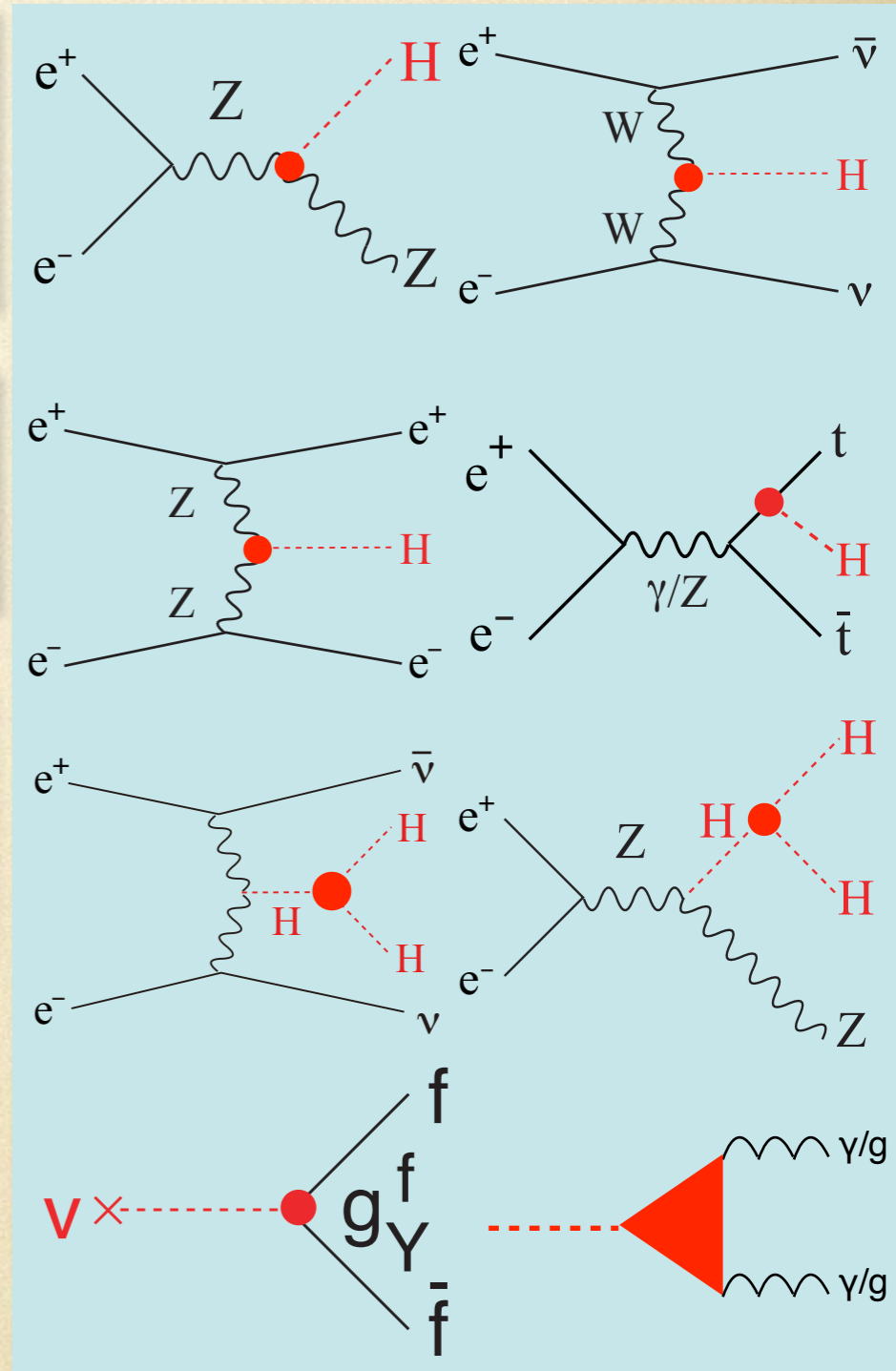
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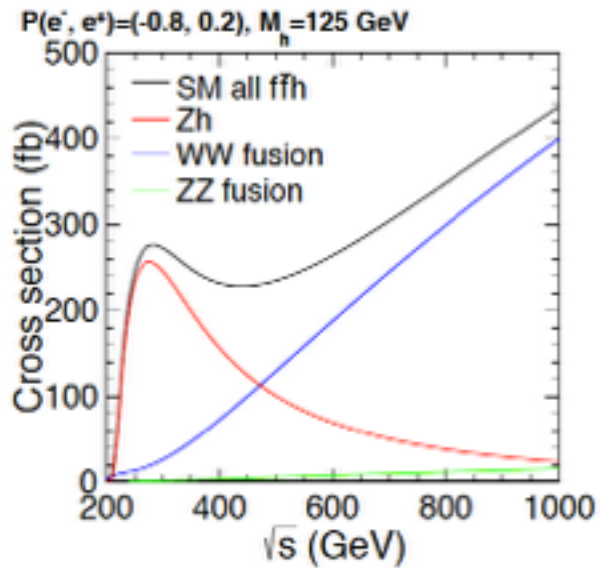
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- ▶ Direct top-Yukawa coupling through ttH
- ▶ Higgs self-coupling through ZHH
- ▶ Total width  $\rightarrow$  all Higgs couplings



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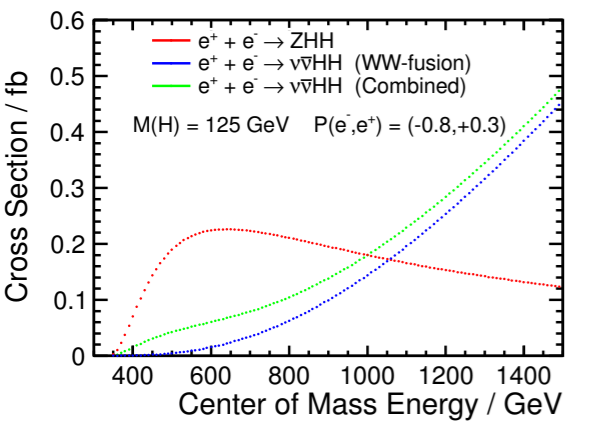
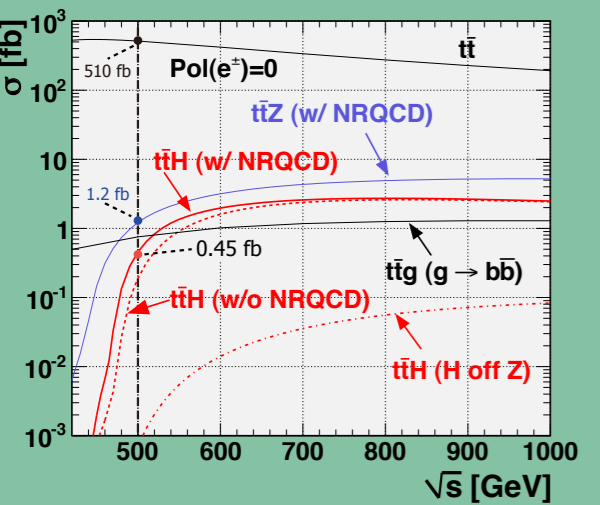
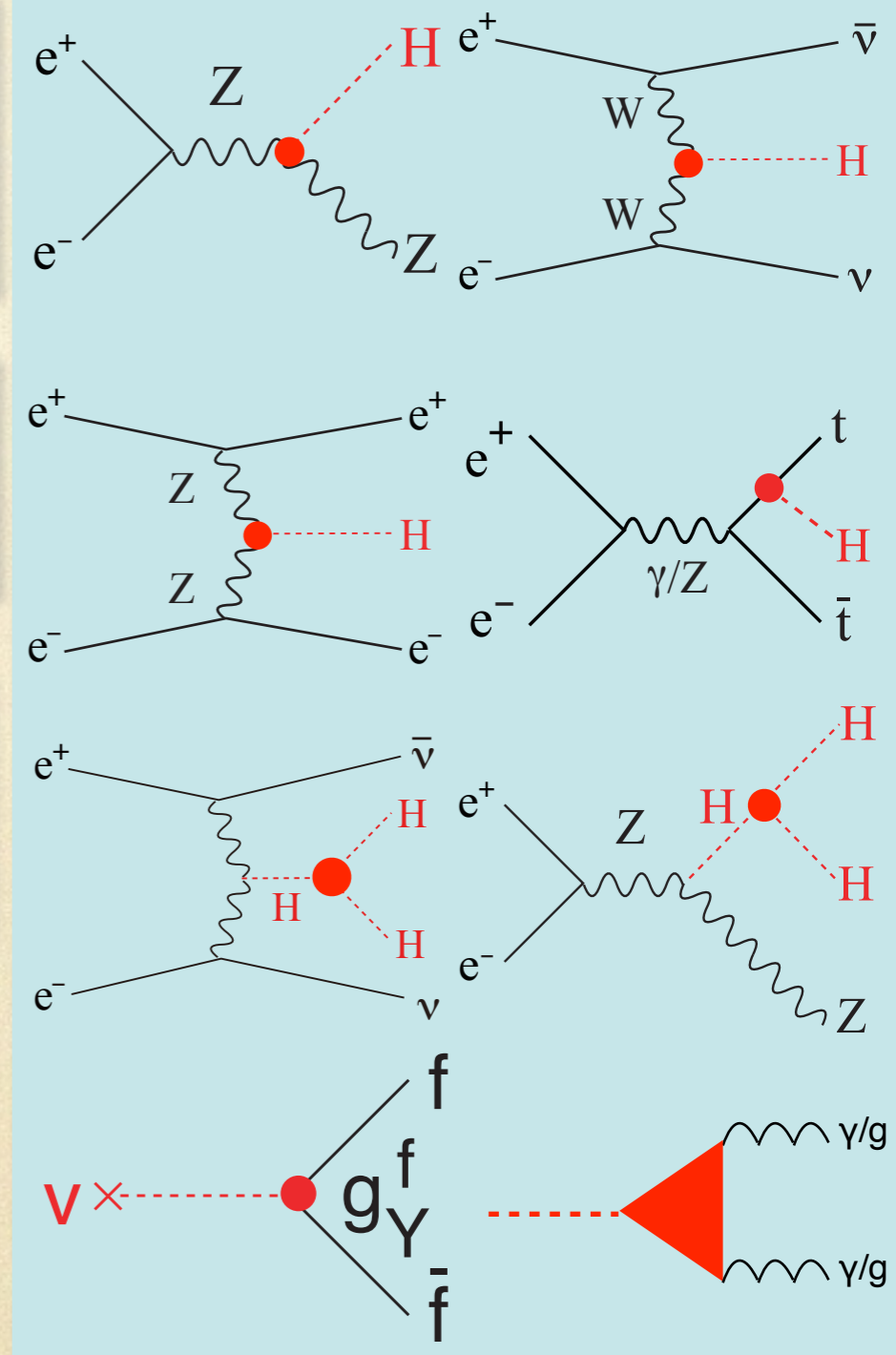
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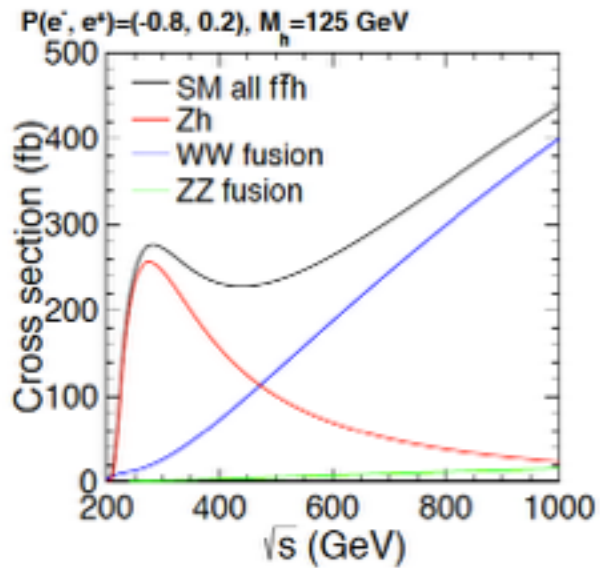
## $\nu\nu HH$ , ttH @ 1 TeV

- ▶ accumulate much more Higgs events
- ▶  $H \rightarrow \mu\mu$  accessible
- ▶ improve Top-Yukawa coupling
- ▶ Higgs self-coupling through  $\nu\nu HH$



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**ZH @ 250 GeV**  $\int L \cdot dt = 250 / 1150 \text{ fb}^{-1}$

- ▶ Higgs mass, spin, CP
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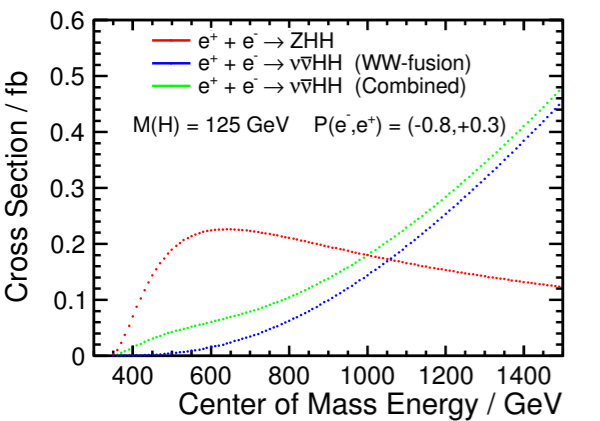
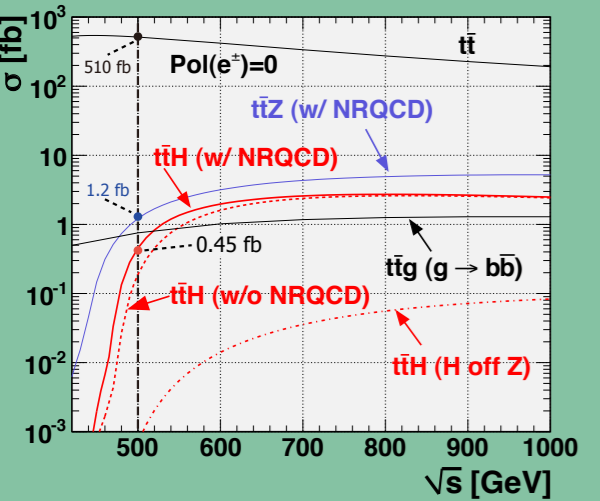
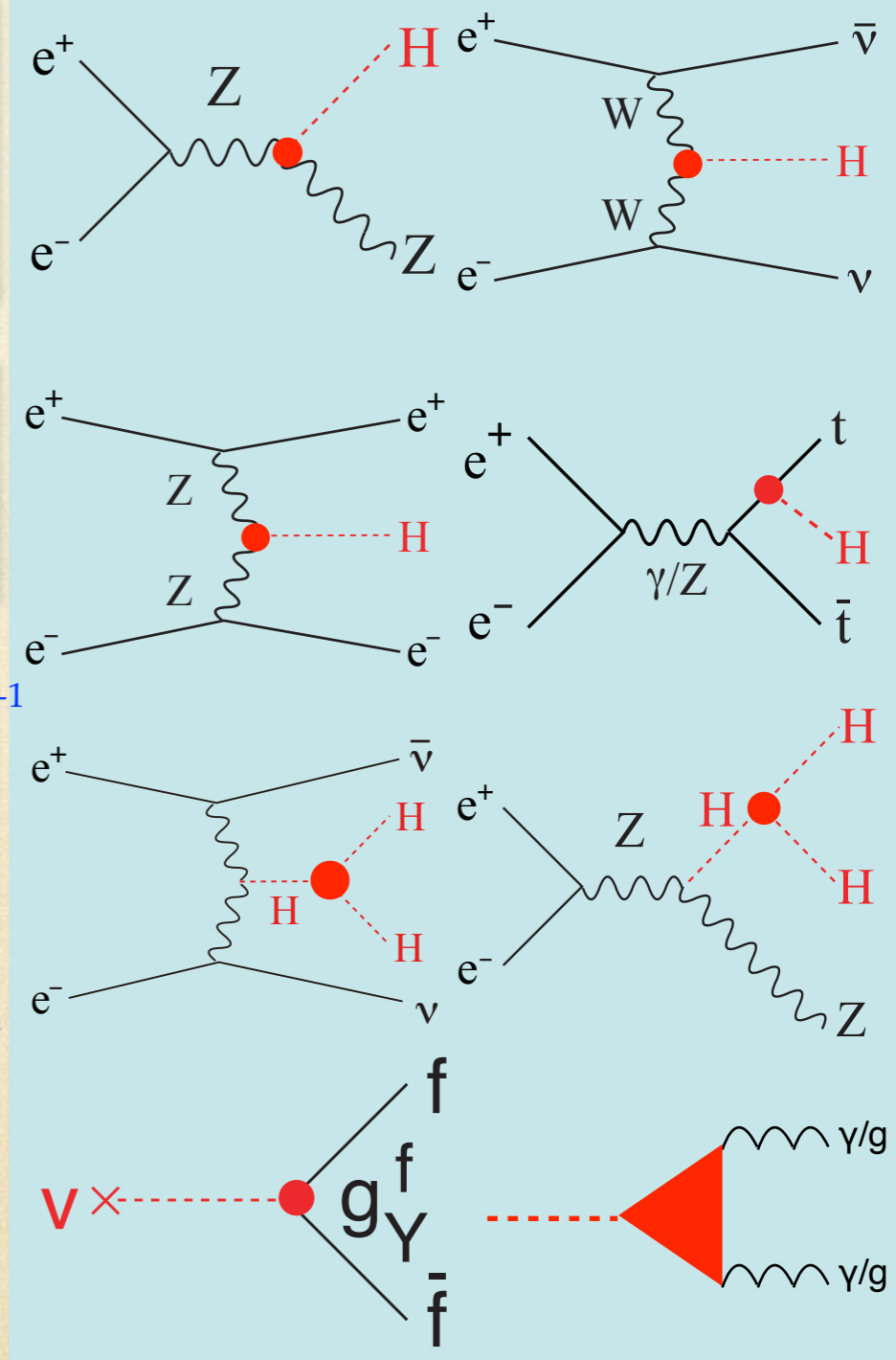
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- ▶ HWW, Total width

**ZHH, ttH @ 500 GeV**  $\int L \cdot dt = 500 / 1600 \text{ fb}^{-1}$

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- ▶ Total width  $\rightarrow$  all Higgs couplings

**$\nu\nu HH$ , ttH @ 1 TeV**  $\int L \cdot dt = 1000 / 2500 \text{ fb}^{-1}$

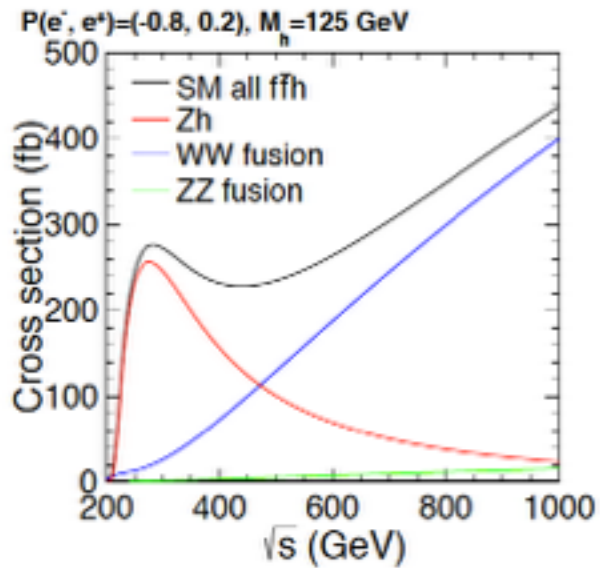
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$\int L \cdot dt = \text{Baseline (TDR is just beginning)} / \text{Luminosity Upgrade (increasing \#bunch, collision rate)}$

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**ZH @ 250 GeV**  $\int L \cdot dt = 250 / 1150 \text{ fb}^{-1}$

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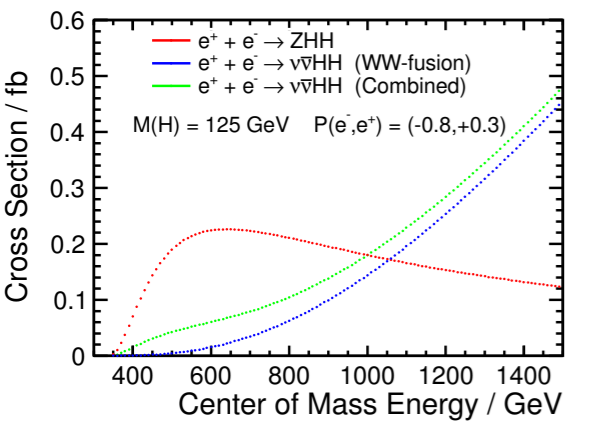
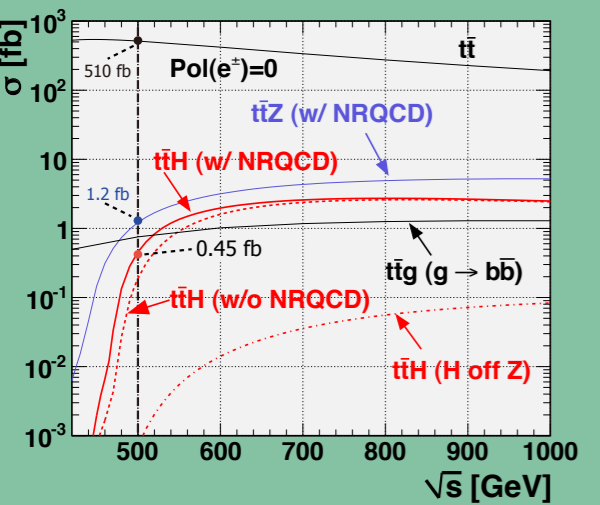
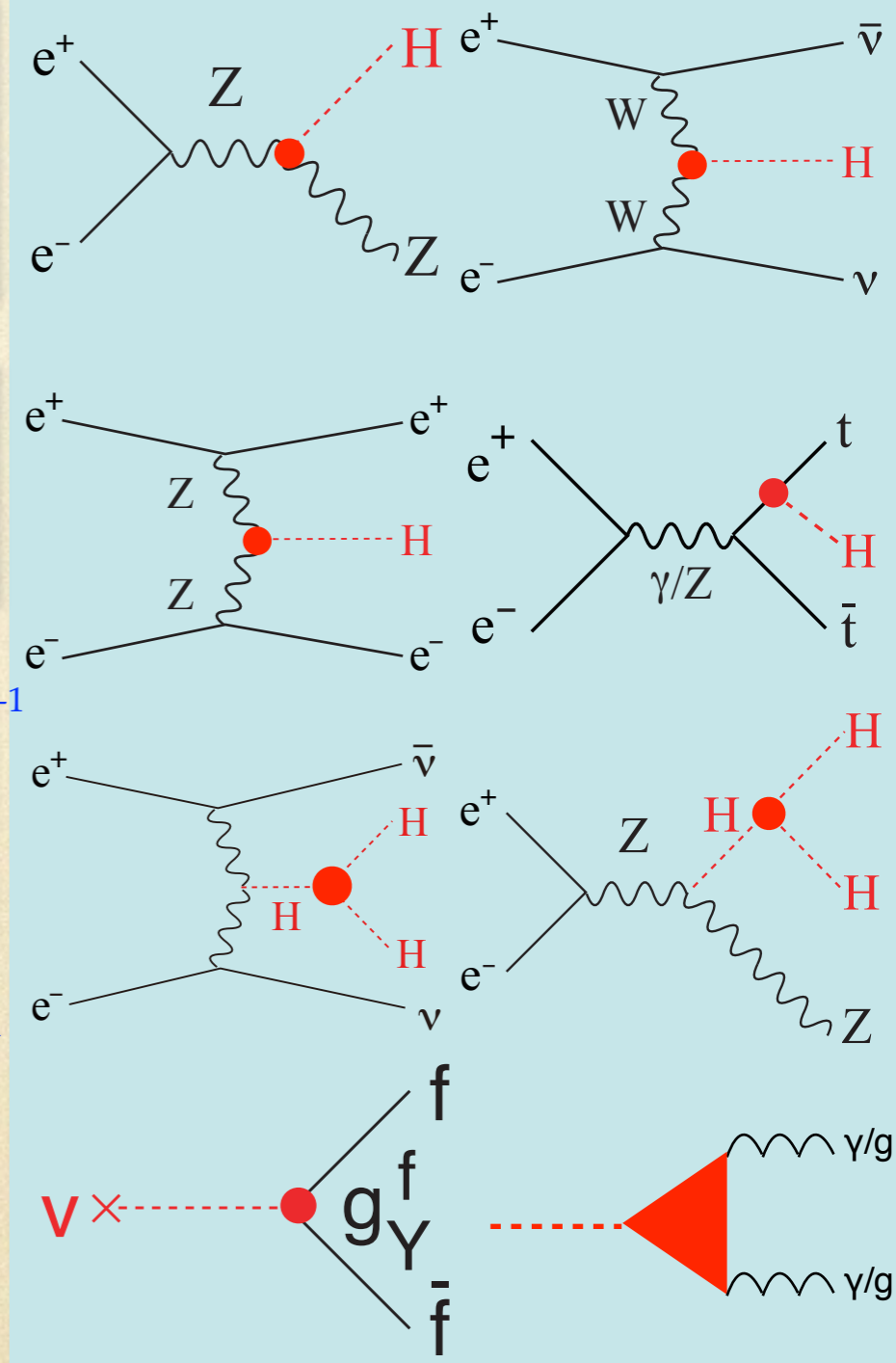
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- ▶ accumulate much more Higgs events
- ▶  $H \rightarrow \mu\mu$  accessible
- ▶ improve Top-Yukawa coupling
- ▶ Higgs self-coupling through  $\nu\nu HH$



$P(e^-, e^+) = (-0.8, +0.3)$  @ 250 - 500 GeV  
 $P(e^-, e^+) = (-0.8, +0.2)$  @ 1 TeV

beam polarisation like a  
 luminosity doubler ( $\nu\nu H$ )!

$\int L \cdot dt = \text{Baseline (TDR is just beginning)} / \text{Luminosity Upgrade (increasing \#bunch, collision rate)}$

# Observables to measure at ILC

- \*  $\sigma_{ZH}$
- \*  $\sigma_{ZH} \times \text{Br}(H \rightarrow bb), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow bb)$
- \*  $\sigma_{ZH} \times \text{Br}(H \rightarrow cc), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow cc)$
- \*  $\sigma_{ZH} \times \text{Br}(H \rightarrow gg), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow gg)$
- \*  $\sigma_{ZH} \times \text{Br}(H \rightarrow WW^*), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow WW^*)$
- \*  $\sigma_{ZH} \times \text{Br}(H \rightarrow ZZ^*), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow ZZ^*)$
- \*  $\sigma_{ZH} \times \text{Br}(H \rightarrow \tau\tau), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow \tau\tau)$
- \*  $\sigma_{ZH} \times \text{Br}(H \rightarrow \gamma\gamma), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow \gamma\gamma)$
- \*  $\sigma_{ZH} \times \text{Br}(H \rightarrow \mu\mu), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow \mu\mu)$
- \*  $\sigma_{ZH} \times \text{Br}(H \rightarrow \text{Invisible})$
- \*  $\sigma_{ttH} \times \text{Br}(H \rightarrow bb)$
- \*  $\sigma_{ZH\bar{H}} \times \text{Br}^2(H \rightarrow bb), \sigma_{\nu\nu H\bar{H}} \times \text{Br}^2(H \rightarrow bb)$

each running stage offers an independent set of measurements

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- \*  $\sigma_{ZH} \times \text{Br}(H \rightarrow bb), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow bb)$
- \*  $\sigma_{ZH} \times \text{Br}(H \rightarrow cc), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow cc)$
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- \*  $\sigma_{ZH} \times \text{Br}(H \rightarrow WW^*), \sigma_{\nu\nu H} \times \text{Br}(H \rightarrow WW^*)$
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each running stage offers an independent set of measurements

# Full Detector Simulation of ILD & SiD

(see detector talks by T.Suehara & M.Oriunno)

Driven by Particle Flow Algorithm, High Granularity,  $\sim 4\pi$  Coverage

momentum resolution:  $\sigma_{1/p_T} \sim 2 \times 10^{-5} \text{ GeV}^{-1}$

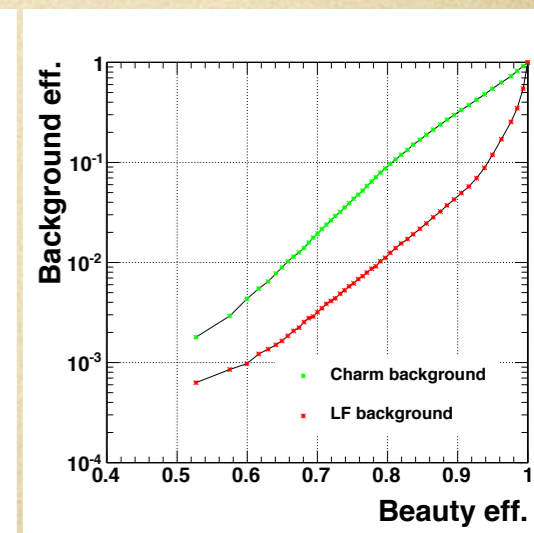
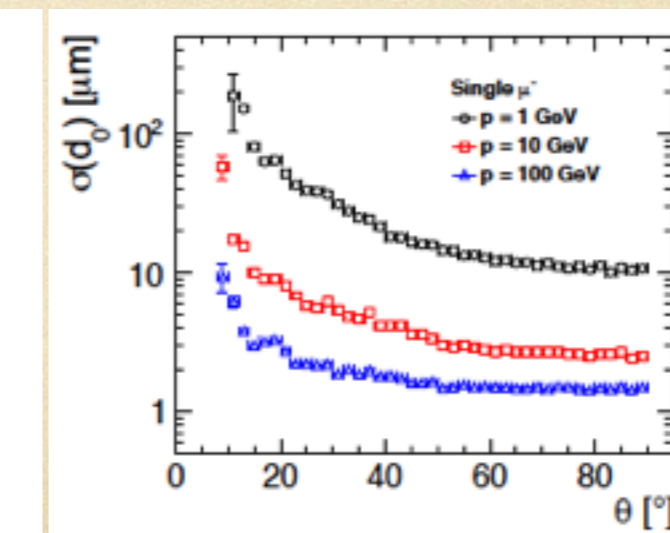
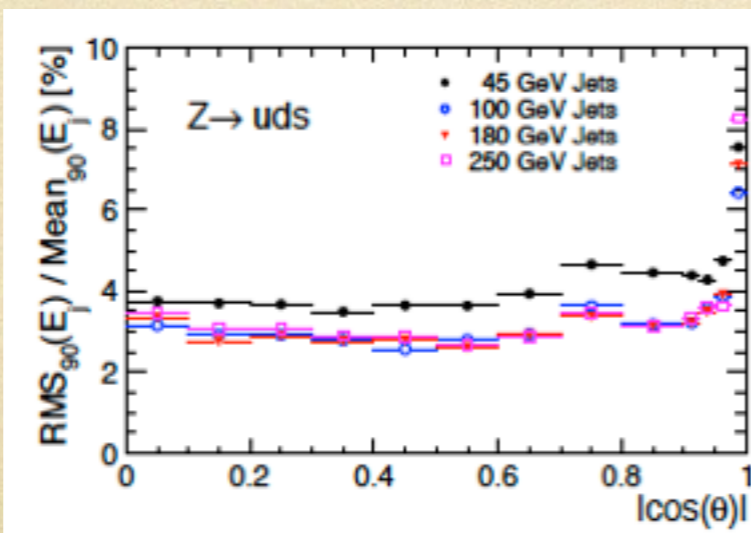
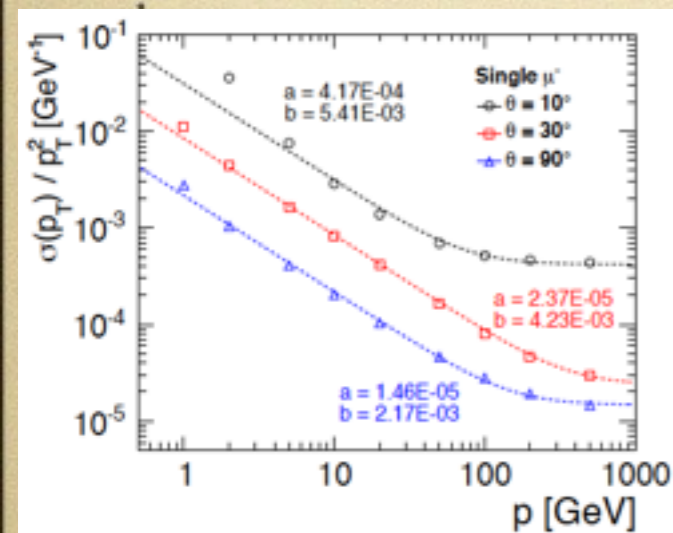
▶ driven by recoil mass measurement  $ZH \rightarrow l^+l^-X$ .

jet energy resolution:  $\sigma_E/E \sim 30\%/\sqrt{E} \sim 3 - 4\% @ 100\text{GeV}$

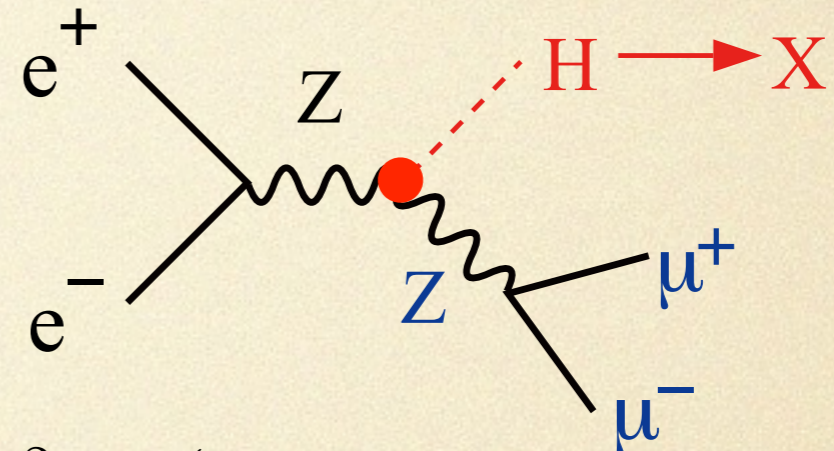
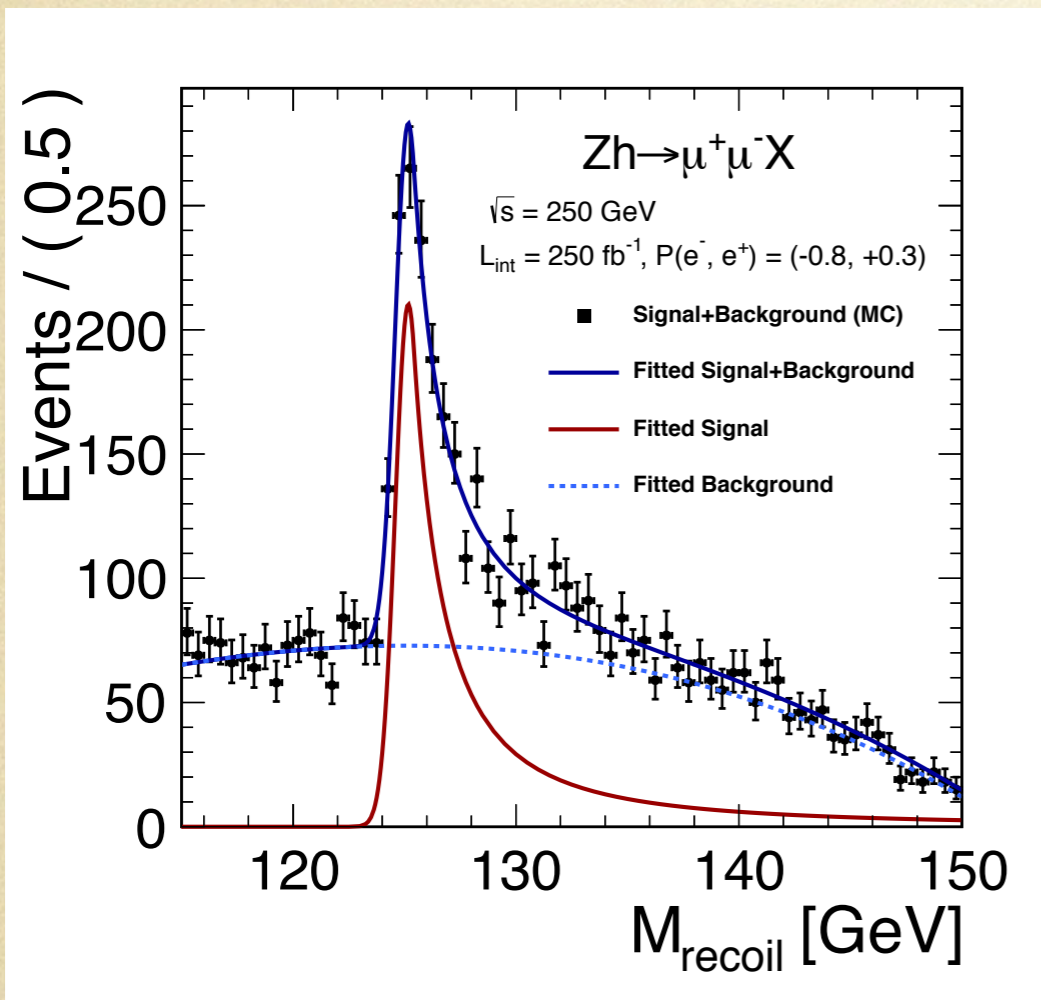
▶ driven by  $3\sigma$  separation of the hadronic decay of W and Z bosons.

impact parameter resolution:  $\sigma_{r\phi} = 5 \mu\text{m} \oplus \frac{10}{p(\text{GeV} \sin^{3/2} \theta)} \mu\text{m}$

▶ driven by excellent tagging and untagging of heavy flavor jets ( $H \rightarrow bb, cc$  and  $gg$ ).



## The flagship measurement of ILC250



$$M_X^2 = (p_{CM} - (p_{\mu^+} + p_{\mu^-}))^2$$

- \* well defined initial states
- \* recoil mass technique
- \* tagged Higgs without looking into H decay
- \* precision mass measurement
- \* absolute cross section of  $e^+e^- \rightarrow ZH$

250 fb<sup>-1</sup> @ 250 GeV  
 $\Delta\sigma_{ZH} / \sigma_{ZH} = 2.6\%$   
 $\Delta m_H = 30 \text{ MeV}$

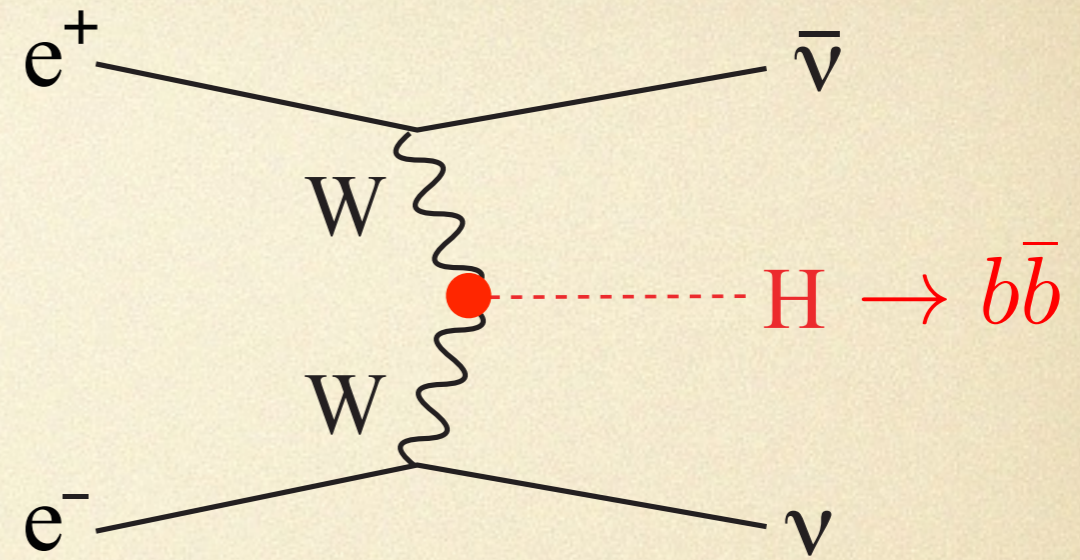
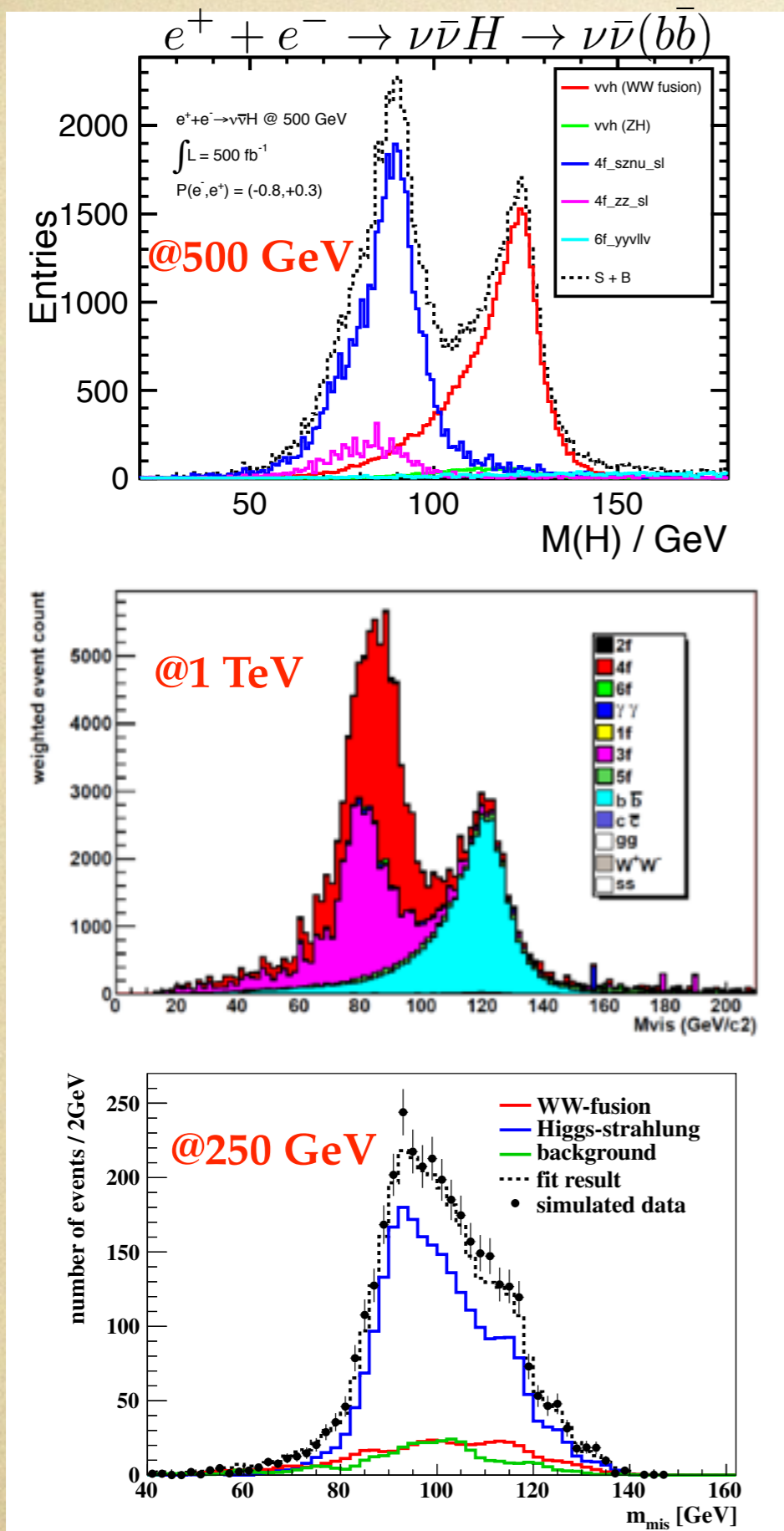
(Z -> e+e- combined, scaled from mH=120 GeV)

key ---> Model-independent measurement of  $\sigma_{ZH}$ , hence HZZ coupling

$$Y_1 = \sigma_{ZH} \propto g_{HZZ}^2$$



# HWW coupling



$$Y_2 = \sigma_{\nu\bar{\nu}H} \cdot \text{Br}(H \rightarrow b\bar{b}) \propto g_{HWW}^2 \cdot \text{Br}(H \rightarrow b\bar{b})$$

$$Y_3 = \sigma_{ZH} \cdot \text{Br}(H \rightarrow b\bar{b}) \propto g_{HZZ}^2 \cdot \text{Br}(H \rightarrow b\bar{b})$$

$$g_{HWW} \propto \sqrt{\frac{Y_2}{Y_3}} \cdot g_{HZZ} \propto \sqrt{\frac{Y_1 Y_2}{Y_3}}$$

- \* it's essential to separate  $\nu\nu H$  from  $ZH$  at lower energy by fitting missing mass (+ angular distribution is ongoing).
- \* much better measured at higher energies.
- \*  $\Delta g_{HWW}$  is actually the limit to all other couplings precisions except  $g_{HZZ}$ .

# Higgs total width $\Gamma_H$

model free, one of the great advantages of ILC

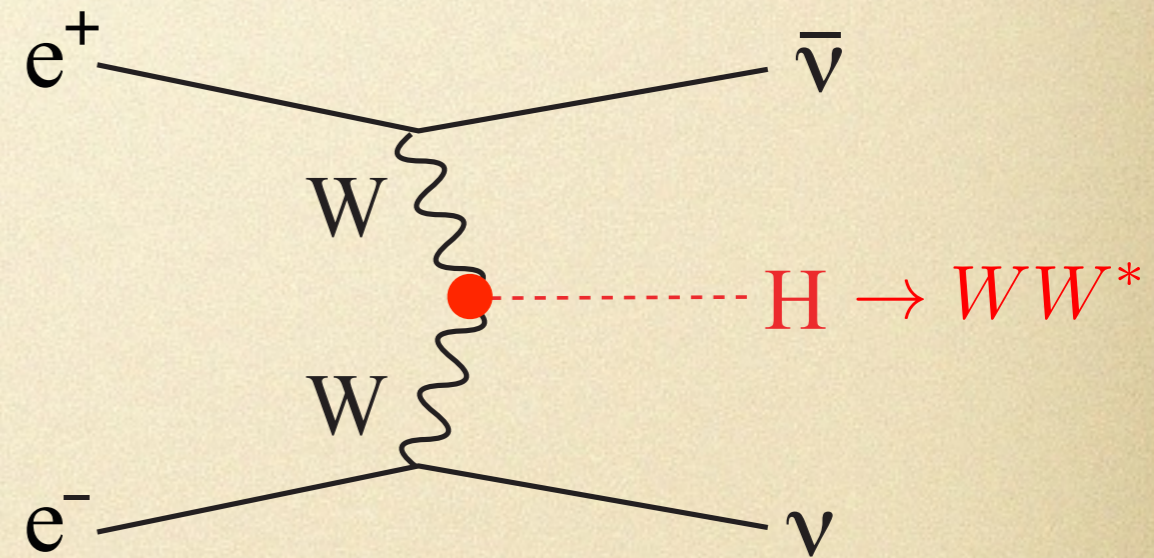
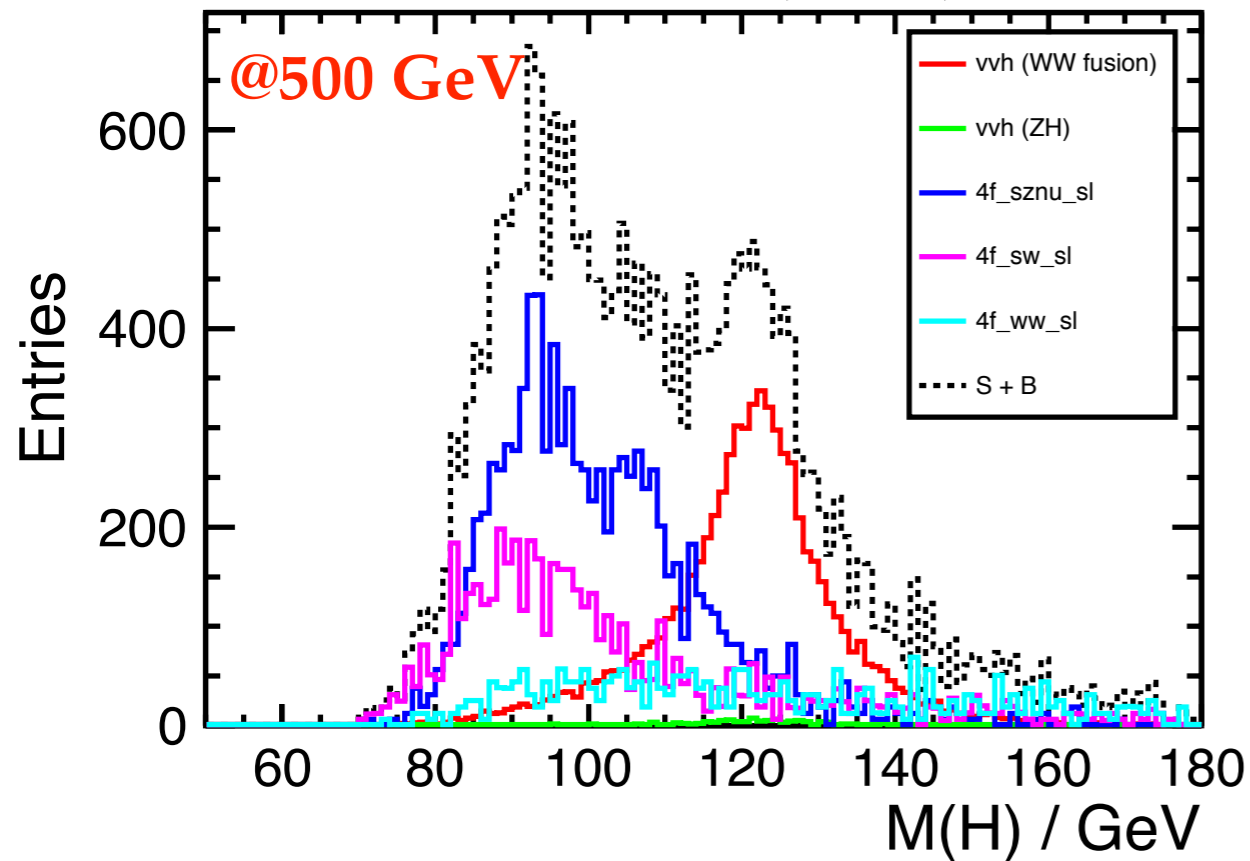
$$\Gamma_H = \frac{\Gamma_{HZZ}}{\text{Br}(H \rightarrow ZZ^*)} \propto \frac{g_{HZZ}^2}{\text{Br}(H \rightarrow ZZ^*)}$$

Br(H->ZZ\*) very small, not very precisely measured

$$\star \Gamma_H = \frac{\Gamma_{HWW}}{\text{Br}(H \rightarrow WW^*)} \propto \frac{g_{HWW}^2}{\text{Br}(H \rightarrow WW^*)}$$

better option!

$e^+ + e^- \rightarrow \nu\bar{\nu}H \rightarrow \nu\bar{\nu}(WW^*) \rightarrow \nu\bar{\nu}qqqq$



$$Y_4 = \sigma_{\nu\bar{\nu}H} \cdot \text{Br}(H \rightarrow WW^*) \propto \frac{g_{HWW}^4}{\Gamma_0}$$

$$\Gamma_H \propto \frac{g_{HWW}^4}{Y_4} \propto \frac{Y_1^2 Y_2^2}{Y_3^2 Y_4}$$

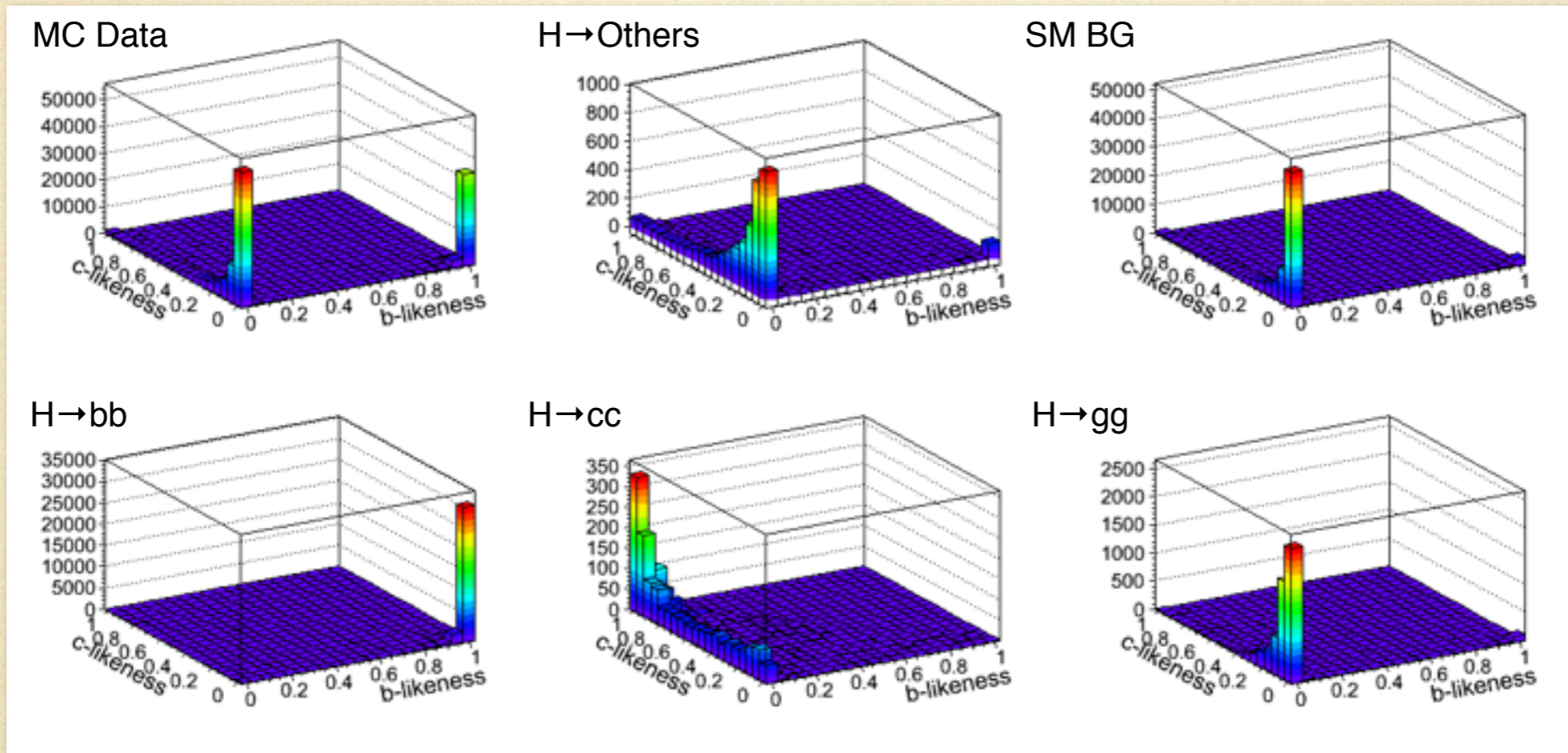
# Higgs couplings to bb, cc and gg

b-vertices and c-vertices can be well reconstructed and separated @ ILC

$$e^+ + e^- \rightarrow ZH \rightarrow f\bar{f}(jj)$$

patterns of b-likeness versus c-likeness of the two jets from Higgs

flavor tagging  
by LCFIPlus  
T.Suehara  
T.Tanabe



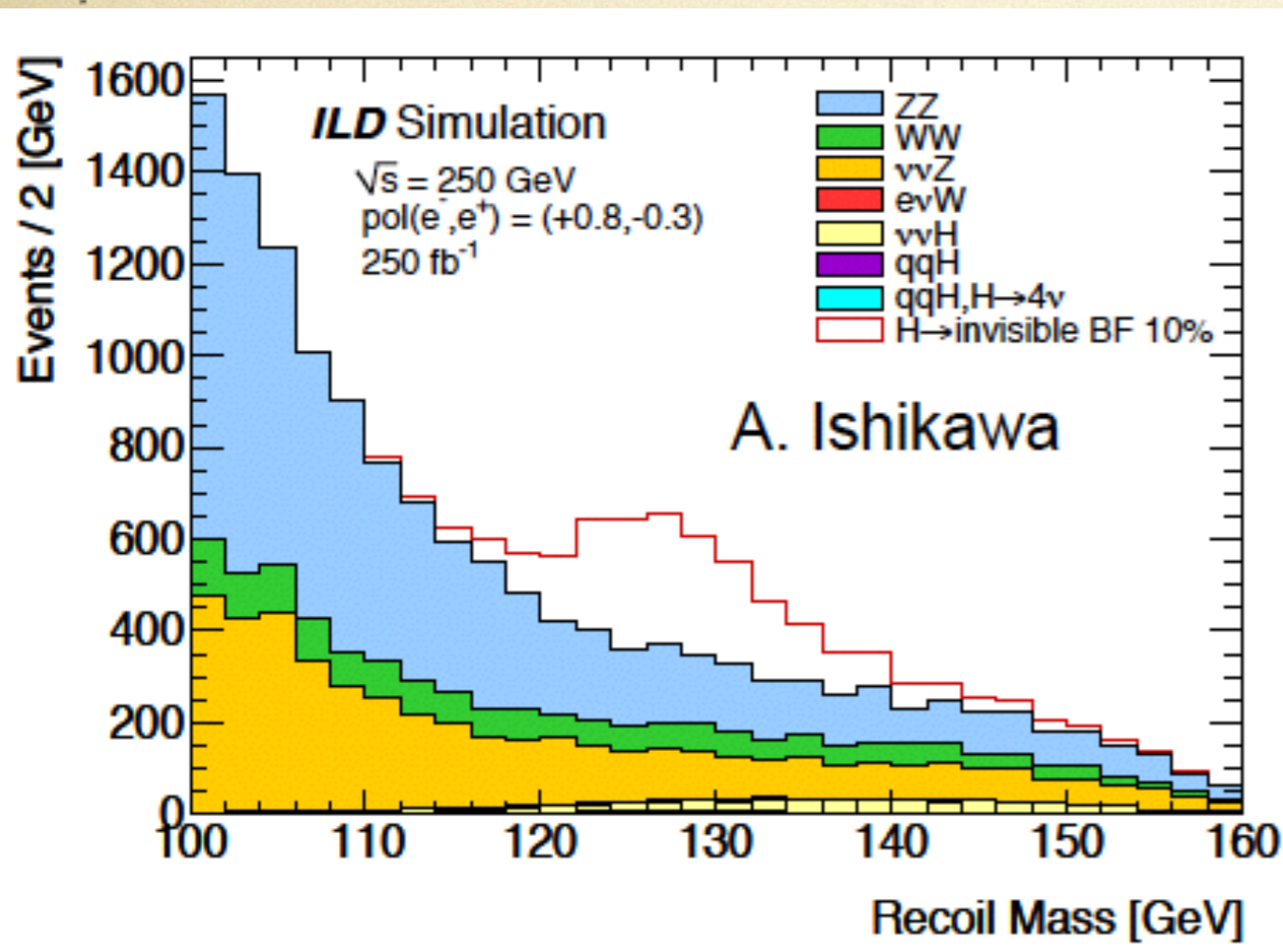
Template Fitting



$$\begin{aligned} \sigma_{ZH} \cdot \text{Br}(H \rightarrow b\bar{b}) &\propto g_{HZZ}^2 g_{Hbb}^2 / \Gamma_H \\ \sigma_{ZH} \cdot \text{Br}(H \rightarrow c\bar{c}) &\propto g_{HZZ}^2 g_{Hcc}^2 / \Gamma_H \\ \sigma_{ZH} \cdot \text{Br}(H \rightarrow gg) &\propto g_{HZZ}^2 g_{Hgg}^2 / \Gamma_H \end{aligned}$$

# Invisible Higgs decay

$$e^+ + e^- \rightarrow ZH \rightarrow l^+ l^- / q\bar{q} + \text{Missing}$$



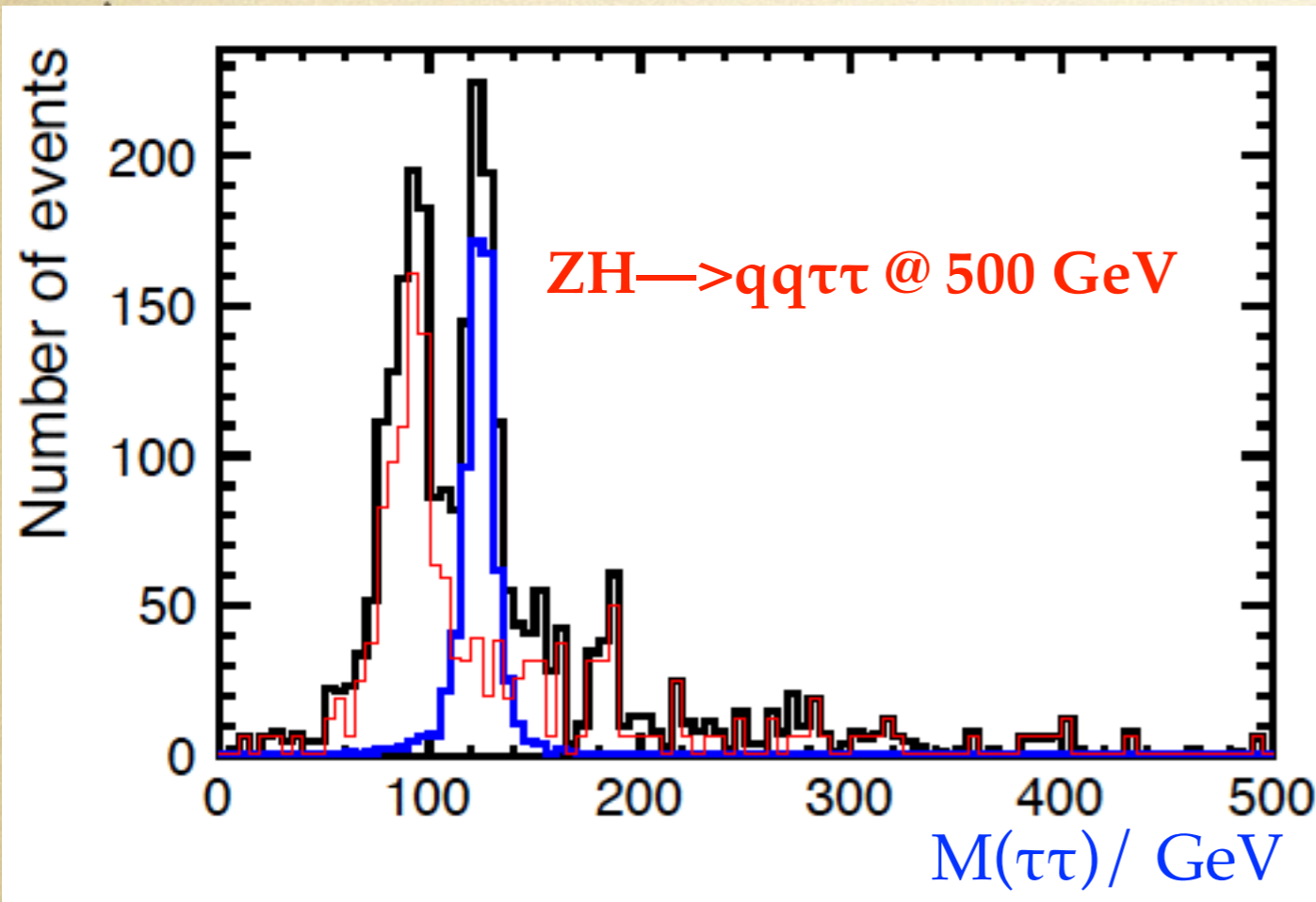
- \*  $Z \rightarrow ll$  or  $qq$ , initial state known
- \* recoil mass technique
- \* model independent
- \*  $\text{Br}(H \rightarrow \text{Inv.}) < 0.95\% @ 95\% \text{ C.L.}$

(ILC250 Baseline)

A. Ishikawa @ Snowmass Energy Frontier Workshop, Seattle, June 30 - July 3, 2013

# H $\tau\tau$ coupling

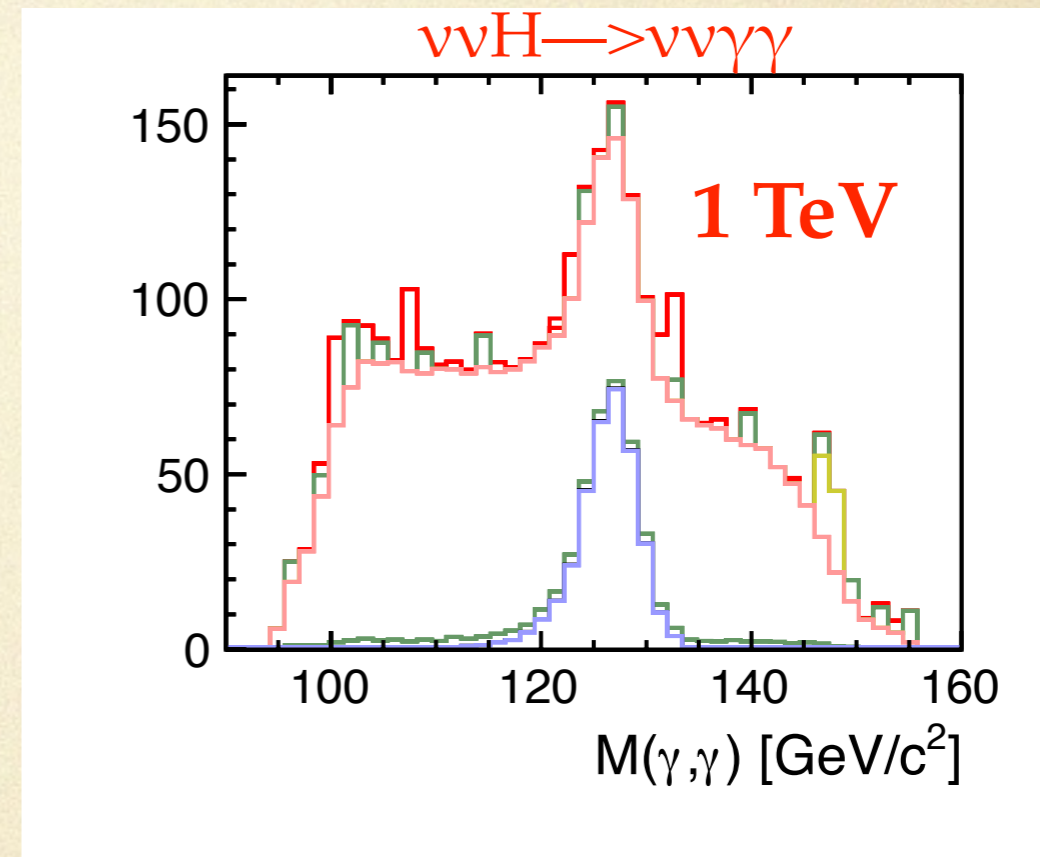
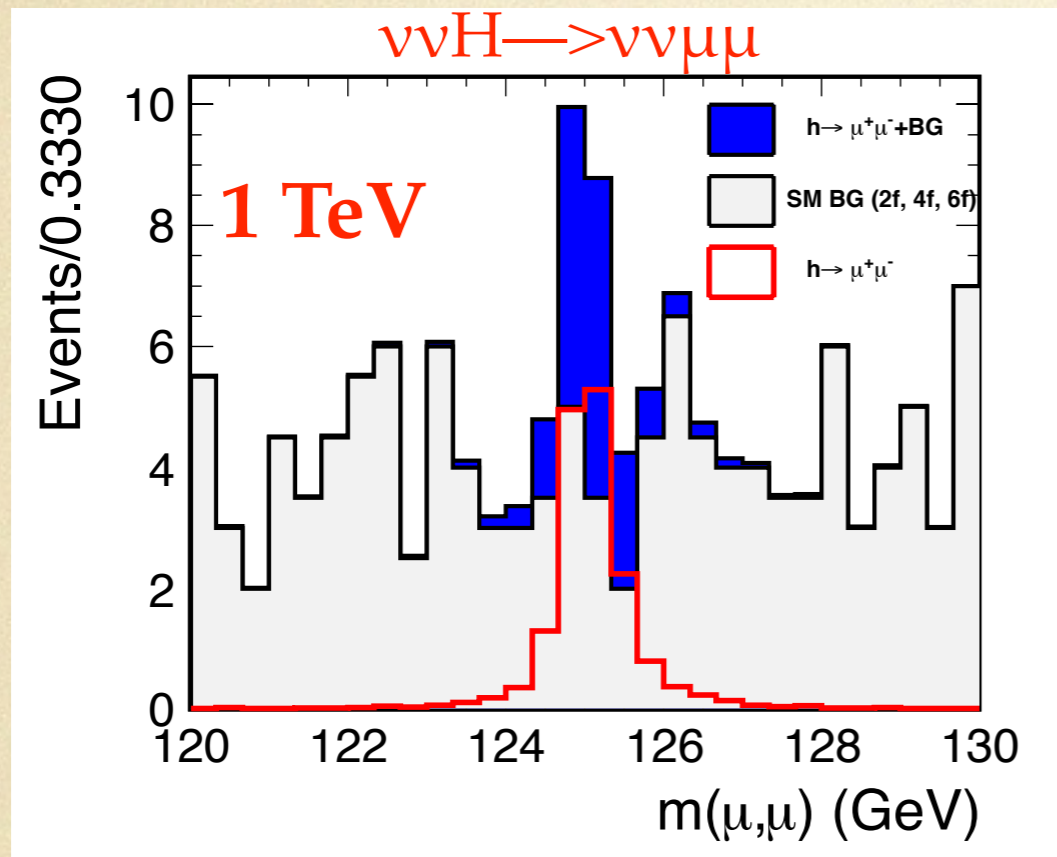
$$e^+ + e^- \rightarrow ZH \rightarrow l^+ l^- / q\bar{q} / \nu\bar{\nu} + \tau^+ \tau^-$$



- \*sophisticated 1/3-prong  $\tau$  finder.
- \* $\tau$  vertex detectable.
- \*neutrino momenta recoverable by using collinear approximation (or 6C fitting, ongoing) for  $Z \rightarrow ll, qq$ .

$$\sigma_{ZH} \cdot \text{Br}(H \rightarrow \tau^+ \tau^-) \propto \frac{g_{HZZ}^2 g_{H\tau\tau}^2}{\Gamma_H}$$

# Higgs couplings to $\gamma\gamma$ and $\mu\mu$

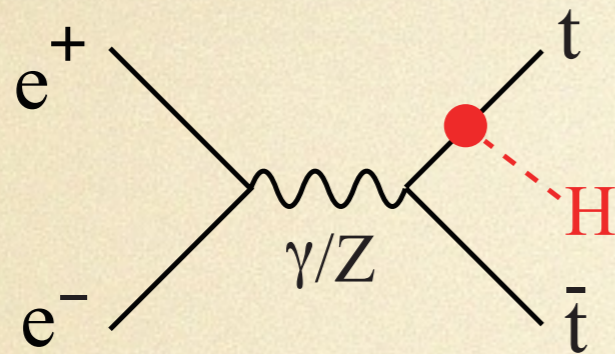


- \* limited by very small BRs, better at higher energies via WW-fusion production  $e^+e^- \rightarrow \nu\nu H$ .
- \* very characteristic signals (events with only two high energy muons or photons).
- \* background dominated by irreducible continuous SM process.
- \* limited by statistics, good synergy with LHC measurements.

$$\sigma_{\nu\bar{\nu}H} \cdot \text{Br}(H \rightarrow \mu^+\mu^-) \propto \frac{g_{HWW}^2 g_{H\mu\mu}^2}{\Gamma_H}$$

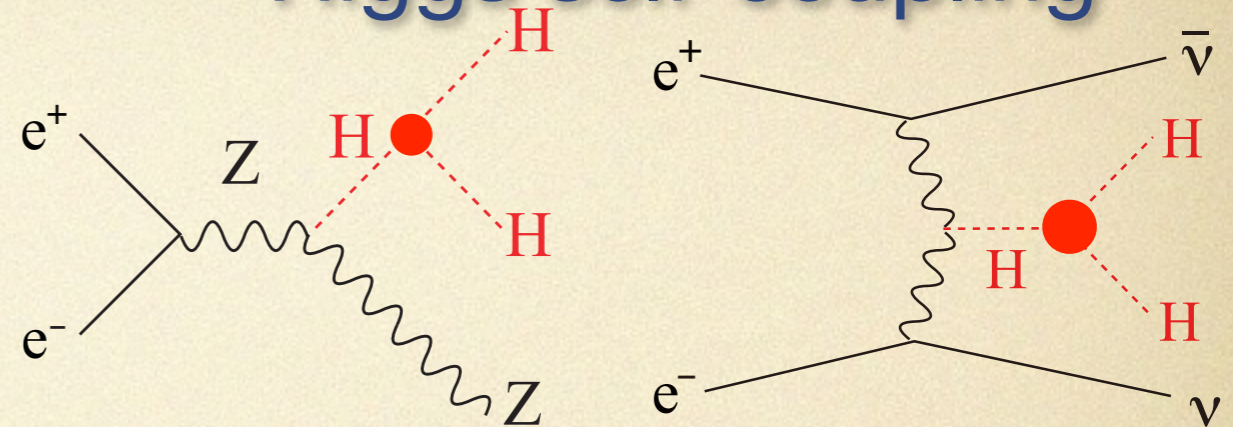
$$\sigma_{\nu\bar{\nu}H} \cdot \text{Br}(H \rightarrow \gamma\gamma) \propto \frac{g_{HWW}^2 g_{H\gamma\gamma}^2}{\Gamma_H}$$

# Top-Yukawa coupling



- \*largest Yukawa coupling.
- \*cross section significantly enhanced from QCD bound state effect at round threshold.
- \*counting experiment,  $\sigma_{ttH} \propto g_{Htt}^2$  direct measurement of  $g_{Htt}$ .
- \*multi-jets final states, detector benchmark analyses.

# Higgs self-coupling



- \*force that makes vacuum condense.
- \* $\Delta\sigma/\sigma$  of double Higgs production measured well.
- \*significant irreducible diagrams effect (interference),  $\Delta g/g = F \cdot \Delta\sigma/\sigma$ ,  $F > 0.5$
- \*new weighting method.
- \*challenging analysis, key is flavor tagging, jet-clustering, etc.

$\Delta g_{ttH} / g_{ttH}$	500 GeV	+ 1 TeV
Baseline	14%	3.2%
LumiUP	7.8%	2%

$\Delta \lambda_{HHH} / \lambda_{HHH}$	500 GeV	+ 1 TeV
Baseline	83%	21%
LumiUP	46%	13%

# Summary of observables @ ILC

Baseline

250 GeV: 250 fb<sup>-1</sup>  
 500 GeV: 500 fb<sup>-1</sup>  
 1 TeV: 1000 fb<sup>-1</sup>

$m_H = 125 \text{ GeV}$   
 $P(e^-, e^+) = (-0.8, +0.3) @ 250, 500 \text{ GeV}$   
 $P(e^-, e^+) = (-0.8, +0.2) @ 1 \text{ TeV}$

ILD & SiD: DBD

ECM	@ 250 GeV		@ 500 GeV		@ 1 TeV
luminosity · fb	250		500		1000
polarization (e <sup>-</sup> , e <sup>+</sup> )	(-0.8, +0.3)		(-0.8, +0.3)		(-0.8, +0.2)
process	ZH	vvH(fusion)	ZH	vvH(fusion)	vvH(fusion)
cross section	2.6%	-	3.0%	-	-
	$\sigma \cdot \text{Br}$	$\sigma \cdot \text{Br}$	$\sigma \cdot \text{Br}$	$\sigma \cdot \text{Br}$	$\sigma \cdot \text{Br}$
H <sup>-&gt;</sup> bb	1.2%	10.5%	1.8%	0.66%	0.32%
H <sup>-&gt;</sup> cc	8.3%		13%	6.2%	3.1%
H <sup>-&gt;</sup> gg	7%		11%	4.1%	2.3%
H <sup>-&gt;</sup> WW*	6.4%		9.2%	2.4%	1.6%
H <sup>-&gt;</sup> $\tau\tau$	4.2%		5.4%	9%	3.1%
H <sup>-&gt;</sup> ZZ*	19%		25%	8.2%	4.1%
H <sup>-&gt;</sup> $\gamma\gamma$	29-38%		29-38%	20-26%	7-10%
H <sup>-&gt;</sup> $\mu\mu$	-		-		31%
ttH, H <sup>-&gt;</sup> bb	-		28%		6%
H <sup>-&gt;</sup> Inv. (95% C.L.)	< 0.95%				-

being updated by new studies with  $m_H = 125 \text{ GeV}$



# From observables to couplings — Global Fit

K.Fujii @ Pheno2014, Pittsburgh

ILC Higgs White Paper

arXiv: 1310.0763

$$\chi^2 = \sum_{i=1}^{35} \left( \frac{Y_i - Y'_i}{\Delta Y_i} \right)^2$$

$$Y'_i = F_i \cdot \frac{g_{HA_i A_i}^2 \cdot g_{HB_i B_i}^2}{\Gamma_0} \quad (A_i = Z, W, t)$$

(i = 1, ..., 33)

$$(B_i = b, c, \tau, \mu, g, \gamma, Z, W : \text{decay})$$

$$F_i = S_i G_i \dots \dots G_i = \left( \frac{\Gamma_i}{g_i^2} \right)$$

$$S_i = \left( \frac{\sigma_{ZH}}{g_{HZZ}^2} \right), \left( \frac{\sigma_{\nu\bar{\nu}H}}{g_{HWW}^2} \right), \text{ or } \left( \frac{\sigma_{t\bar{t}H}}{g_{Htt}^2} \right)$$

- It is the recoil mass measurement that is the key to unlock the door to this completely model-independent analysis!
- Cross section calculations (S<sub>i</sub>) do not involve QCD ISR.
- Partial width calculations (G<sub>i</sub>) do not need quark mass as input.

## Systematic Errors

	Baseline	LumUp
luminosity	0.1%	0.05%
polarization	0.1%	0.05%
b-tag efficiency	0.3%	0.15%

★ theoretical calculations of Higgs particle widths are now at O(1%), and are expected to achieve per-mille level in next decade! (M.Peskin, et. al, arXiv:1404.0319)

# Precisions of absolute Higgs couplings @ ILC

model independent global fit

coupling $\Delta g/g$	Baseline			LumiUP		
	250 GeV	+ 500 GeV	+ 1 TeV	250 GeV	+ 500 GeV	+ 1 TeV
HZZ	1.3%	1%	1%	0.61%	0.51%	0.51%
HWW	4.8%	1.2%	1.1%	2.3%	0.58%	0.56%
Hbb	5.3%	1.6%	1.3%	2.5%	0.83%	0.66%
Hcc	6.8%	2.8%	1.8%	3.2%	1.5%	1%
Hgg	6.4%	2.3%	1.6%	3%	1.2%	0.87%
H $\tau\tau$	5.7%	2.3%	1.7%	2.7%	1.2%	0.93%
H $\gamma\gamma$	18%	8.4%	4%	8.2%	4.5%	2.4%
H $\mu\mu$	-	-	16%	-	-	10%
Htt	-	14%	3.1%	-	7.8%	1.9%
$\Gamma$	11%	5%	4.6%	5.4%	2.5%	2.3%
Br(Inv)	<0.95%	<0.95%	<0.95%	0.44%	0.44%	0.44%
HHH	-	83%	21%	-	46%	13%

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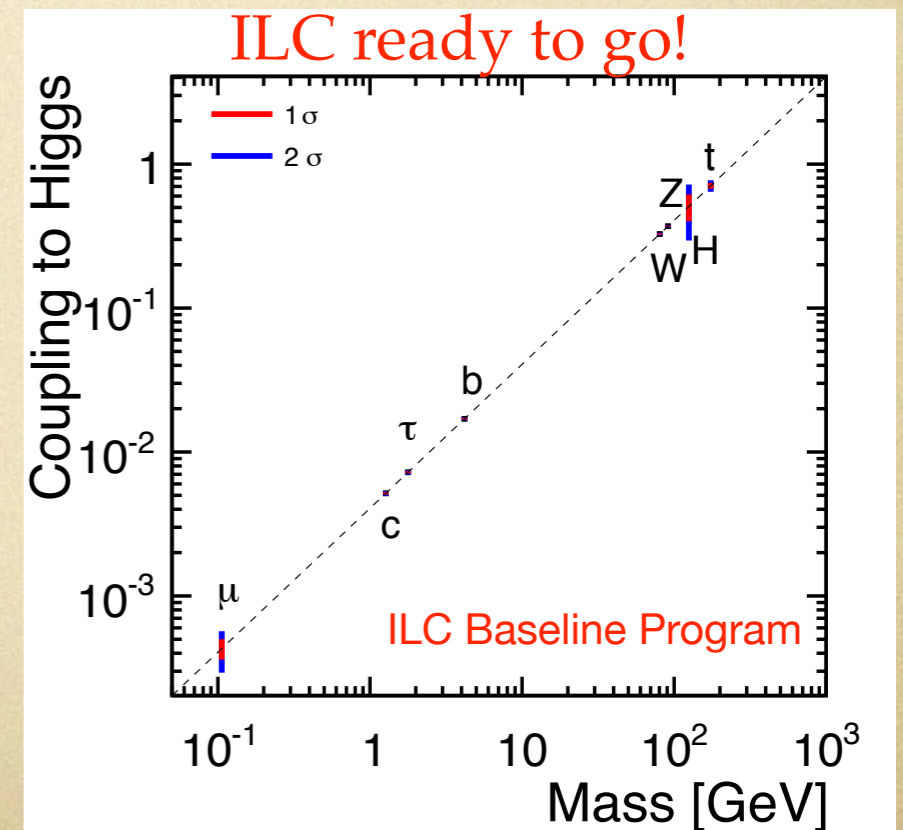
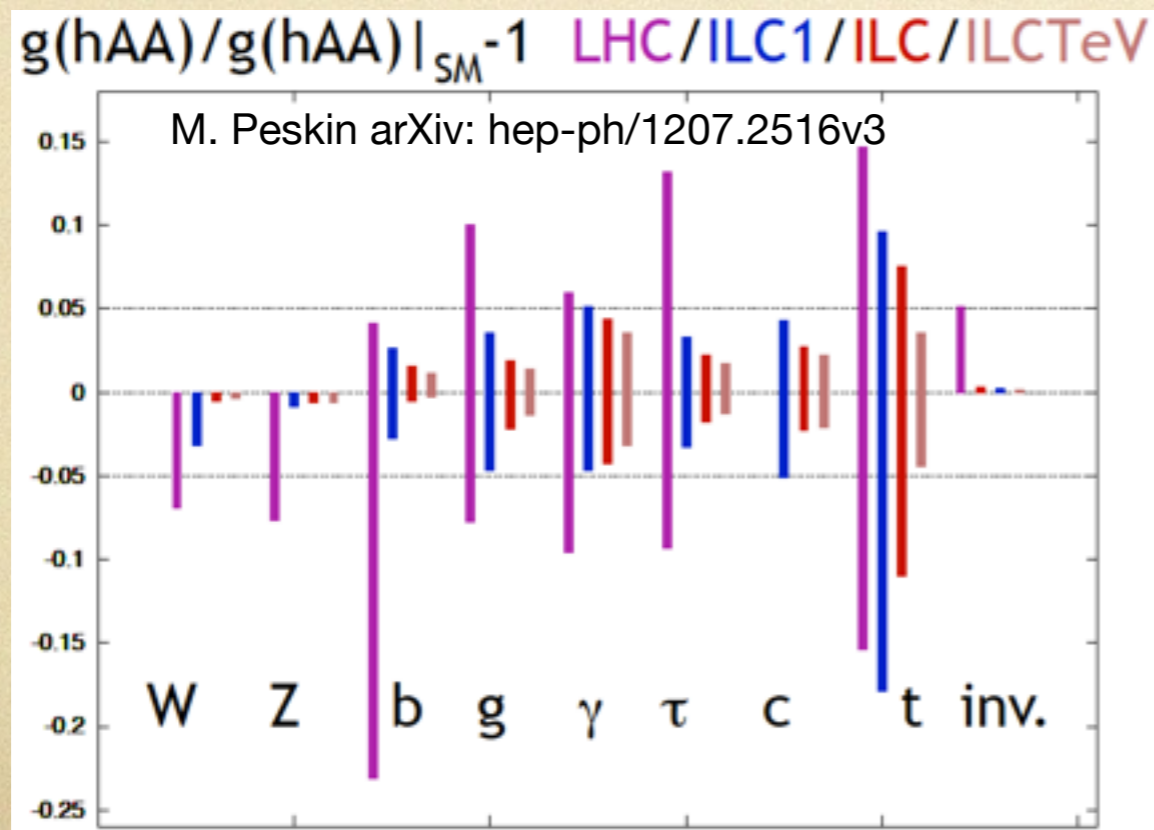
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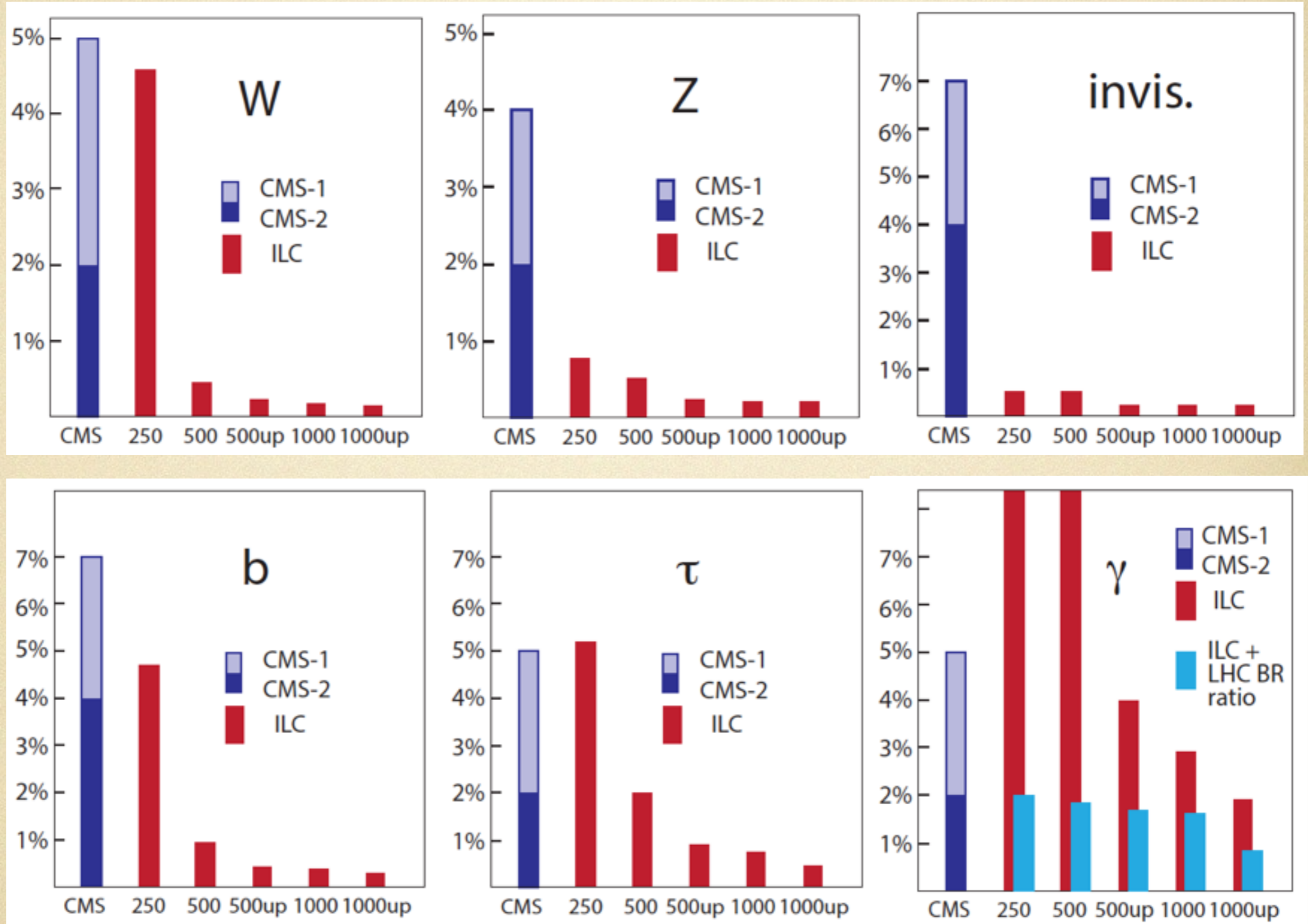
# Summary

- \* ILC is the ideal machine to measure all Higgs boson couplings precisely and model independently, eventually to reveal the nature of EWSB and mass generation; performance of detectors ILD & SiD can meet the physics goal.
- \* Recoil mass measurement @ 250 GeV gives the absolute HZZ coupling, be able to model independently normalize all the Higgs couplings and total width; HWW coupling determination is crucial for precisions of all other couplings, and is essential to be improved significantly at higher ECM.
- \* It is essential to go to 500 GeV to directly measure top-Yukawa coupling and Higgs self-coupling which can be further improved at 1 TeV.
- \* Complementary to LHC, ability of energy scan and beam polarization can make ILC run at optimal energy and study in detail what LHC would discover.



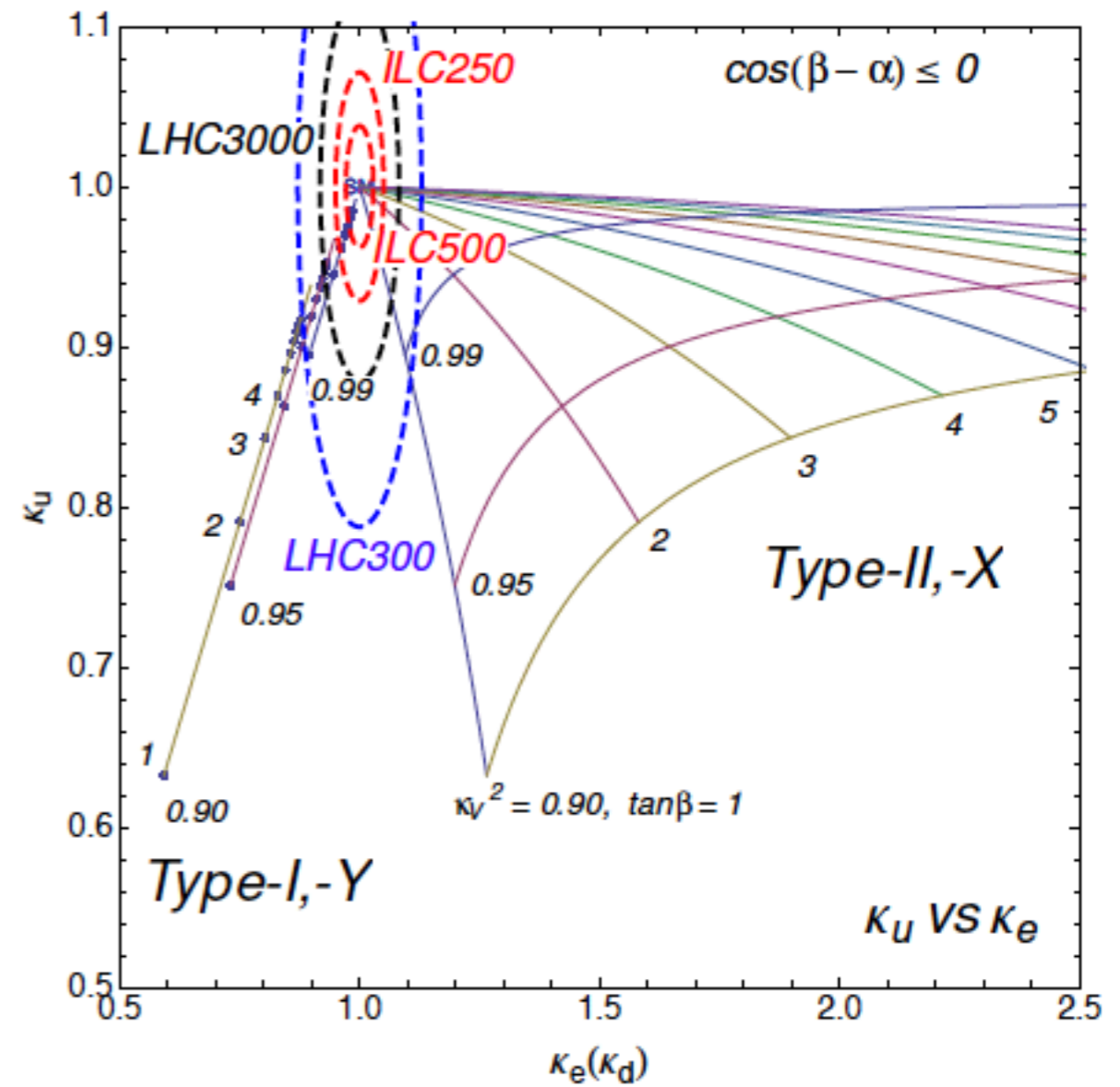
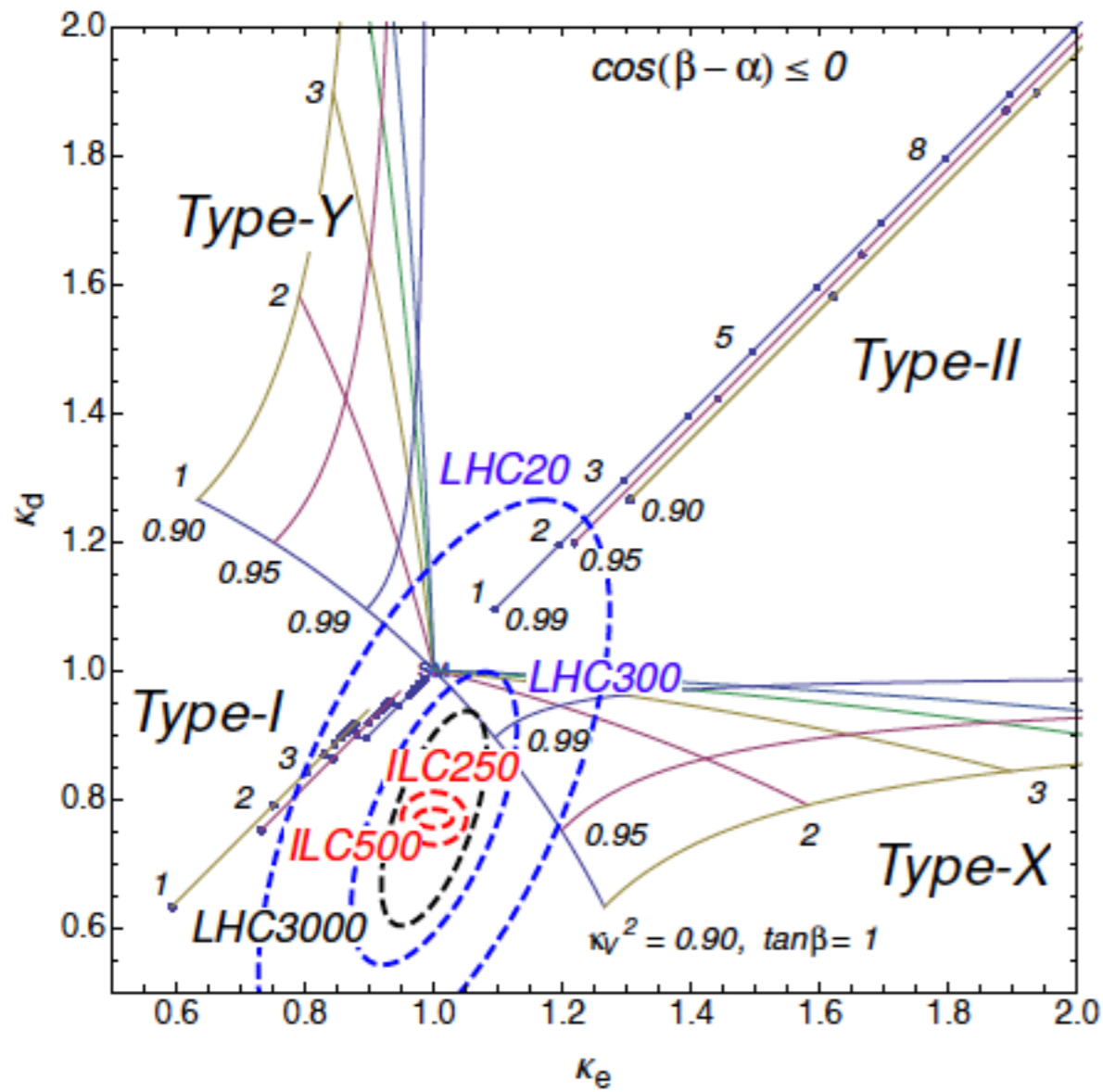
backup

# LHC and ILC comparison / synergy





# Fingerprinting non-minimal Higgs sector



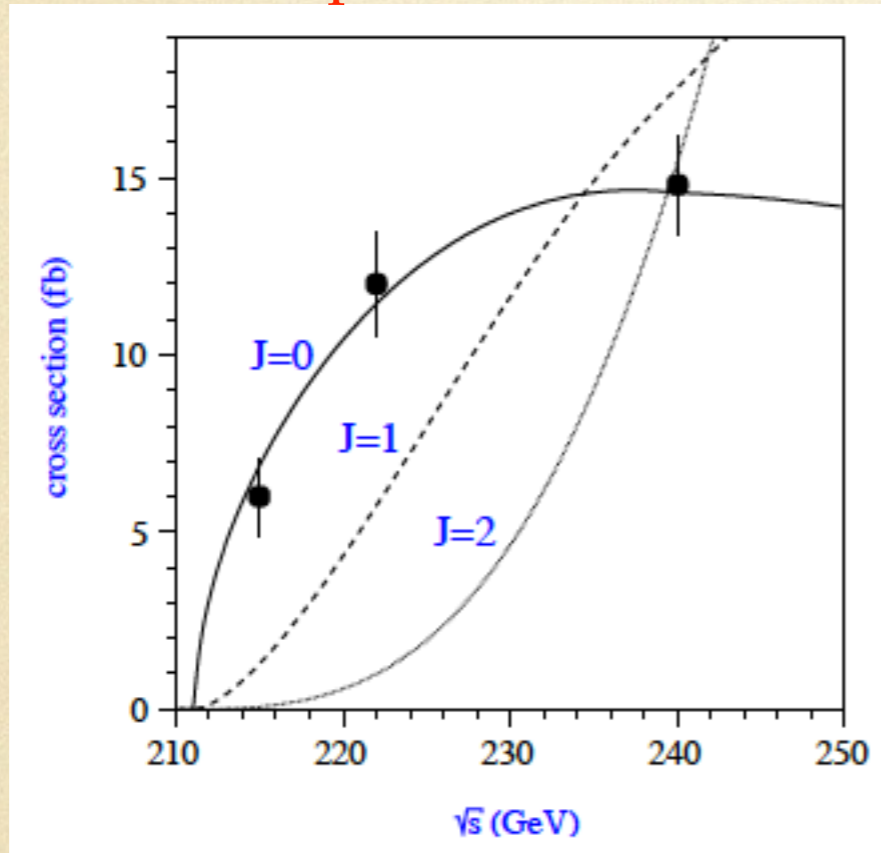
S.Kanemura, K.Yagyu, et al., arXiv: 1406.3294

# Higgs Quantum Numbers

$J^{CP}$

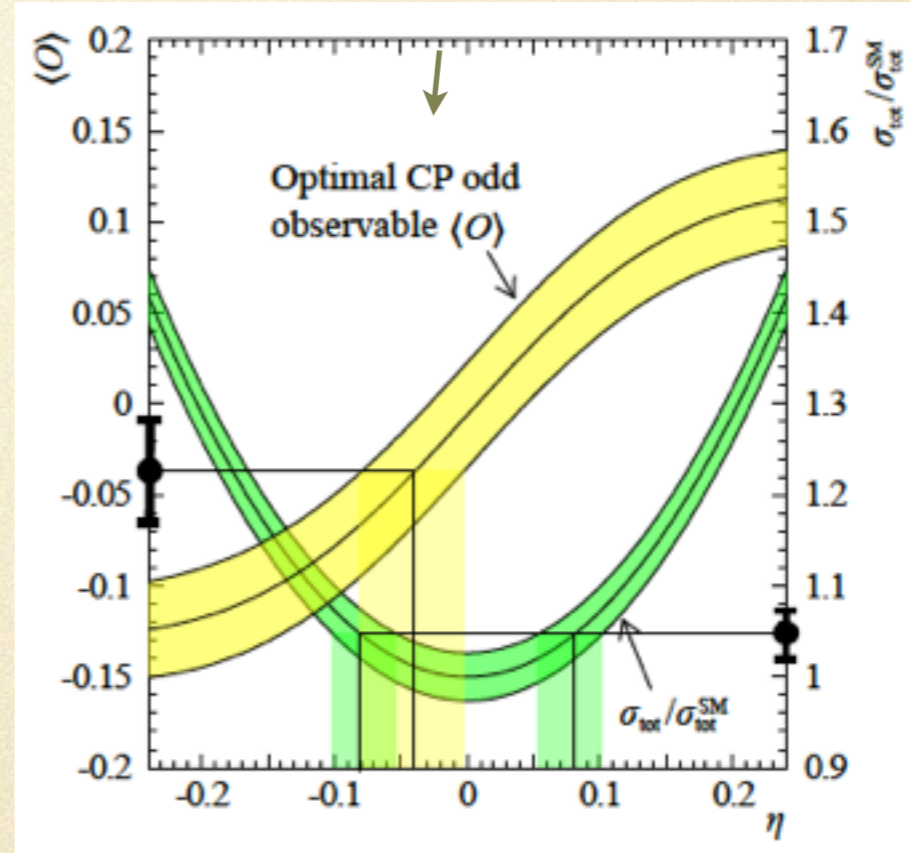
in addition to the spin study by  $H \rightarrow ZZ^*$  and  $WW^*$ , ILC offers an orthogonal way and be able to measure the mixture of CP

three-20 fb<sup>-1</sup>-points threshold scan



W.Lohmann, et al., arXiv: hep-ph/0302113

if a mixture of CP even and CP odd



--> few % of mixing angle

M. Schumacher, LC Note LC-PHSM-2001-003

a more complete CP search program

$$A(X_{J=0} \rightarrow VV) = v^{-1} \left( a_1 m_V^2 \epsilon_1^* \epsilon_2^* + a_2 f_{\mu\nu}^{*(1)} f^{*(2),\mu\nu} + a_3 f_{\mu\nu}^{*(1)} \tilde{f}^{*(2),\mu\nu} \right)$$

$$A(X_{J=0} \rightarrow f\bar{f}) = \frac{m_f}{v} \bar{u}_2 (b_1 + ib_2 \gamma_5) u_1$$

\* via production channels  $e^+e^- \rightarrow ZH$  and  $e^+e^-H$  (ZZ-fusion): probe anomalous HZZ coupling.

\* via decay  $H \rightarrow WW^*$ : probe anomalous HWW coupling.

\* via decay  $H \rightarrow \tau^+\tau^-$ : probe CP mixture for down-type coupling

\* via production  $e^+e^- \rightarrow t\bar{t}H$ : probe CP mixture up-type coupling.

# limiting factors of coupling precisions

$$Y_1 = \sigma_{ZH} \propto g_{HZZ}^2$$

$$Y_2 = \sigma_{\nu\bar{\nu}H} \cdot \text{Br}(H \rightarrow b\bar{b}) \propto \frac{g_{HWW}^2 g_{Hbb}^2}{\Gamma_H}$$

$$Y_3 = \sigma_{ZH} \cdot \text{Br}(H \rightarrow b\bar{b}) \propto \frac{g_{HZZ}^2 g_{Hbb}^2}{\Gamma_H}$$

$$Y_4 = \sigma_{\nu\bar{\nu}H} \cdot \text{Br}(H \rightarrow WW^*) \propto \frac{g_{HWW}^4}{\Gamma_H}$$

$$\Delta g_{HZZ} \sim \frac{1}{2} \Delta Y_1$$

$$\Delta g_{HWW} \sim \frac{1}{2} \Delta Y_1 \oplus \frac{1}{2} \Delta Y_2 \oplus \frac{1}{2} \Delta Y_3$$

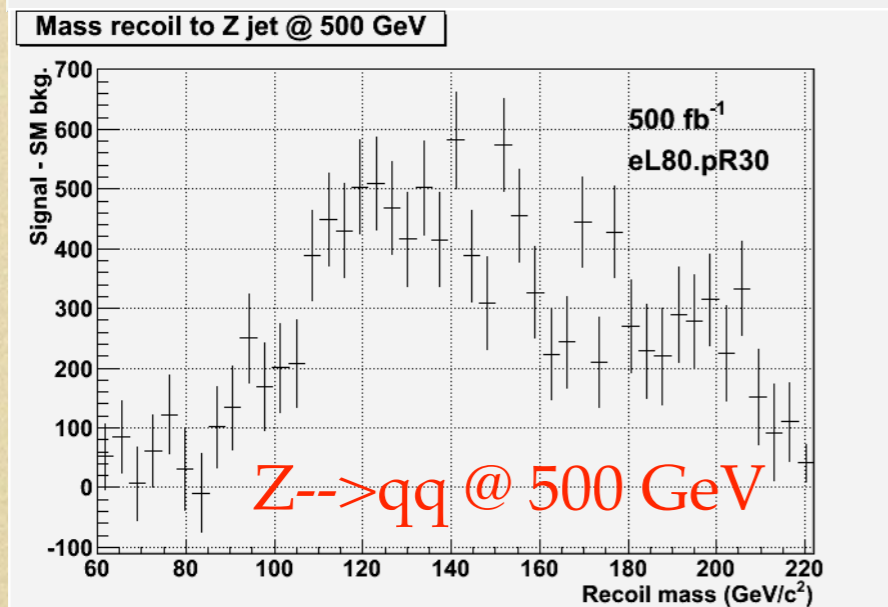
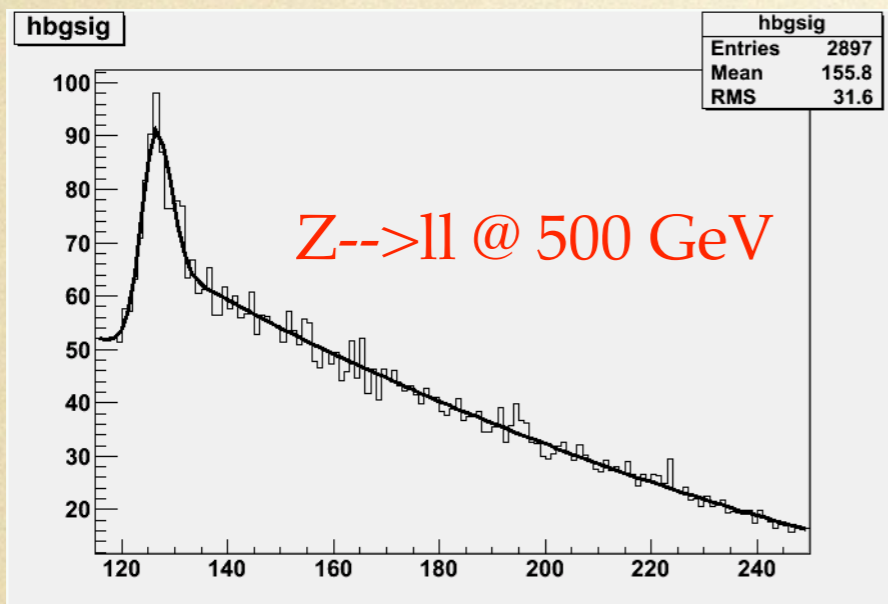
$$\Delta g_{Hbb} \sim \frac{1}{2} \Delta Y_1 \oplus \Delta Y_2 \oplus \frac{1}{2} \Delta Y_3 \oplus \frac{1}{2} \Delta Y_4$$

$$\Delta \Gamma_H \sim 2\Delta Y_1 \oplus 2\Delta Y_2 \oplus 2\Delta Y_3 \oplus \Delta Y_4$$

both ZH and  $\nu\nu H$   
productions matter!

# recoil against $Z \rightarrow ll, qq$ at 500 GeV

study ongoing, preliminary



- performance using  $Z \rightarrow ll$  depends on momentum resolution, which is usually worse at higher energy, but partly compensated by higher luminosity
- recoil technique can be also applied to  $Z \rightarrow qq$  mode, more boosted at higher energy, better separation between Z and H decay products

$\Delta g_{HZZ} / g_{HZZ}$	250 GeV	+ 500 GeV
Baseline	1.3%	1%
LumiUP	0.61%	0.51%

S. Watanuki, T. Suehara,  
A. Miyamoto, arXiv: 1311.2248

# recoil against $Z \rightarrow qq$ at 250 GeV

study ongoing, preliminary

Cut efficiency (ex. 4-jet, 0-lepton) Cont.

mode	before	after	difference from mean	$\epsilon_n^i \times \frac{\Delta\epsilon_n^i}{\epsilon^i}$	$BR_n \times \epsilon_n^i \times \frac{\Delta\epsilon_n^i}{\epsilon^i}$
H→all (100%)	216,195 (41.2%)	53.0%	---	---	---
H→bb (55.6%)	128,085 (44.0%)	51.1%	-1.9%	-1.6%	-0.9%
H→WW (l) (2.4%)	1,331 (10.7%)	58.2%	+5.2%	+1.0%	0.0%
H→WW (sl) (10.0%)	13,588 (25.8%)	61.0%	+8.0%	+3.9%	+0.4%
H→WW (h) (10.5%)	16,471 (29.9%)	41.3%	-11.7%	-6.6%	-0.7%
H→gg (9.0%)	24,154 (51.0%)	52.8%	-0.2%	-0.2%	0.0%
H→ττ (6.7%)	18,354 (52.3%)	69.6%	+16.6%	+16.4%	+1.1%
H→ZZ (3.0%)	5,696 (36.4%)	54.0%	+1.0%	+0.7%	0.0%
H→cc (2.6%)	7,503 (54.2%)	54.0%	+1.0%	+1.0%	0.0%
H→γγ (0.4%)	1,135 (56.9%)	54.8%	+1.8%	+1.9%	0.0%

cut efficiencies are almost the same except for tau and W.

Americas Workshop on Linear Colliders 14/05/2014 : Tatsuhiko Tomita

14

## model dependent fit (7 parameters @ LHC)

$$\chi^2 = \sum_{i=1}^{i=33} \left( \frac{Y_i - Y'_i}{\Delta Y_i} \right)^2 + \left( \frac{\xi_{ct}}{\Delta \xi_{ct}} \right)^2 + \left( \frac{\xi_{\mu\tau}}{\Delta \xi_{\mu\tau}} \right)^2 + \left( \frac{\xi_{\Gamma}}{\Delta \xi_{\Gamma}} \right)^2$$

$$\xi_{ct} = \kappa_c - \kappa_t$$

$$\xi_{\mu\tau} = \kappa_{\mu} - \kappa_{\tau}$$

$$\xi_{\Gamma} = \kappa_H - \sum_i \kappa_i^2 \text{Br}_i |_{\text{SM}}$$

$$\Delta \xi_{ct} = \Delta \xi_{\mu\tau} = 0.5\%$$

$$\Delta \xi_{\Gamma} = 0.5\% \times 0.63$$

## theory error (loop, parameter)

$$\Delta_{\text{Theory}} = 0 ; 0.1\% ; 0.5\%$$

$$\Delta Y_i^2 = \Delta Y_i^2(\text{exp}) + (\Delta_{\text{Theory}} Y'_i)^2$$

## systematic error

	Baseline	LumiUP
luminosity	0.1%	0.05%
polarisation	0.1%	0.05%
b-tag efficiency *	0.3%	0.15%

(\* only for H $\rightarrow$ bb)

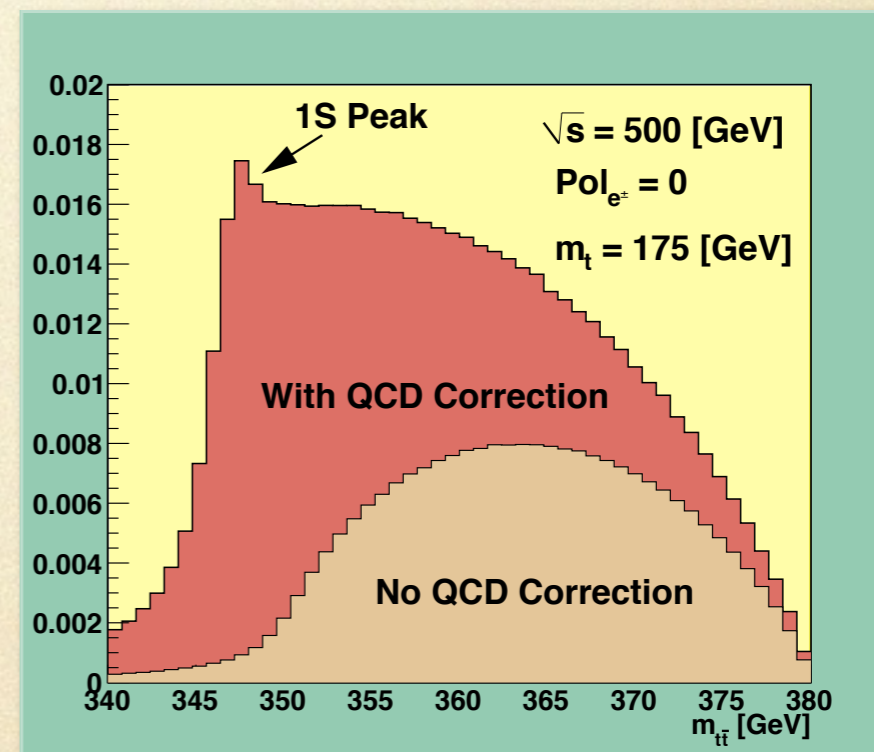
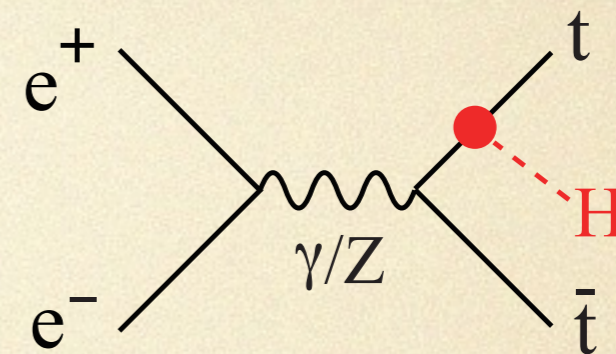
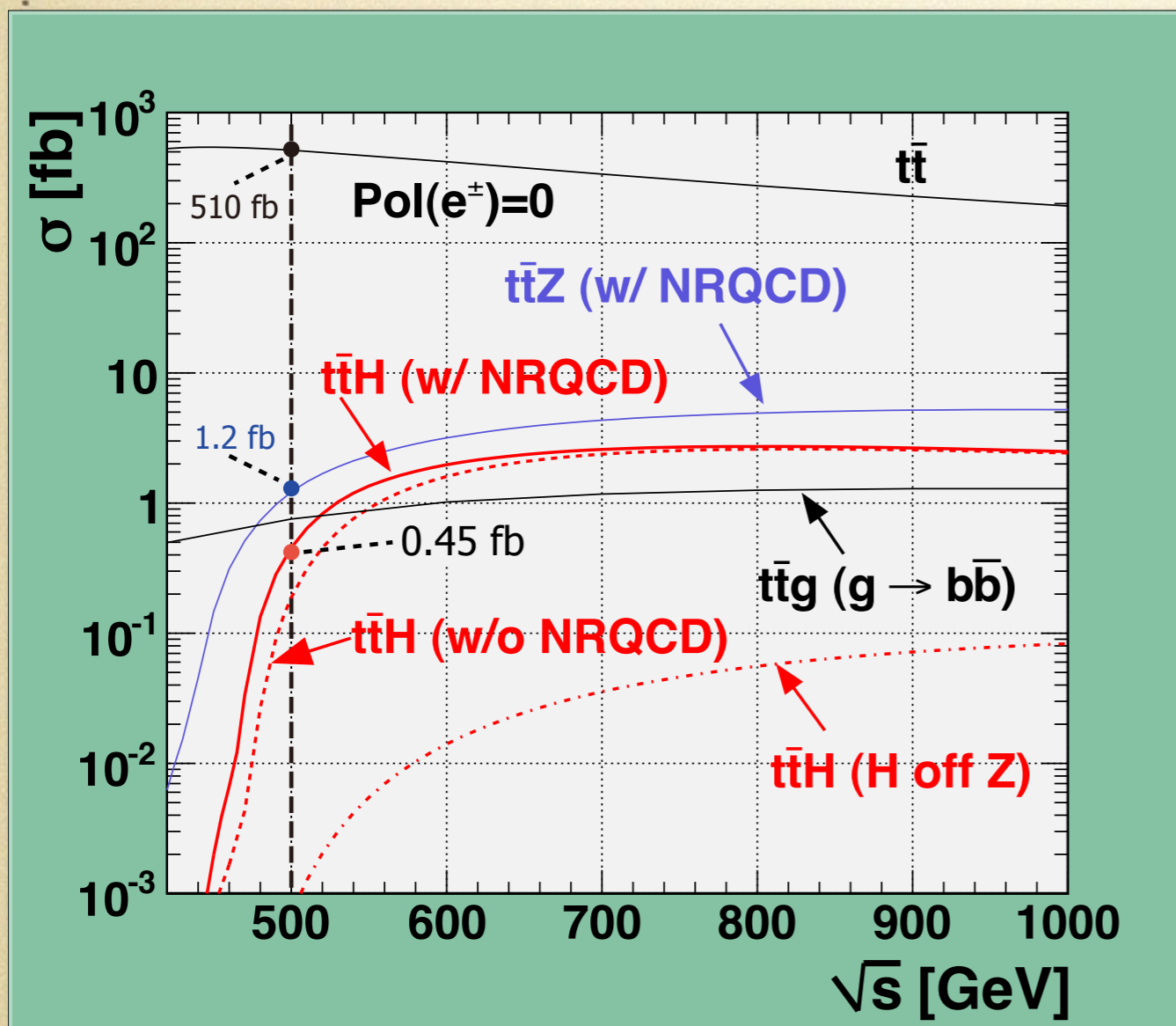
global fit --model dependent + sys + theory error (0.1%)

coupling $\Delta g / g$	baseline			luminosity upgrade		
	250 GeV	250 GeV + 500 GeV	250 GeV + 500 GeV + 1 TeV	250 GeV	250 GeV + 500 GeV	250 GeV + 500 GeV + 1 TeV
HZZ	0.74%	0.49%	0.45%	0.36%	0.27%	0.25%
HWW	4.7%	0.43%	0.27%	2.2%	0.27%	0.2%
Hbb	4.7%	0.97%	0.57%	2.2%	0.55%	0.36%
Hcc	6.4%	2.5%	1.3%	3%	1.3%	0.78%
Hgg	6.1%	2%	1.1%	2.8%	1.1%	0.69%
H $\tau\tau$	5.2%	1.9%	1.3%	2.4%	1%	0.74%
H $\gamma\gamma$	17%	8.3%	3.8%	8.1%	4.4%	2.3%
H $\mu\mu$	5.2%	1.9%	1.4%	2.4%	1%	0.89%
Htt	6.4%	2.5%	1.3%	3%	1.4%	0.87%
$\Gamma$	9%	1.7%	1.1%	4.2%	1%	0.8%
Br(Inv)	<0.95%	<0.95%	<0.95%	0.44%	0.44%	0.44%
HHH	-	83%	21%	-	46%	13%

# Top-Yukawa Coupling and Higgs

The largest among matter fermions

direct measurement!



A factor of 2 enhancement from QCD bound-state effects  
8-jets mode and lv+6jets mode combined

main BG:  $ttZ$  /  $ttg$  ( $g \rightarrow b\bar{b}$ )

Notice  $\sigma(500+20\text{GeV})/\sigma(500\text{GeV}) \sim 2$   
Moving up a little bit helps significantly!

R. Yonamine, et. al, Phys.Rev. D84 (2011)  
014033, confirmed by full simulation

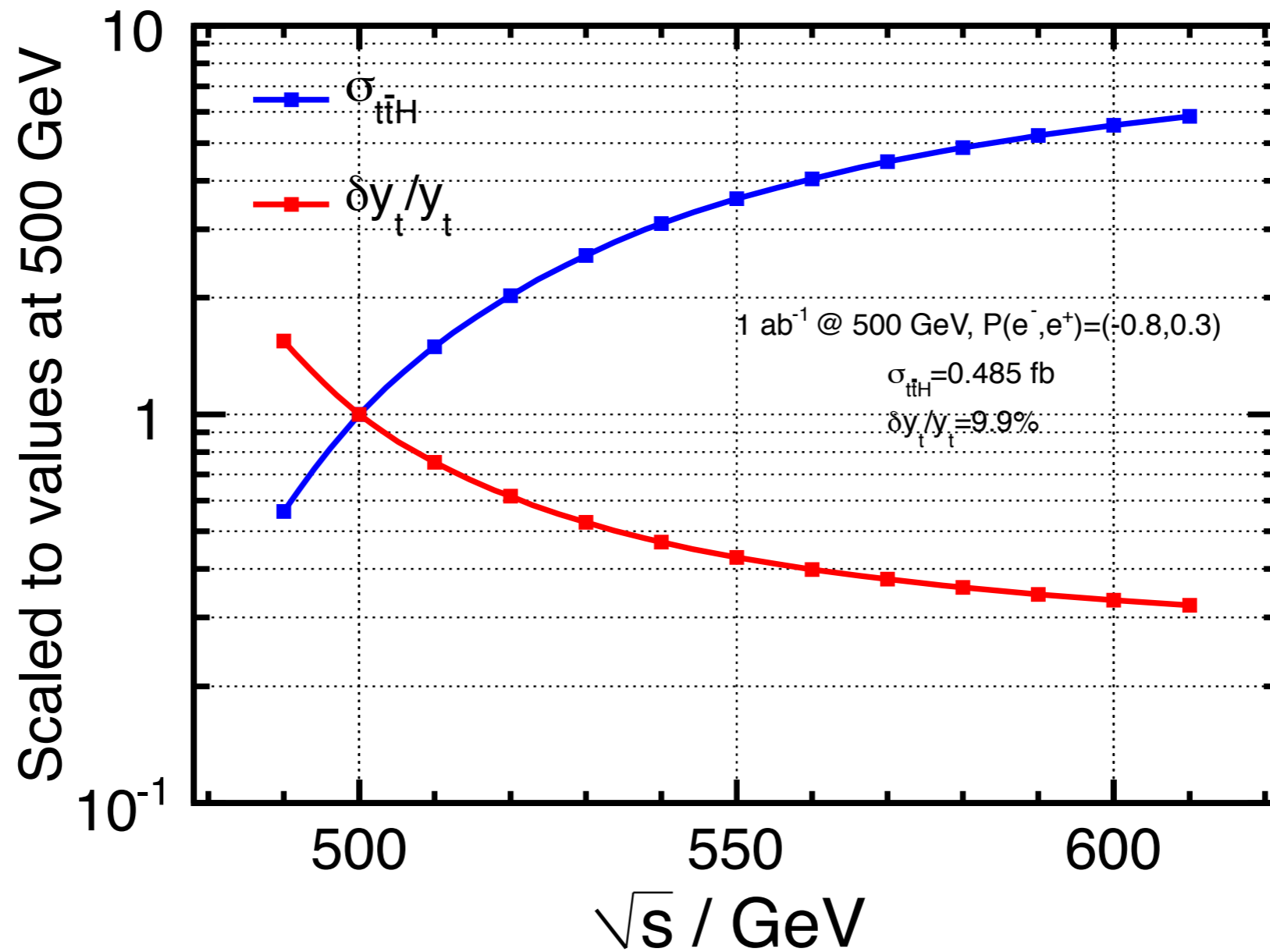
T. Tanabe, T. Price, et. al, LC-REP-2013-004

$\Delta g_{ttH} / g_{ttH}$	500 GeV	500 GeV + 1 TeV
Baseline	14%	3.2%
LumiUP	7.8%	2%

see more details in poster by J.Strube



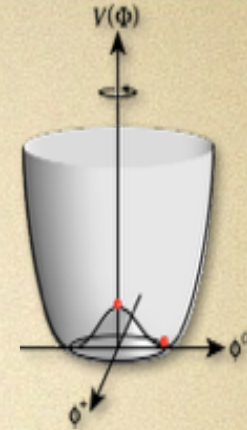
# top-Yukawa coupling



Y. Sudo

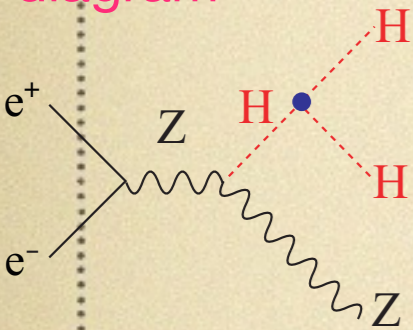
# Higgs Self-coupling

The force that makes Higgs boson condense in the vacuum

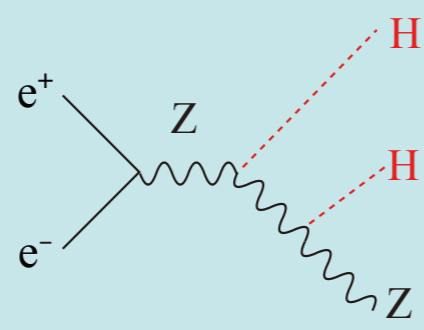


Higgs Potential: 
$$V(\eta_H) = \frac{1}{2} m_H^2 \eta_H^2 + \lambda v \eta_H^3 + \frac{1}{4} \lambda \eta_H^4$$

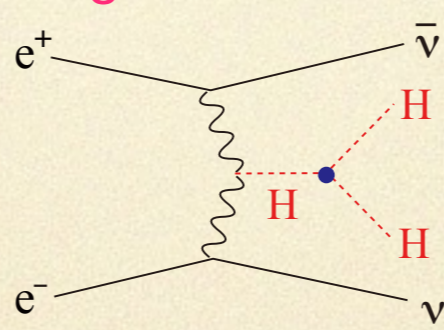
Signal diagram



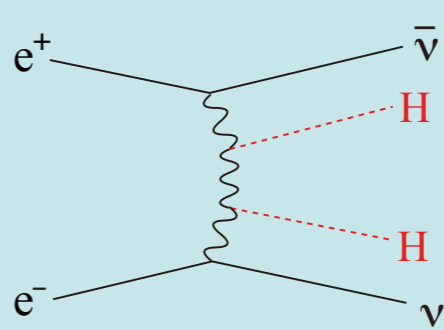
Irreducible BG diagrams



Signal diagram



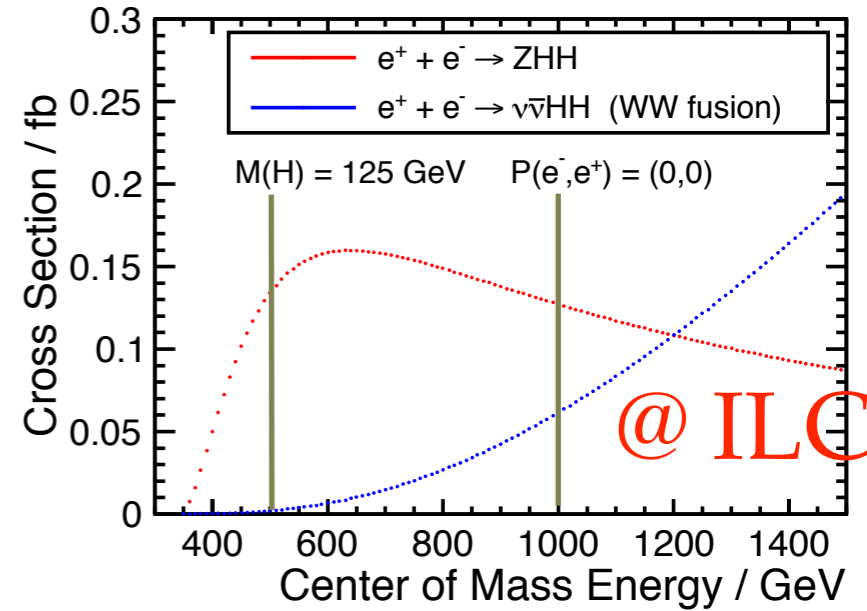
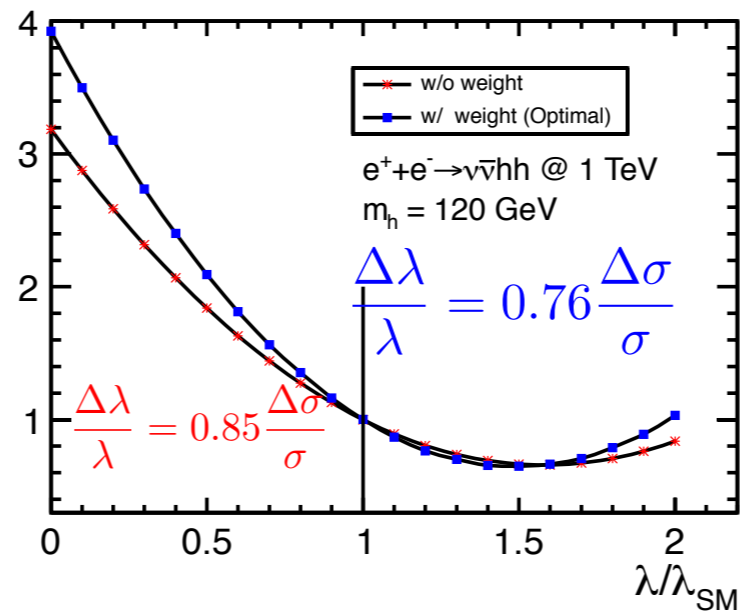
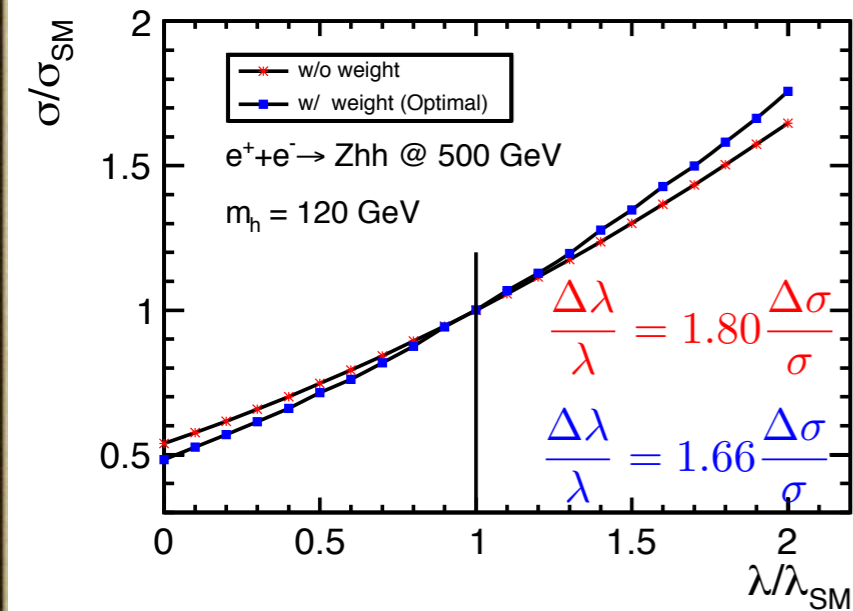
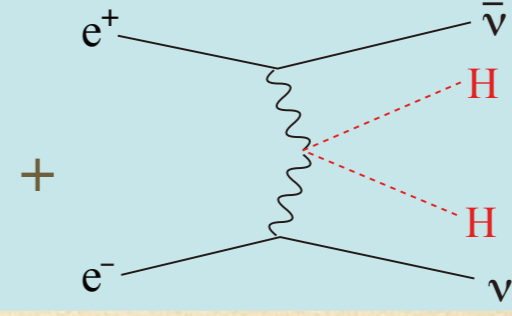
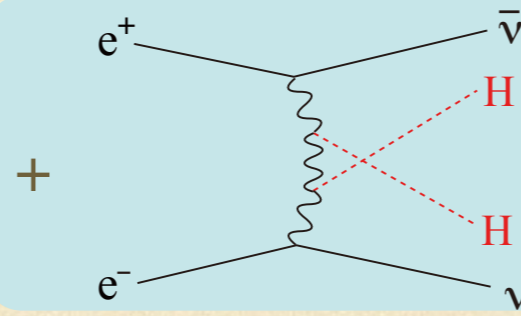
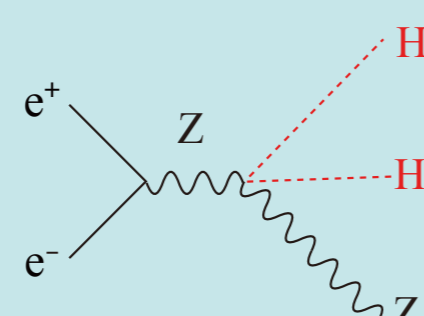
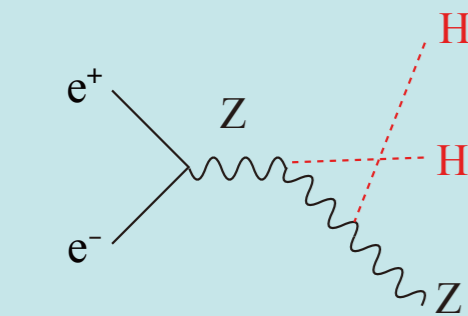
Irreducible BG diagrams



$\sigma = \lambda^2 S + \lambda I + B$

$\frac{\Delta\lambda}{\lambda} = F \cdot \frac{\Delta\sigma}{\sigma}$

**F=0.5 if no BG diagrams**



# Higgs Self-coupling Projections @ ILC

see more details in poster by J.Strube

full simulation done w/  $m_H = 120$  GeV, being updated to  $m_H = 125$  GeV

$\Delta\lambda_{HHH}/\lambda_{HHH}$	500 GeV			500 GeV + 1 TeV		
Scenario	A	B	C	A	B	C
Baseline	104%	83%	66%	26%	21%	17%
LumiUP	58%	46%	37%	16%	13%	10%

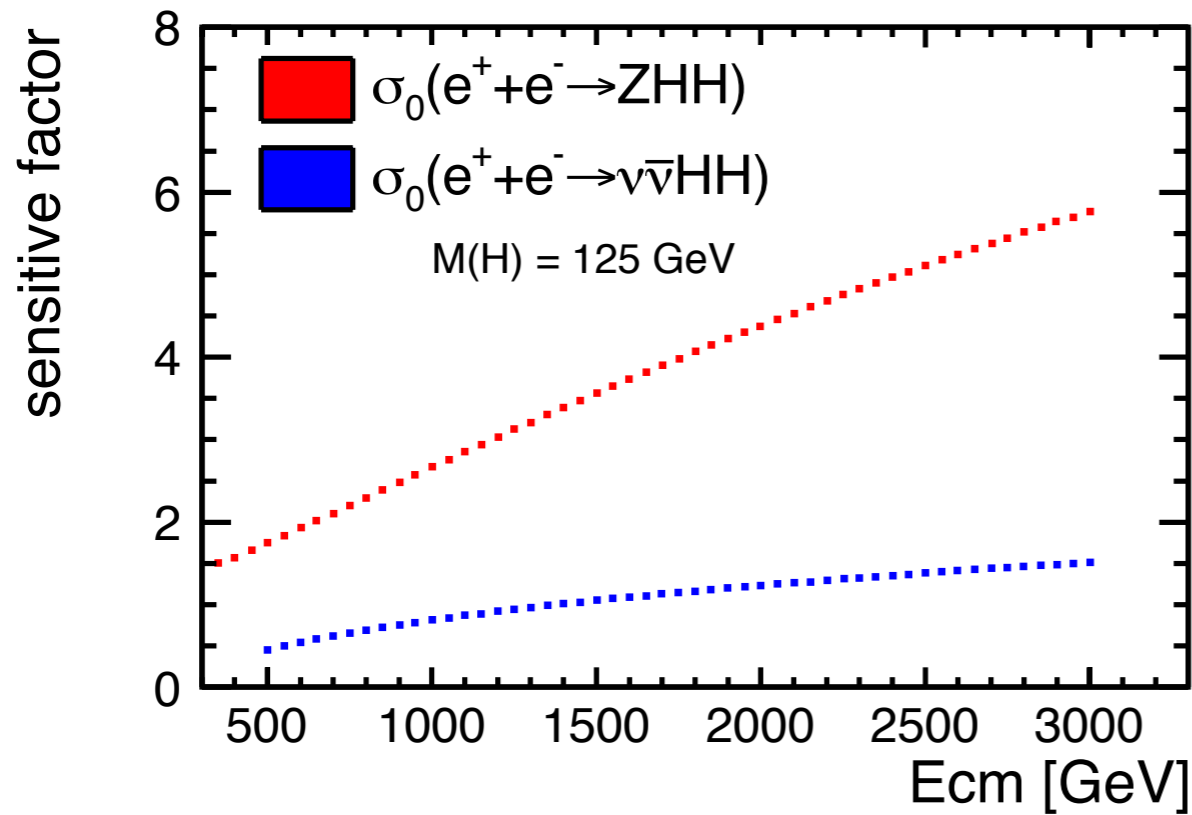
Scenario A (done): HH-->bbbb, full simulation done

Scenario B (done): adding HH-->bbWW\*, full simulation done, ~20% relative improvement

Scenario C (ongoing): color-singlet clustering, matrix element method, kinematic fitting, flavor tagging, expected ~20% relative improvement (conservative)

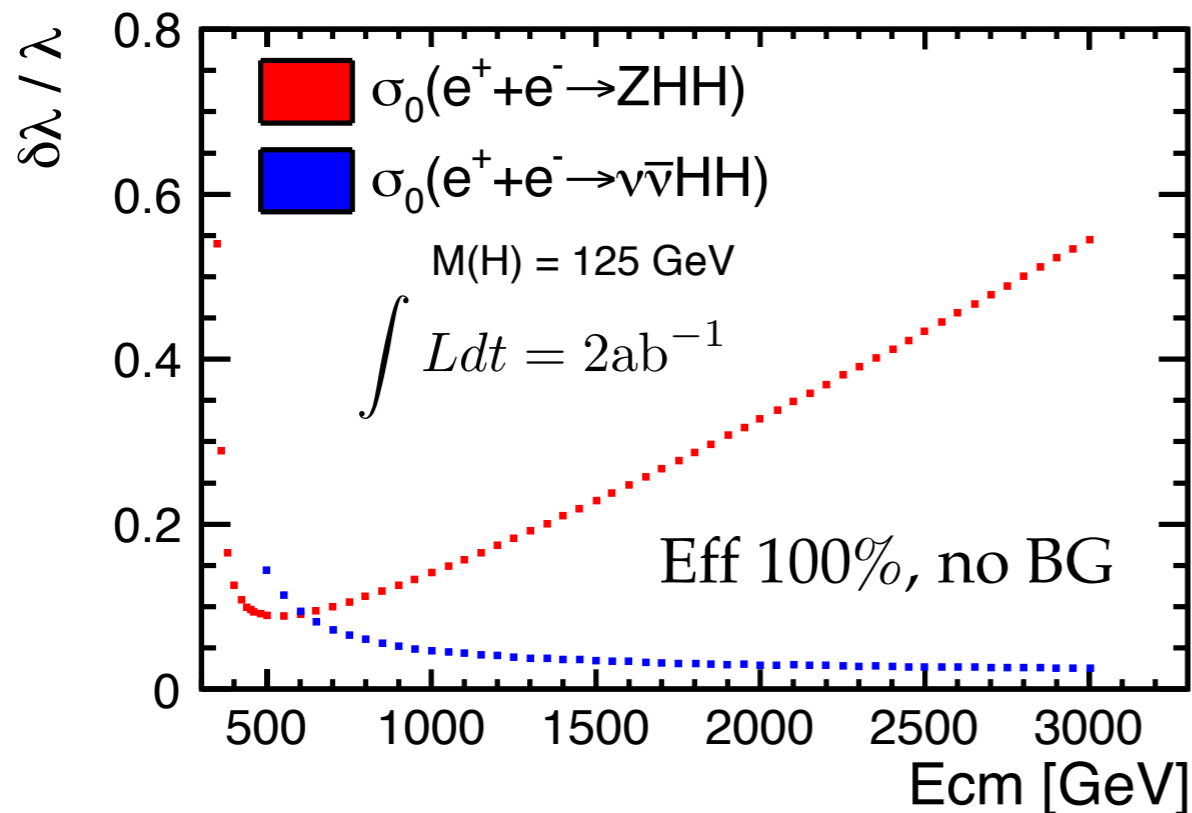
if positron polarisation 30%(20%) --> 60%(40%), gain relatively 10% improvement

# General issue: running of the sensitive factor and expected coupling precision at different Ecm



$$\frac{\Delta\lambda}{\lambda} = F \cdot \frac{\Delta\sigma}{\sigma}$$

Factor increases quickly as going to higher energy

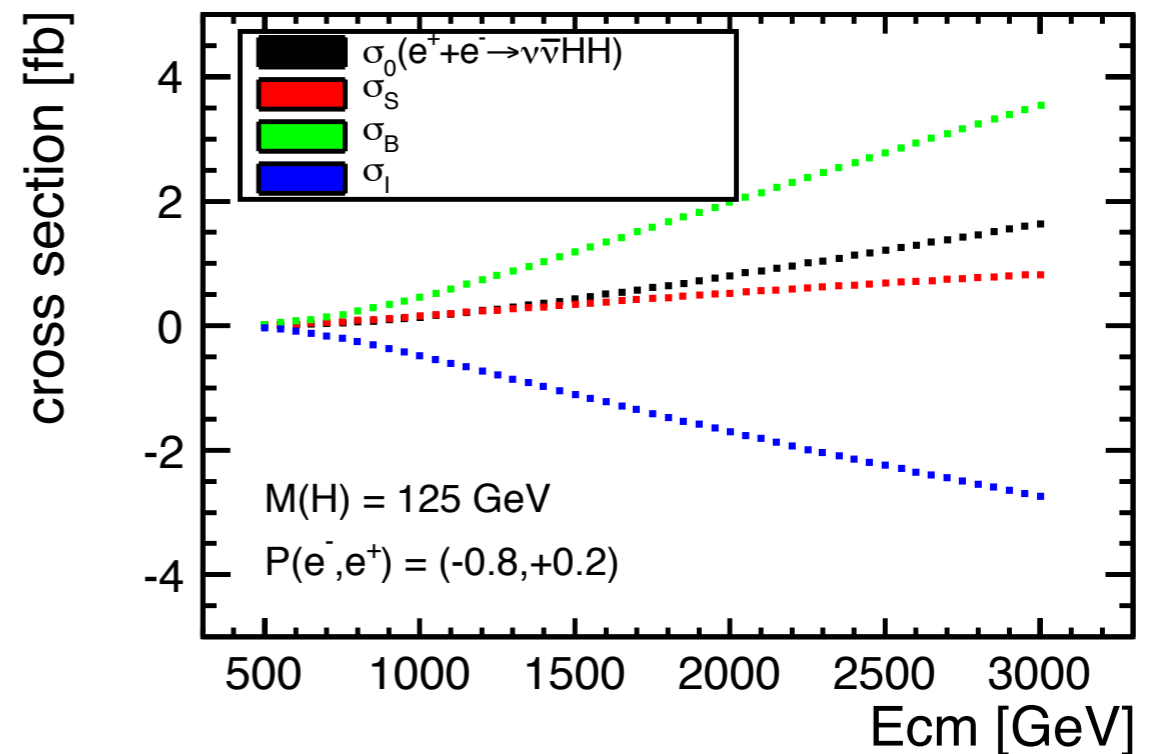
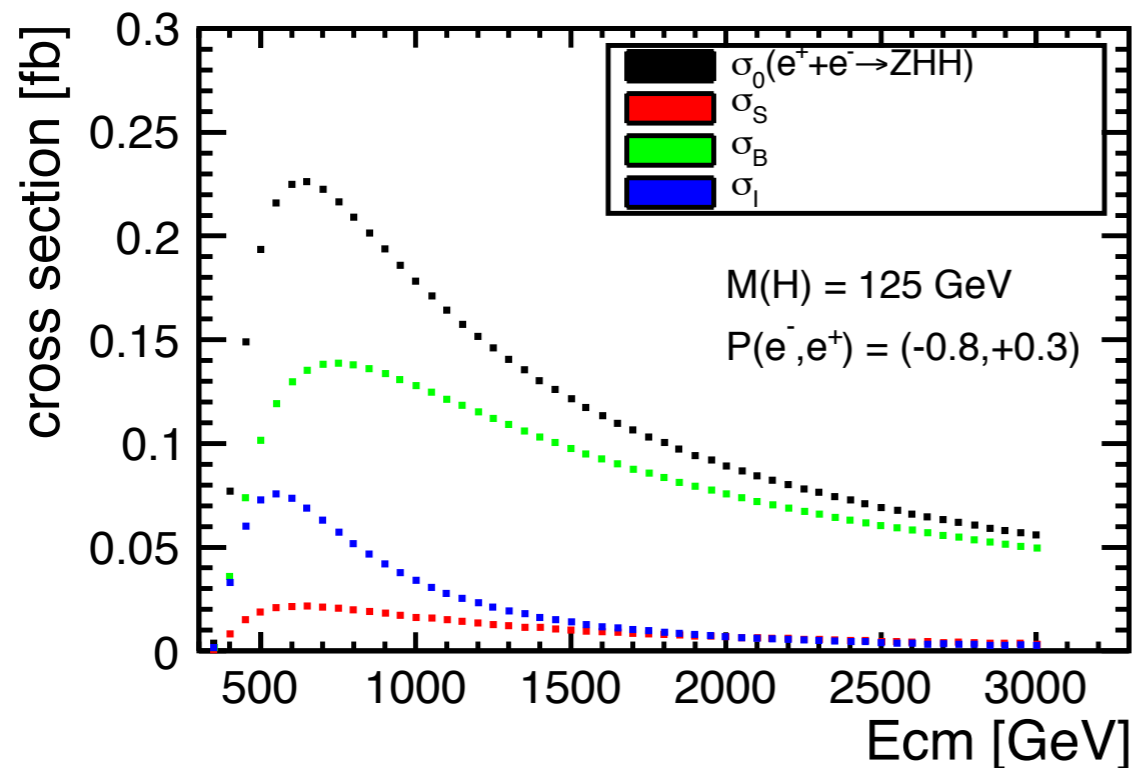


for ZHH, the expected optimal energy  $\sim 500 \text{ GeV}$  (though cross section is maximum  $\sim 600 \text{ GeV}$ )

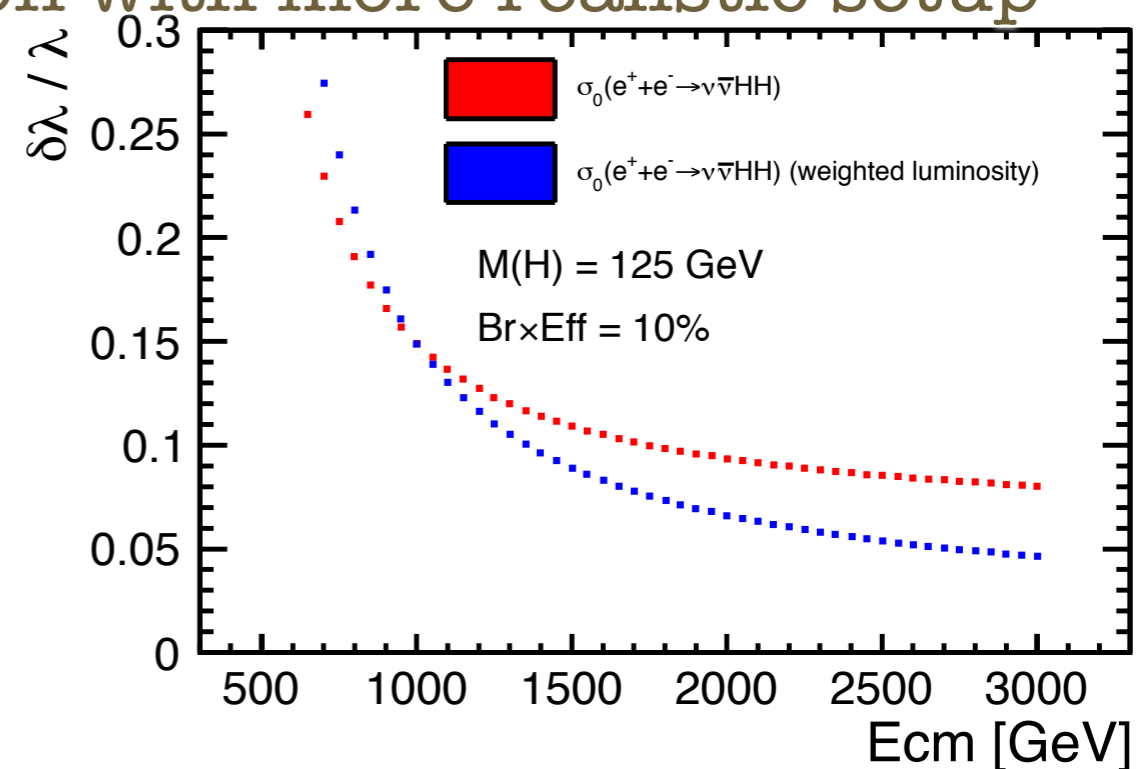
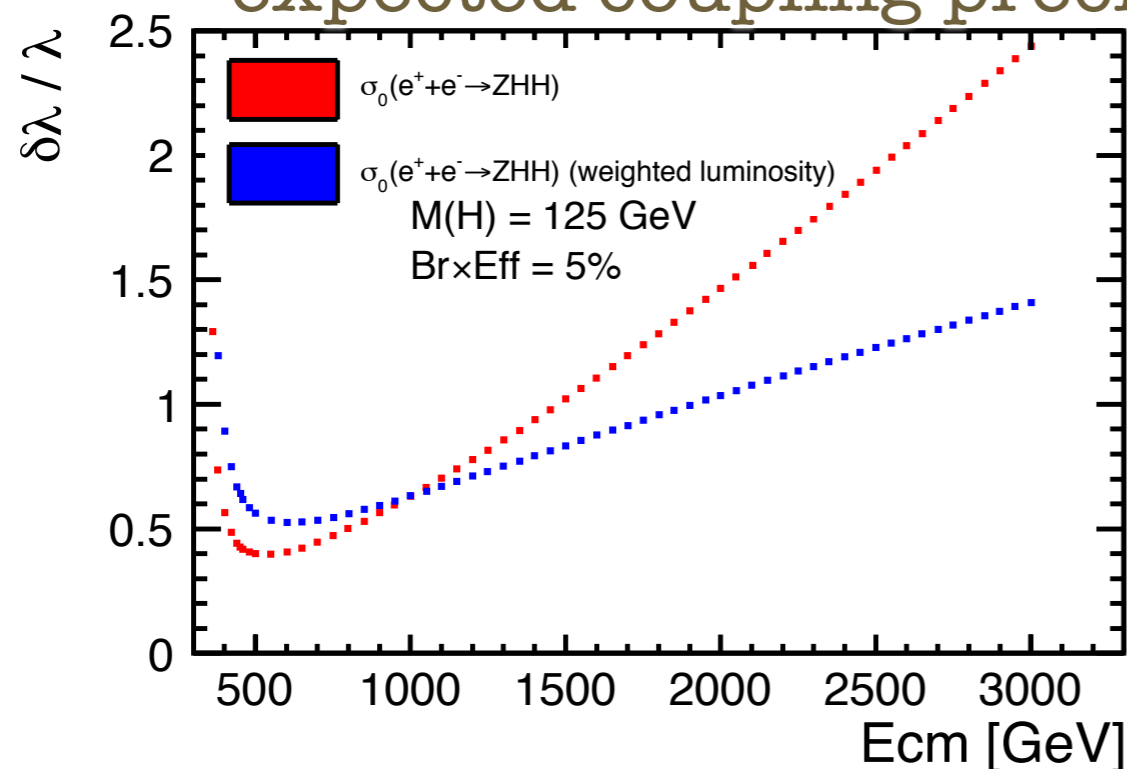
for  $\nu\nu HH$ , expected precision improves slowly as going to higher energy

# General issue: cross sections of each contribution

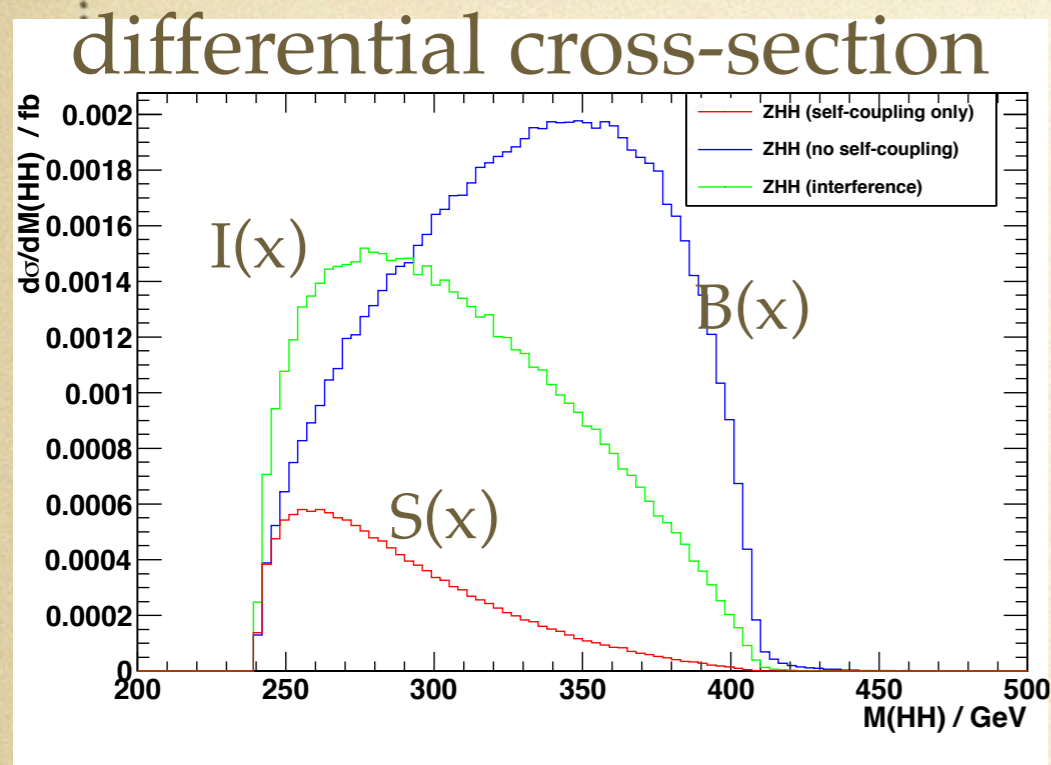
$$\sigma_0 = a\lambda^2 + b\lambda + c = \sigma_S + \sigma_I + \sigma_B$$



## expected coupling precision with more realistic setup



new weighting method to enhance the coupling sensitivity

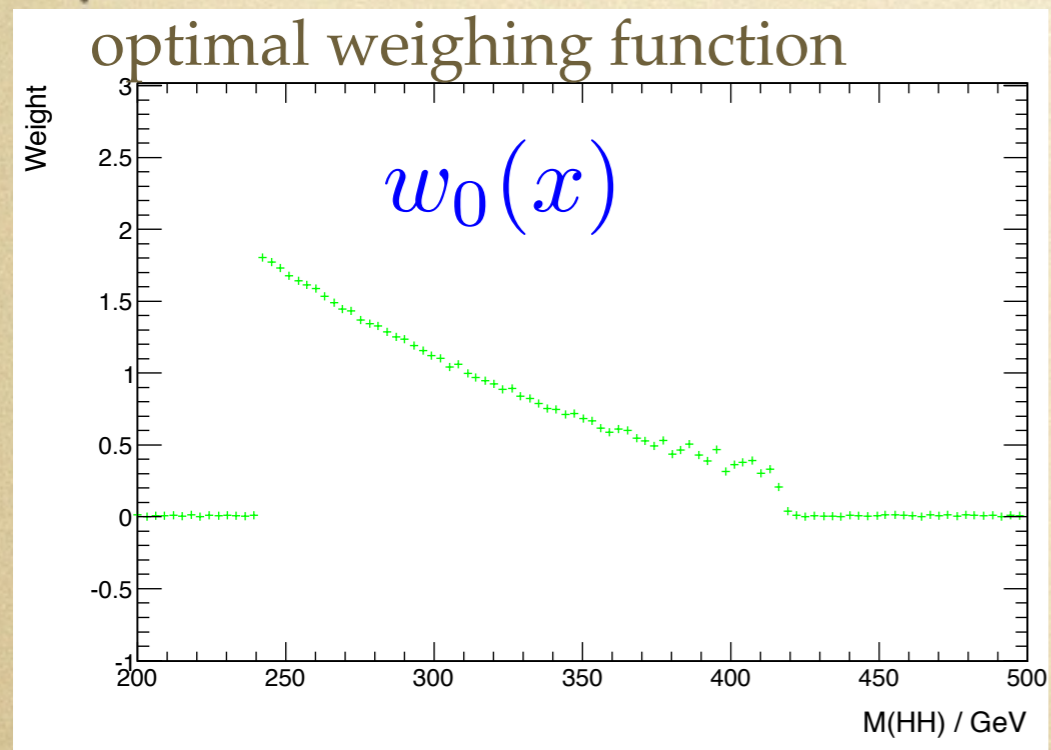


$$\frac{d\sigma}{dx} = B(x) + \lambda I(x) + \lambda^2 S(x)$$

irreducible
interference
self-coupling

observable: weighted cross-section

$$\sigma_w = \int \frac{d\sigma}{dx} w(x) dx$$



equation of the optimal  $w(x)$  (variance principle):

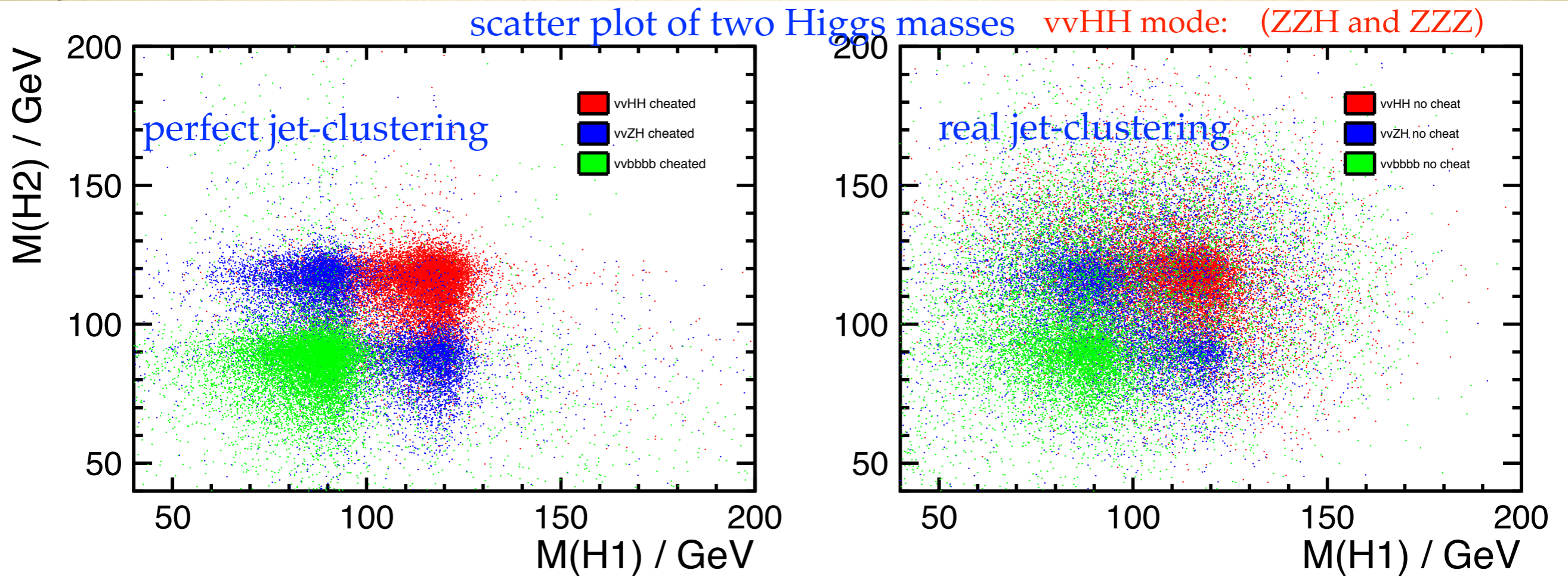
$$\sigma(x)w_0(x) \int (I(x) + 2S(x))w_0(x)dx = (I(x) + 2S(x)) \int \sigma(x)w_0^2(x)dx$$

general solution:

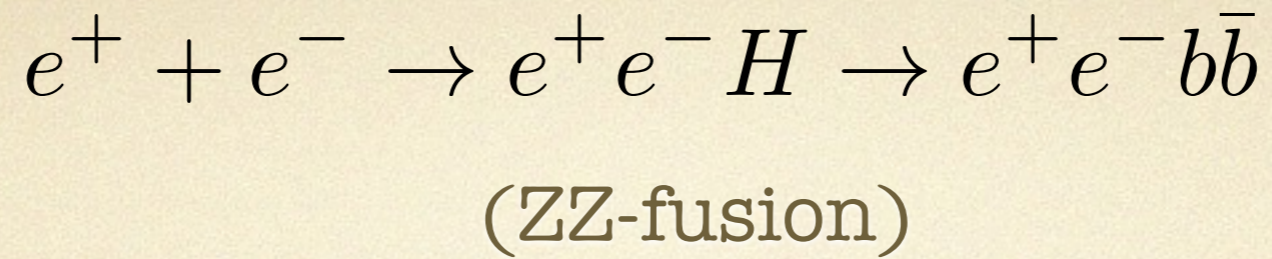
$$w_0(x) = c \cdot \frac{I(x) + 2S(x)}{\sigma(x)}$$

$c$ : arbitrary normalization factor

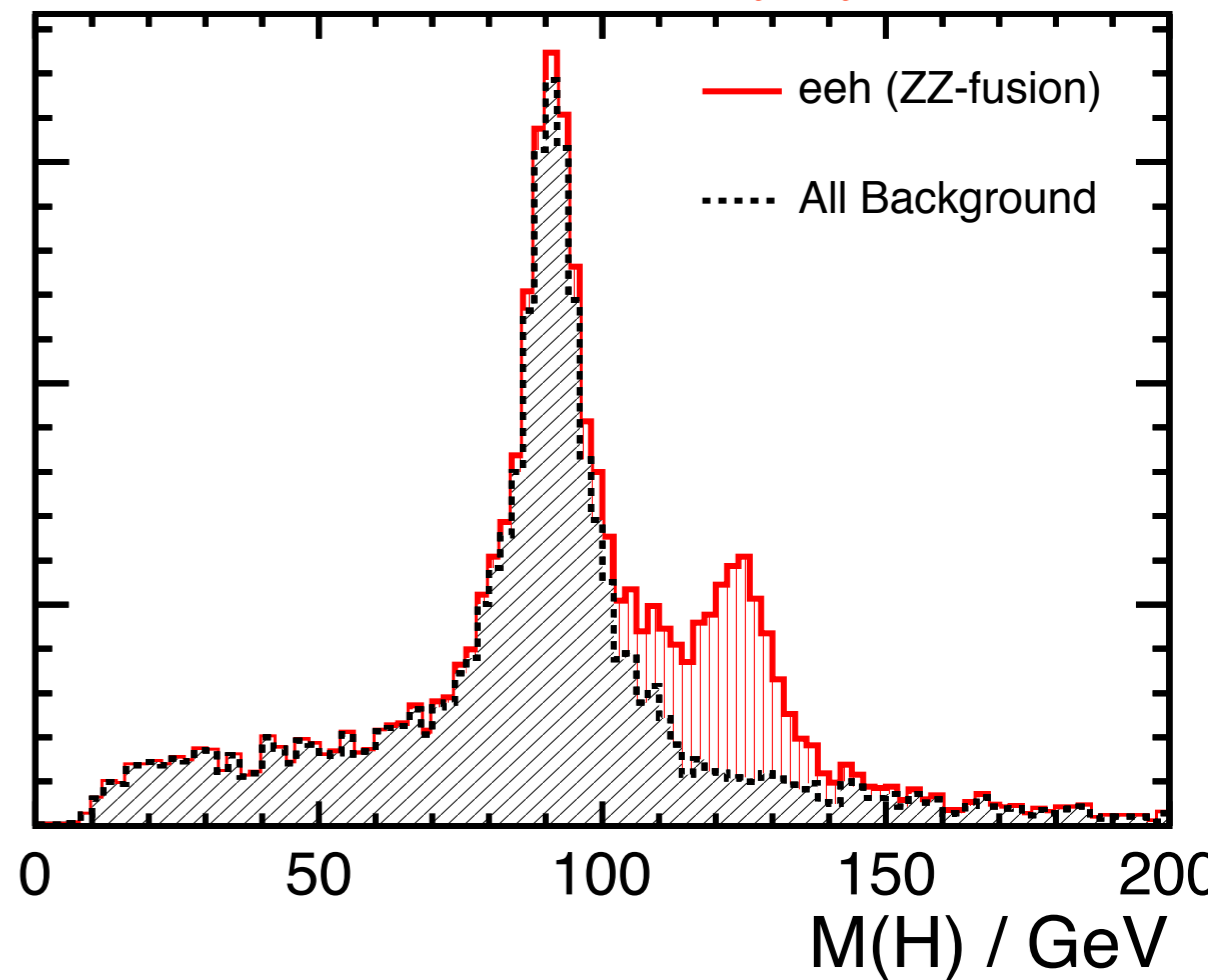
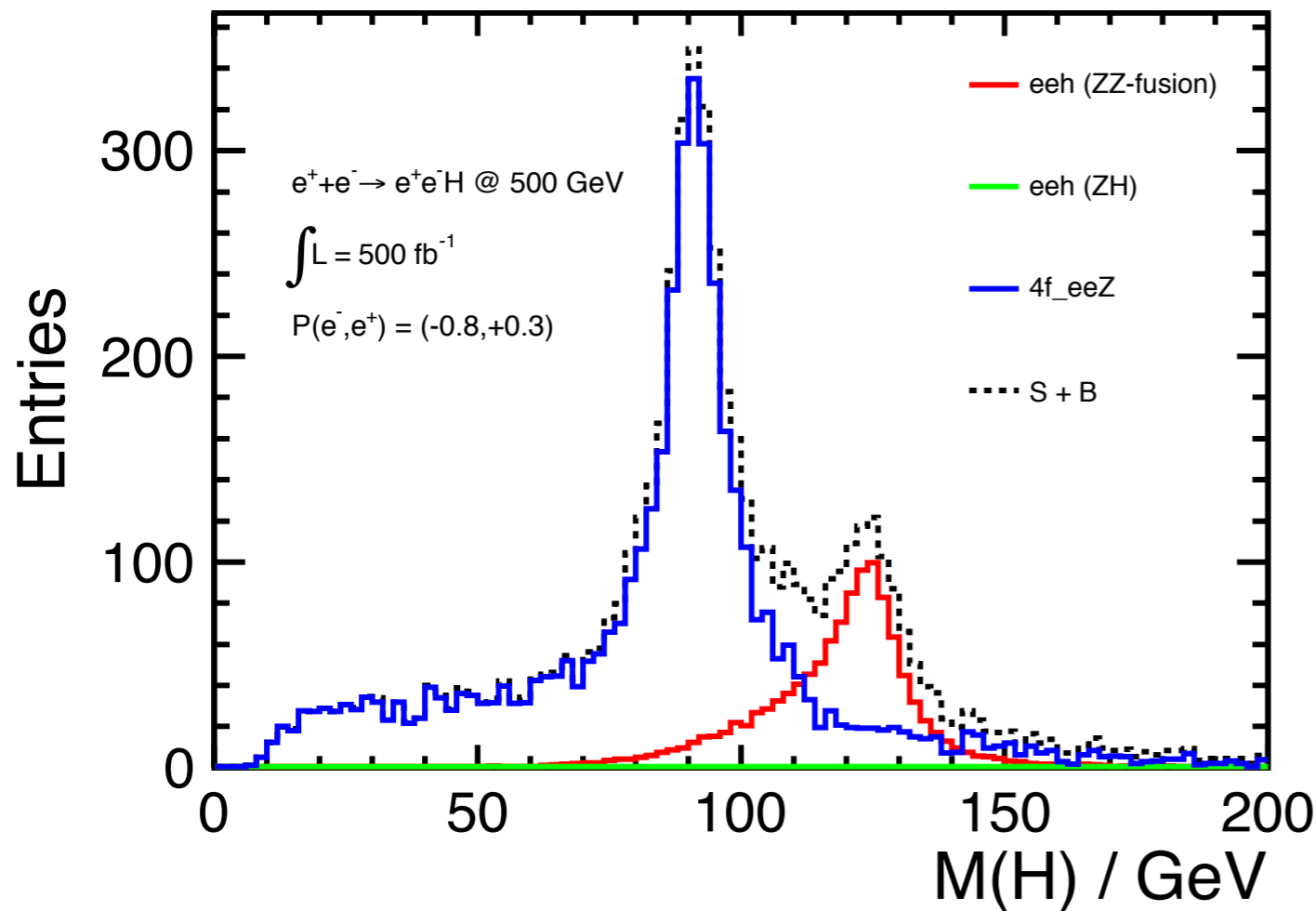
# prospect of Higgs self-coupling



- ♦ the mis-clustering of particles degrades the mass resolution very much
- ♦ it is studied using perfect color-singlet jet-clustering can improve  $\delta\lambda/\lambda$  by 40%
- ♦ Mini-jet based clustering (Durham works when  $N_p$  in mini-jet  $\sim 5$ , need better algorithm to combine the mini-jets, using such as color-singlet dynamics)
- ♦ looks very challenging now...
- ♦ including  $H \rightarrow WW^*$  (ongoing)
- ♦ kinematic fitting, matrix element method



excess from BG (discovery by ZZ-fusion)



$$\frac{\delta(\sigma_{eeH} \cdot \text{Br}(H \rightarrow b\bar{b}))}{\sigma \cdot \text{Br}} = 3.9\% \quad (2.2\%)$$

(LumiUP)