

# Higgs Physics

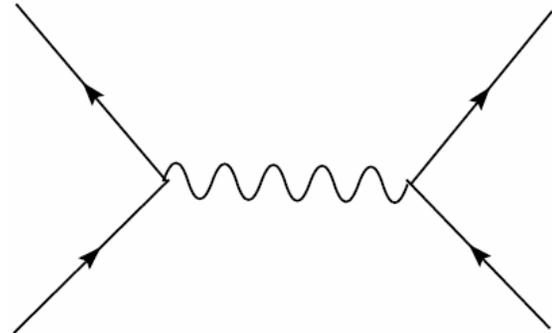
Yasuhiro Okada (KEK)

November 26, 2004, at KEK

# Higgs mechanism

- One of two principles of the Standard Model.  
“Gauge invariance” and “Higgs mechanism”
- Origin of the weak scale.  
“Why is the weak interaction so weak?”

$$G_F = \frac{1}{\sqrt{2}v^2}$$



# Goals of Higgs physics

- Find Higgs bosons and establish the mass generation mechanism of quarks, leptons and the gauge bosons.

## Coupling constant measurements

- Clarify physics behind the electroweak symmetry breaking.

“What is the Higgs particle?”

Elementary or composite?

A window to the physics beyond the Standard Model.

# Higgs boson mass

- Higgs mass -> Strength of the dynamics responsible for the electroweak symmetry breaking.
- In the SM,

$$m_h = \sqrt{2\lambda}v \quad V = -\mu^2|\phi|^2 + \lambda|\phi|^4$$

- In general,  
a light Higgs boson is consistent with  
weakly interacting scenario  
(GUT/SUSY/String unification ?),  
a heavy Higgs boson implies  
strongly interacting scenario.

# Theoretical bounds on the Higgs boson

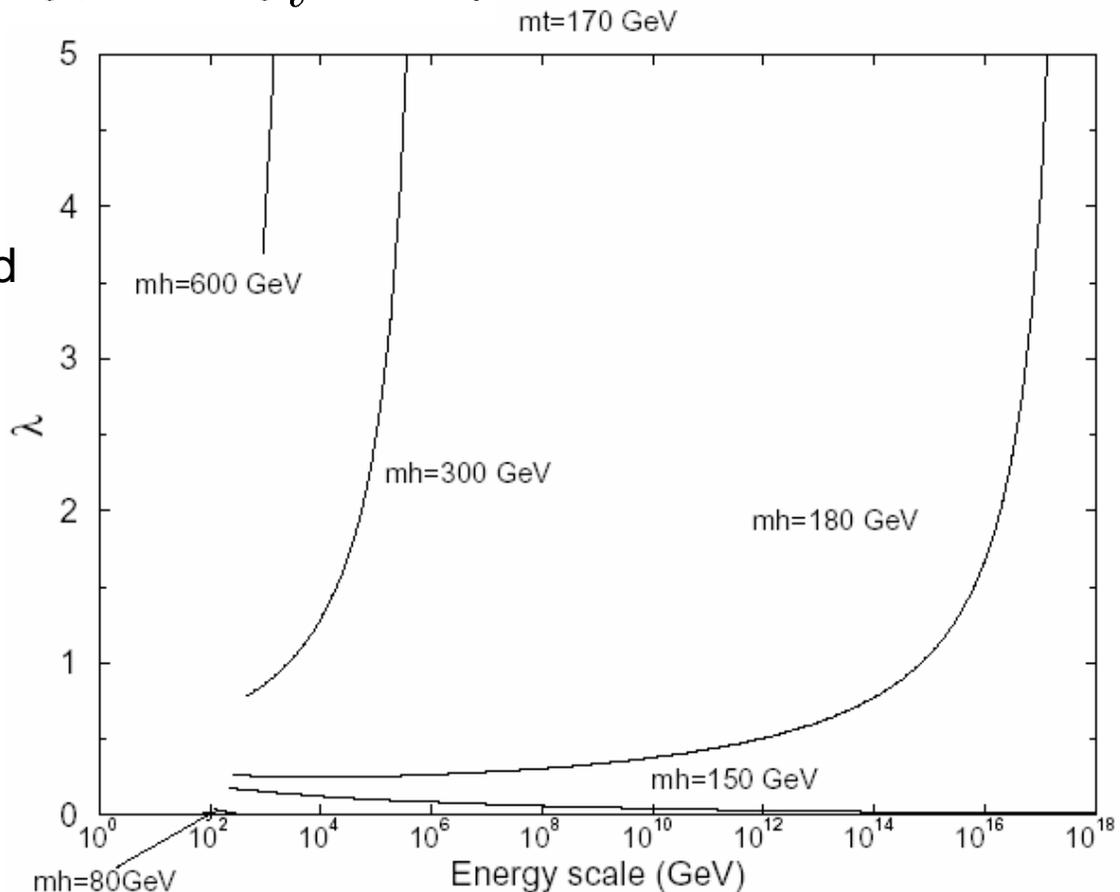
## mass in the SM

RGE for the Higgs self-coupling constant in the SM

$$\mu \frac{d}{d\mu} \lambda = \frac{1}{16\pi^2} (24\lambda^2 + 12y_t\lambda - 6y_t^2 + \dots)$$

If we require that the SM is valid up to  $10^{19}$  GeV,

$$130 \text{ GeV} \leq m_h \leq 180 \text{ GeV}$$



# Higgs mass in SUSY models

- SUSY models include at least two Higgs doublets.
- In the minimal SUSY Standard Model (MSSM), the lightest CP-even Higgs boson mass has theoretical upper bound.

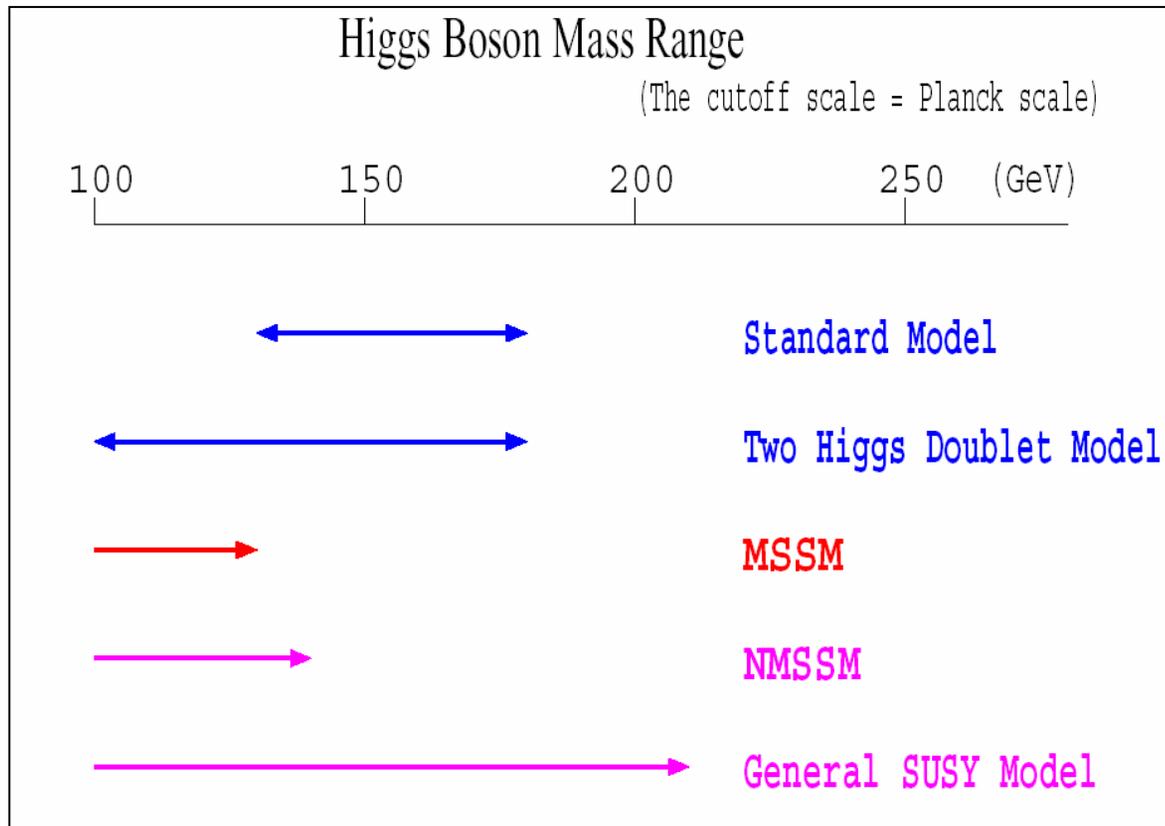
$$V_{Higgs} = m_1^2 |H_1|^2 + m_2^2 |H_2|^2 - m_3^2 (H_1 \cdot H_2 + \bar{H}_1 \cdot \bar{H}_2) \\ + \frac{g_2^2}{8} (\bar{H}_1 \tau^a H_1 + \bar{H}_2 \tau^a H_2)^2 + \frac{g_1^2}{8} (|H_1|^2 - |H_2|^2)^2 \\ + \Delta V.$$

$$m_h^2 \leq m_Z^2 \cos^2 2\beta + \frac{6}{(2\pi)^2} \frac{m_t^4}{v^2} \ln \frac{m_{stop}^2}{m_t^2}, \quad (\tan \beta = \frac{\langle H_2^0 \rangle}{\langle H_1^0 \rangle})$$

$$m_h < 135 \text{ GeV}$$

Possible vacuum instability is saved by supersymmetry.

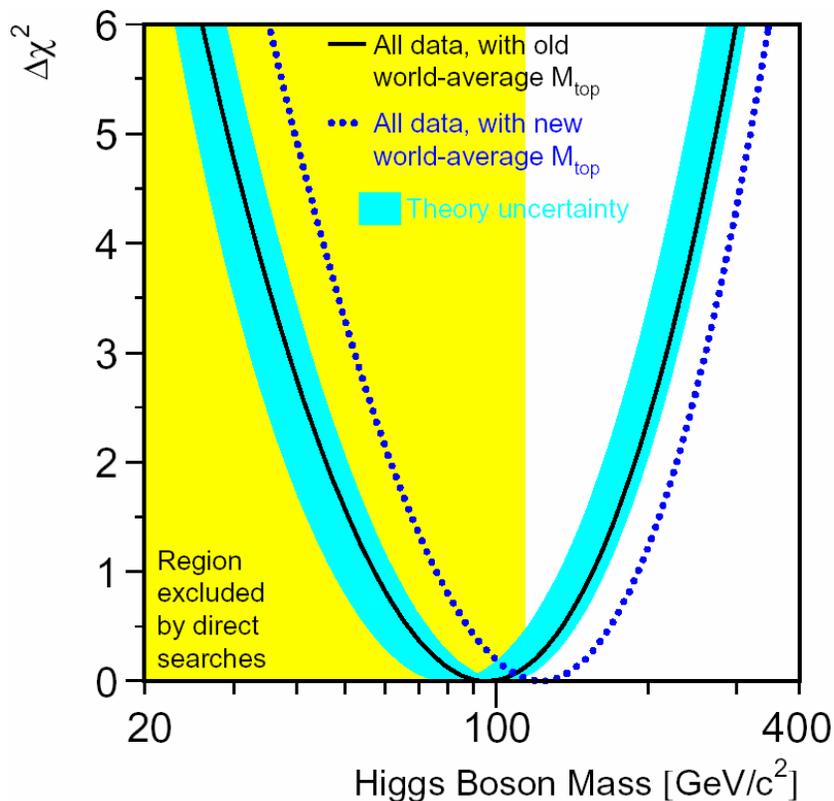
# Possible range of the lightest Higgs boson mass for the Planck scale cutoff



As long as theory behaves weakly-coupled up to the Planck scale, the Higgs boson mass is less than  $\sim 200$  GeV.

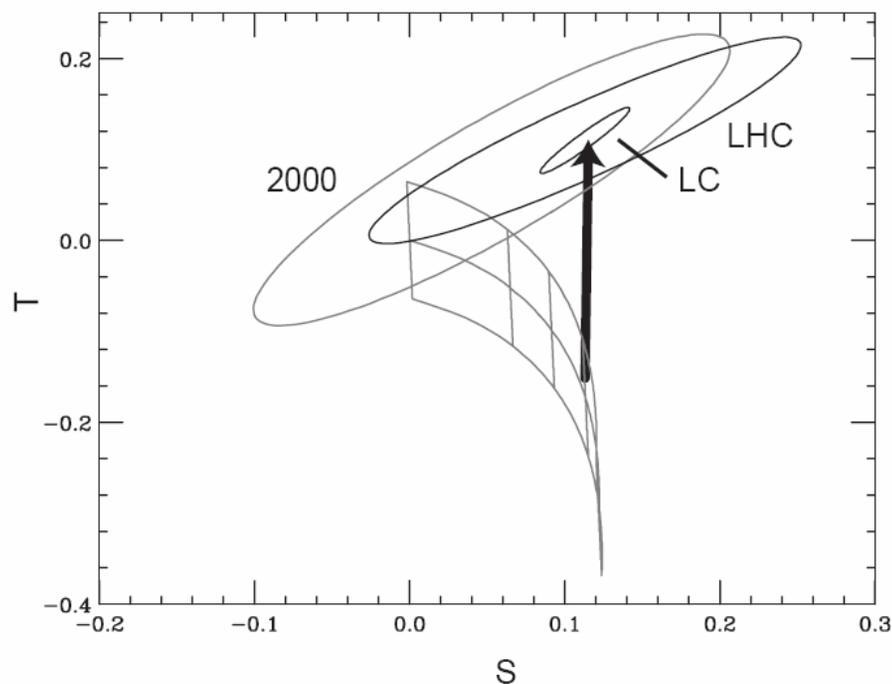
# Precision EW test and the Higgs Mass

In the SM, the global fit suggests a light Higgs boson.



$$m_h < 251 \text{ GeV (95\%CL)}$$

M.Peskin and J.Wells



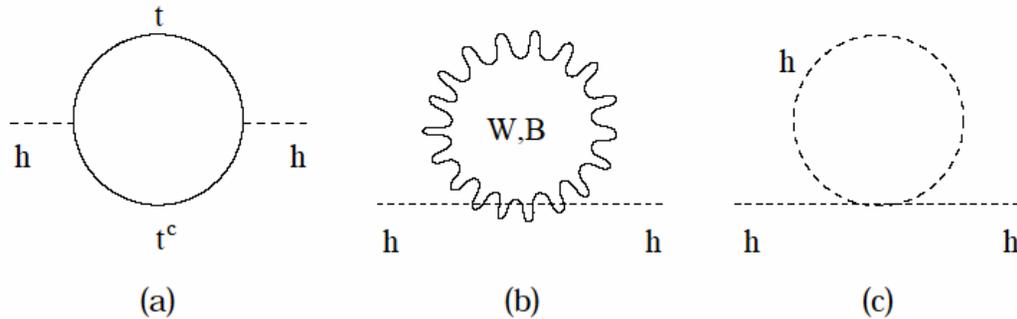
$$m_t = 174.3 \pm 5.1 \text{ GeV}$$

$$m_h = 100, 200, 300, 500, 1000 \text{ GeV}$$

Additional new physics is needed to accommodate a heavy Higgs boson.

# Hierarchy problem

- If the cutoff scale is very high, fine tuning of the Higgs boson mass is serious problem.

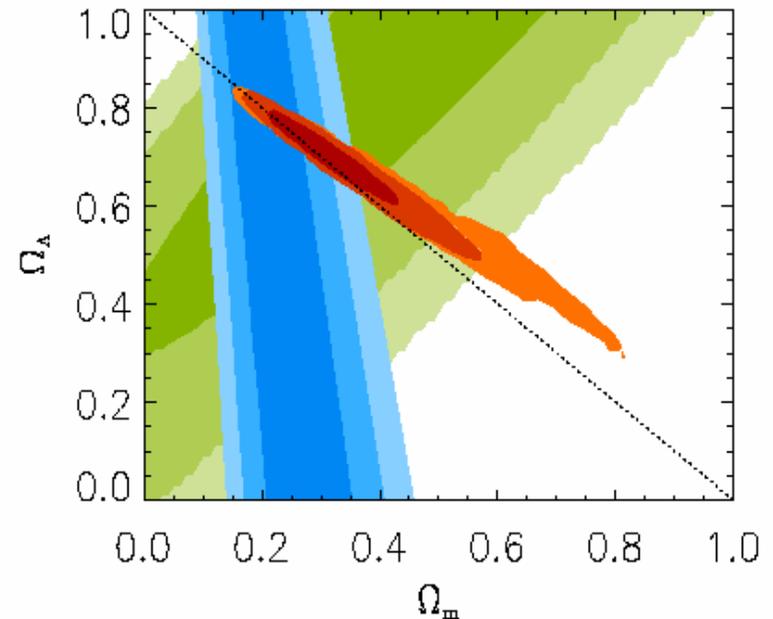
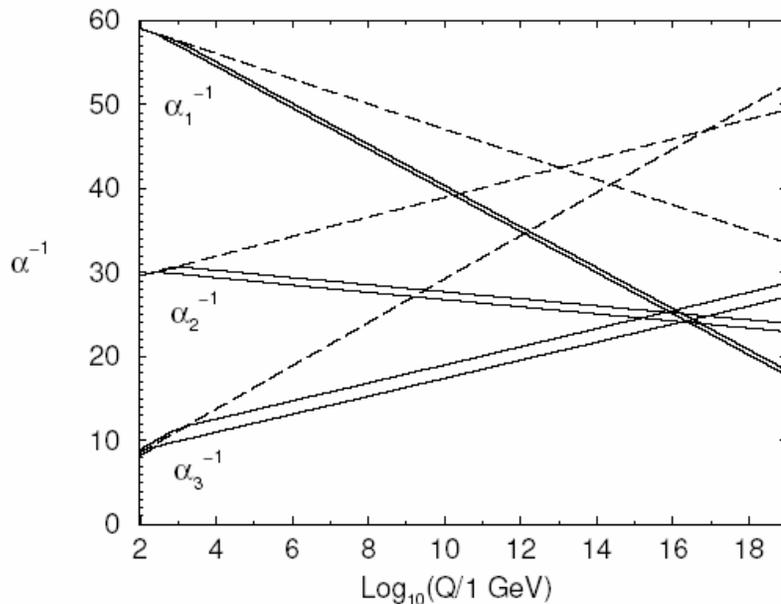


$$m_{phys}^2 = m_0^2 + g^2 \Lambda_{cutoff}^2$$

We need to find a reason to keep the Higgs boson mass light.

# Supersymmetry

- Extend relativity.
- Introduce SUSY partners
- No quadratic divergence in scalar mass renormalization in SUSY theory.
- Justification of elementary scalar fields up to the Planck scale.
- Gauge coupling unification, dark matter candidate.



# Compositeness

- The Higgs boson is a composite state of some strong interaction.
- This scenario is usually severely constrained by the precision EW measurements.
- New ideas are proposed.
  - Deconstruction, Little Higgs model, Higgsless model, etc.

- Deconstruction.

Gauge theory with a discretized fifth dimension.

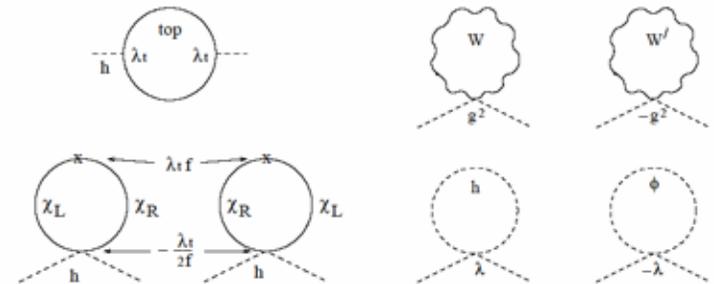
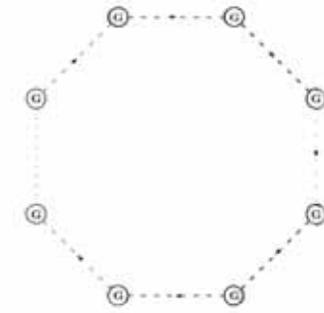
- Little Higgs model.

Higgs as a pseudo NG boson.

No quadratic divergence at one-loop.

- Higgsless Model .

5dim model without a Higgs boson. Unitarity is saved by KK modes of gauge bosons



$W_L W_L$  scattering amplitude in the SM

$$i\mathcal{M}(W_L^a W_L^b \rightarrow W_L^c W_L^d) = \text{[t-channel diagram]} + \text{[W boson exchange diagram]} + \text{[Higgs exchange diagram]} + \text{crossed.}$$

Common feature

New states at  $\sim 1\text{TeV}$

Cutoff scale  $> 10\text{ TeV}$

Severe constraints from EW precision tests

# Summary 1

- Higgs physics : Understanding the weak scale.
- What is the Higgs particle?  
Elementary ( like gravity ) or composite (like pion)?  
Very important implications for particle physics and cosmology.
- How is the hierarchy problem solved?  
SUSY?
- Higgs physics is a central issue in and beyond the SM.

# Phenomenology of Higgs bosons

- In order to establish the mass generation mechanism of elementary particles, various Higgs boson couplings have to be determined.
- A Higgs boson will be discovered at LHC, but we need ILC to establish the Higgs mechanism.

Higgs potential in the SM

$$V = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$

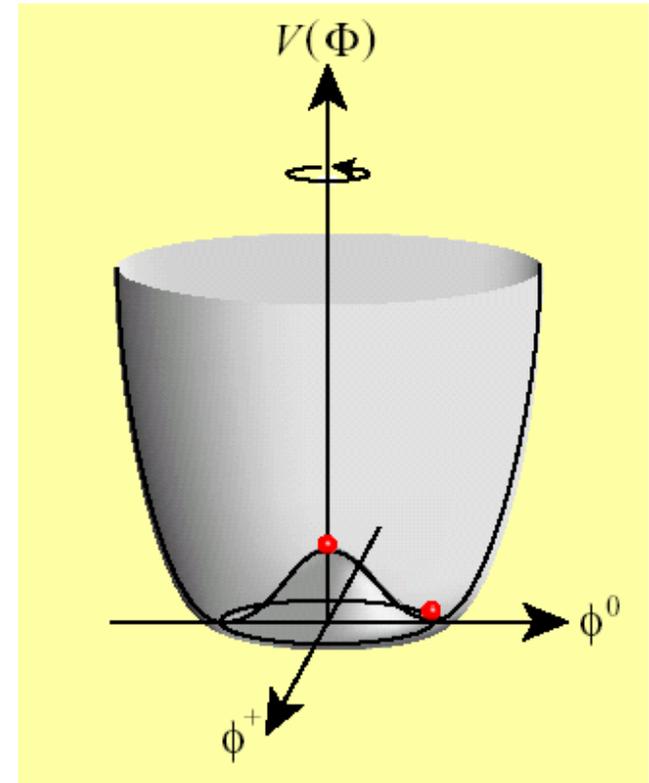
Mass formulas of elementary particles in the SM

Higgs particle  $m_h = \sqrt{2\lambda}v$

Top quark  $m_t = \frac{y_t}{\sqrt{2}}v$

W boson  $m_W = \frac{g_2}{2}v$

Z boson  $m_Z = \frac{\sqrt{g_1^2 + g_2^2}}{2}v$



VEV of the Higgs field

$$\langle \phi^0 \rangle = v/\sqrt{2}$$

# Higgs search at LHC

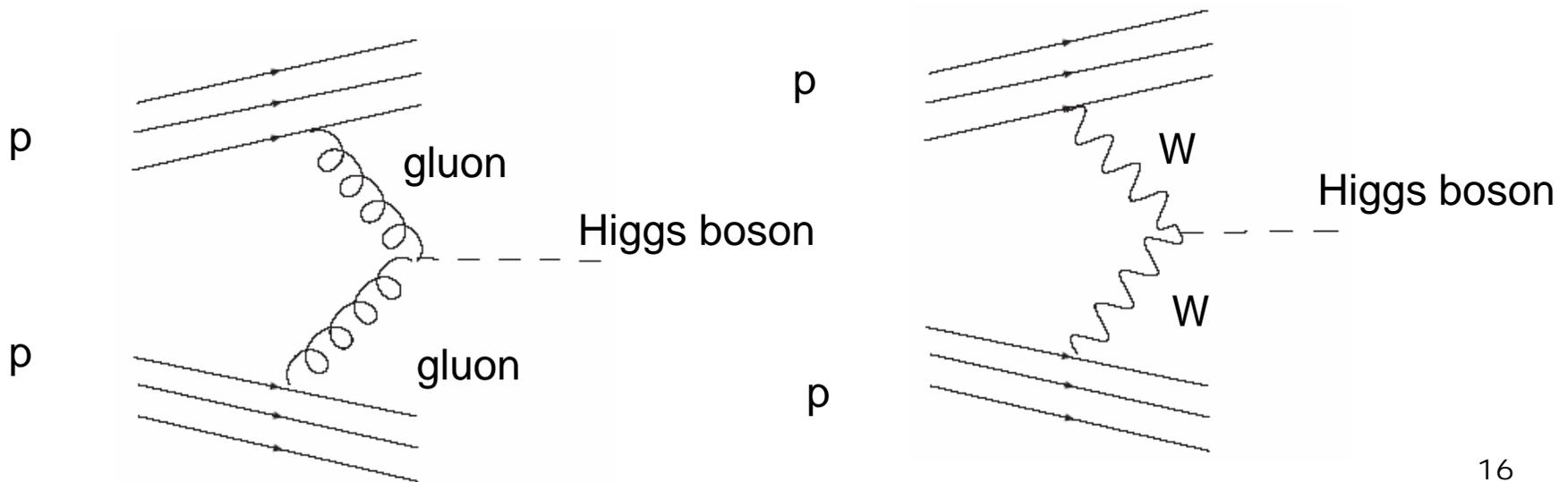
LHC: 2007 14 TeV pp collider

Discovery of the Higgs boson is a main target.

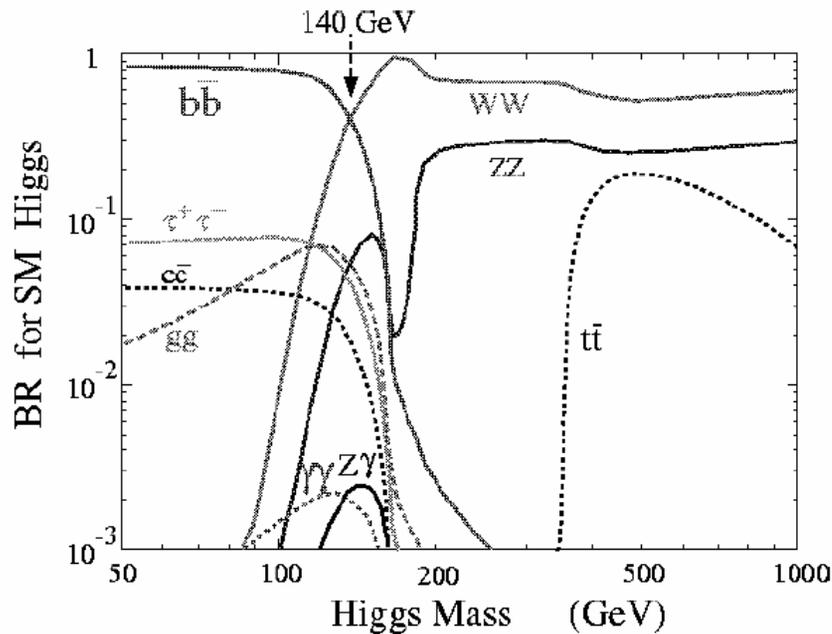
Higgs boson search depends on the Higgs boson mass

Production: gluon fusion, WW fusion

Decay: decay to heavier particles if kinematically allowed.

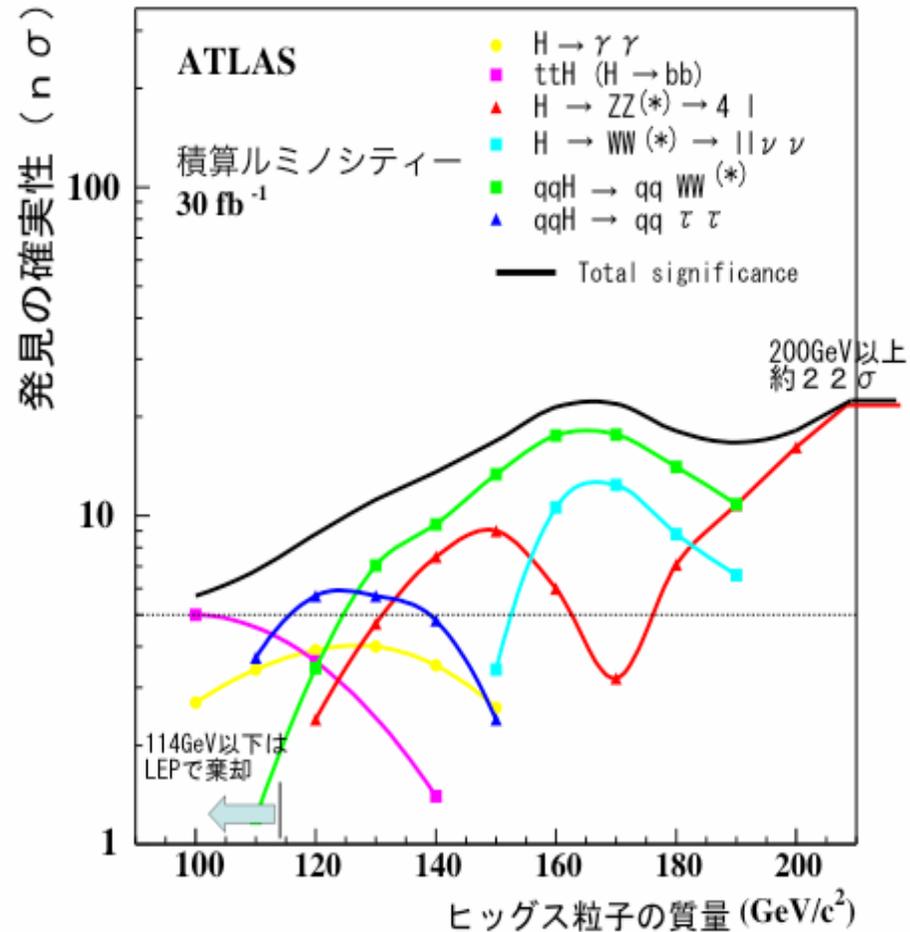


## SM Higgs boson decay branching ratios



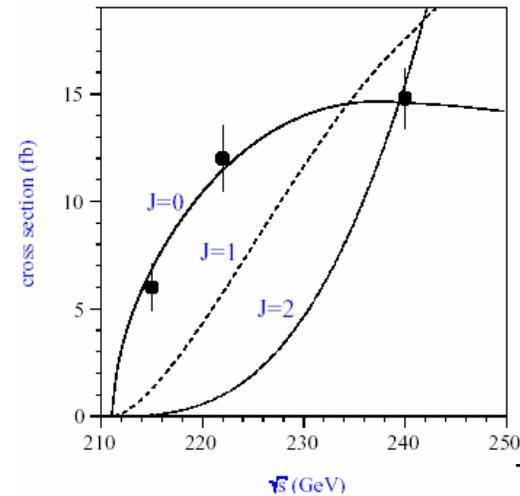
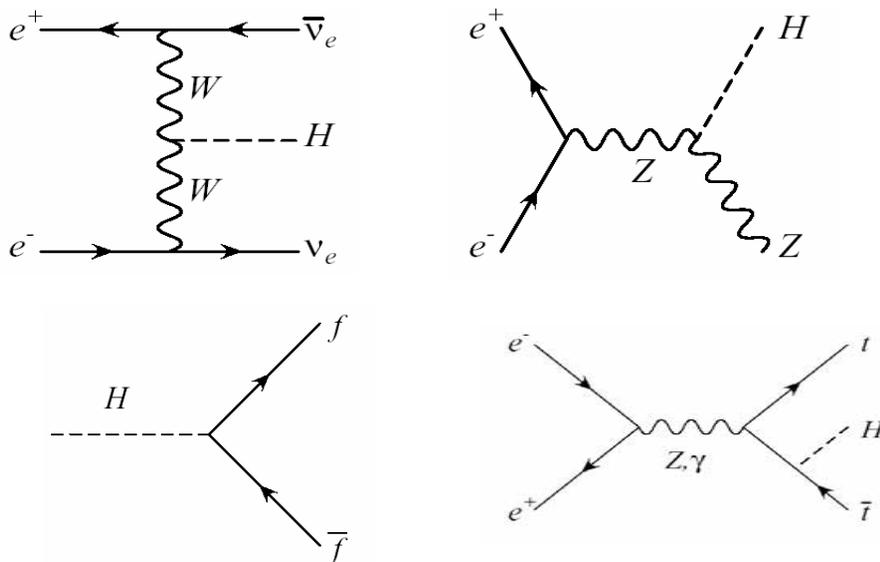
At LHC, a SM-like Higgs boson can be discovered independent of its mass.

## Higgs discovery at ATLAS

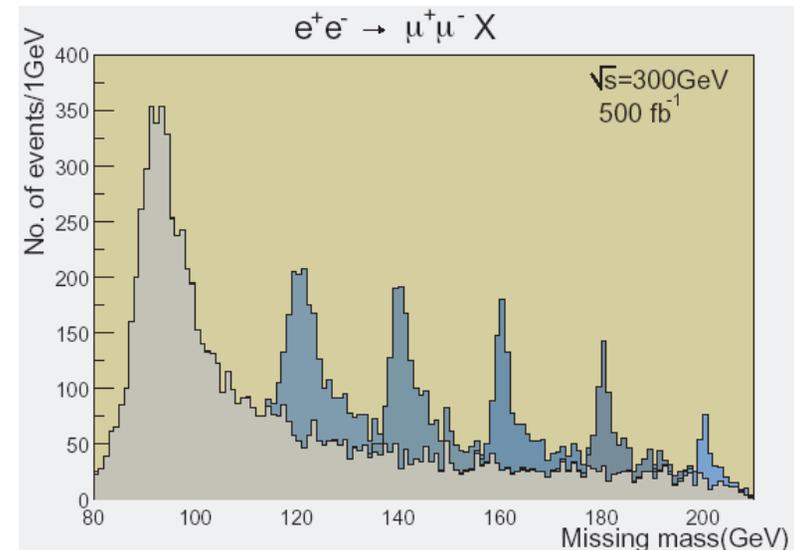


# Higgs physics at LC

- Determination of spin and parity.
- Precise mass determination .  
( $\delta m_H \sim 40$  MeV for  $m_H = 120$  GeV)
- Detection of the Higgs boson independent of its decay property.  
(Recoil mass distribution in the HZ mode)
- **Coupling measurement**  
-> Mass generation mechanism of elementary particles.



TESLA TDR



GLC report

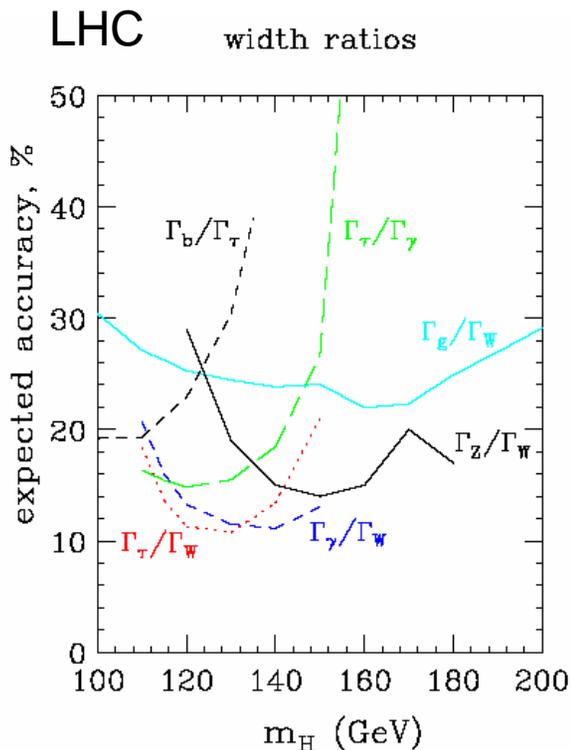
# Higgs coupling measurement

LHC: O(10%) measurements for some ratios of coupling constants.

LC: O(1%) determination for various coupling constants.

LC

Precision of coupling determination  
 $m_H=120$  GeV, 500/fb



$\sqrt{s}$	300 GeV	400 GeV	500 GeV
$\Delta m_{th}$ (lepton-only)	80 MeV	—	—
$\Delta m_{th}$	40 MeV	—	—
$\Delta\sigma/\sigma$ (lepton-only)	2.1%	2.5%	2.9%
$\Delta\sigma/\sigma$	1.3%	—	—
$\Delta(\sigma_h\text{-Br}(b\bar{b}))$	2.0%	—	—
ZZH-coupling $\Delta ZZH/ZZH$	1.1%	1.3%	1.5%
WWH-coupling $\Delta WWH/WWH$	1.6%	—	—
$\Delta\Gamma_{h^0}/\Gamma_{h^0}$	5.5%	12%	16%
Yukawa coupling $\Delta\lambda/\lambda$			
$\lambda_b$	2.8%	6.1%	8.1%
$\lambda_\tau$	3.5%	—	—
$\lambda_c$	11.3%	13%	15%
$\lambda_b/\lambda_\tau$	2.3%	—	—
$\lambda_b/\lambda_c$	11%	12%	14%
$\lambda_{up\text{-type}}$	4.1%	—	—
$\lambda_{down\text{-type}}/\lambda_{up\text{-type}}$	3.2%	—	—
$\Delta(\sigma\text{-Br})/(\sigma\text{-Br})$			
$h^0 \rightarrow b\bar{b}$	1.1%	1.3%	1.7%
$h^0 \rightarrow W^+W^-$	5.1%	12%	16%
$h^0 \rightarrow \tau^+\tau^-$	4.4%	—	—
$h^0 \rightarrow c\bar{c}+gg$	6.3%	—	—
$h^0 \rightarrow c\bar{c}$	22%	23%	27%
$h^0 \rightarrow gg$	10%	11%	13%
$h^0 \rightarrow \gamma\gamma$	—	—	—
$h^0 \rightarrow Z^0\gamma$	—	—	—

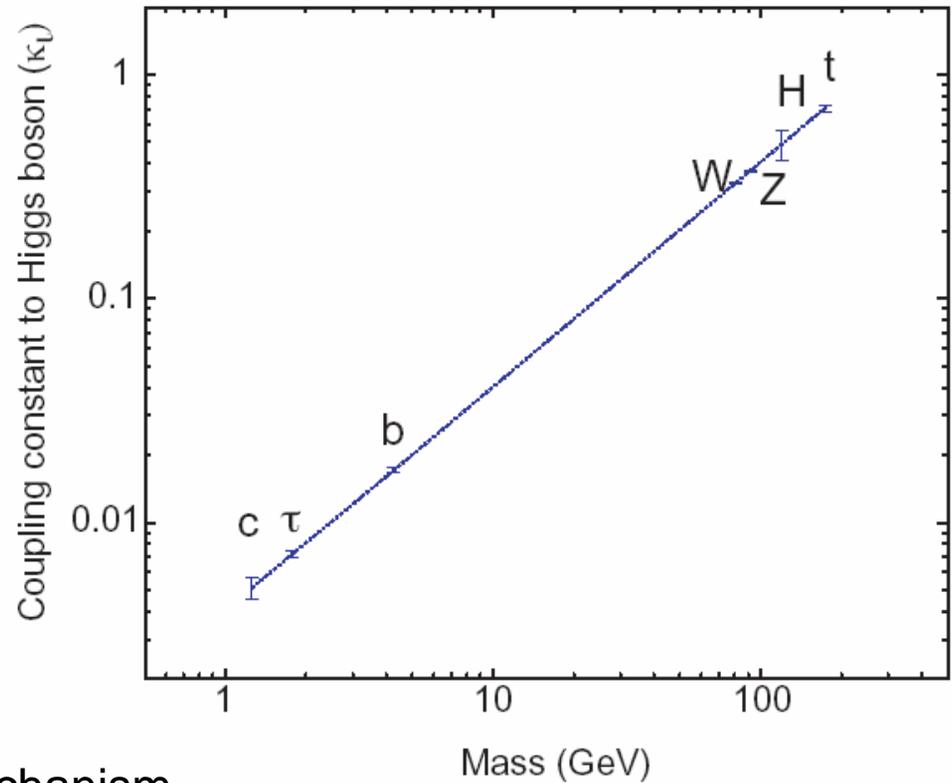
# Coupling Mass relation

Coupling-Mass Relation GLC Report

Particle mass

$$m_i = v \times \kappa_i$$

Higgs coupling constant



Establish the mass generation mechanism

LC:300 – 700 GeV

# Implication of the branching ratio measurements for MSSM

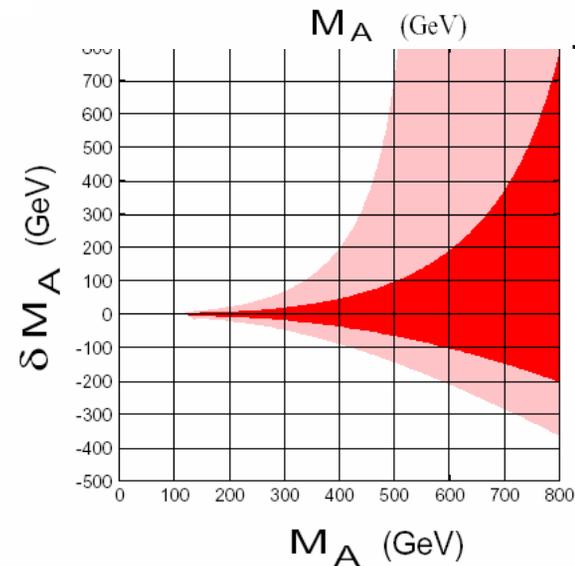
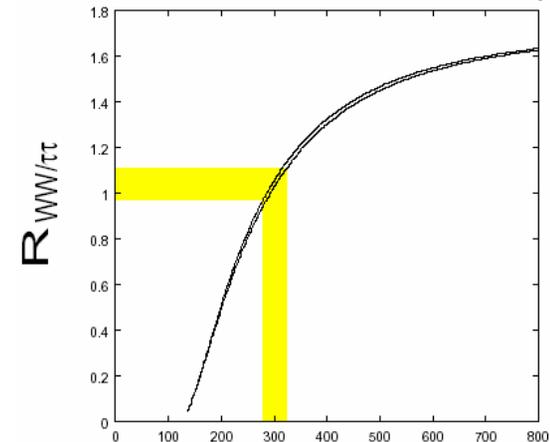
ACFA report 2001

In the MSSM, the ratio of the branching ratios like  $B(h \rightarrow cc)/B(h \rightarrow bb)$  is useful to constrain the SUSY parameter, especially the heavy Higgs boson mass.

(Kamoshita-Okada-Tanaka, 1995)

$$\begin{aligned}
 R_{cc+gg/\tau\tau} &\equiv \frac{B(h \rightarrow c\bar{c}) + B(h \rightarrow gg)}{B(h \rightarrow \tau\bar{\tau})} \\
 &\approx \left( \frac{m_A^2 - m_h^2}{m_A^2 + m_Z^2} \right)^2 R_{cc+gg/\tau\tau}(SM) \\
 R_{WW/\tau\tau} &\equiv B(h \rightarrow W^{(*)}W^{(*)})/B(h \rightarrow \tau\bar{\tau}) \\
 &\approx \left( \frac{m_A^2 - m_h^2}{m_A^2 + m_Z^2} \right)^2 R_{WW/\tau\tau}(SM)
 \end{aligned}$$

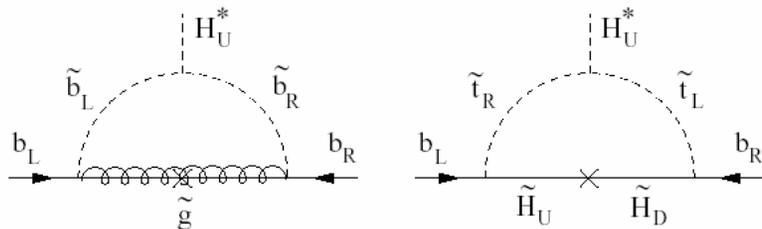
This is particularly important when LHC and the first stage of LC find the only one Light SUSY Higgs boson.



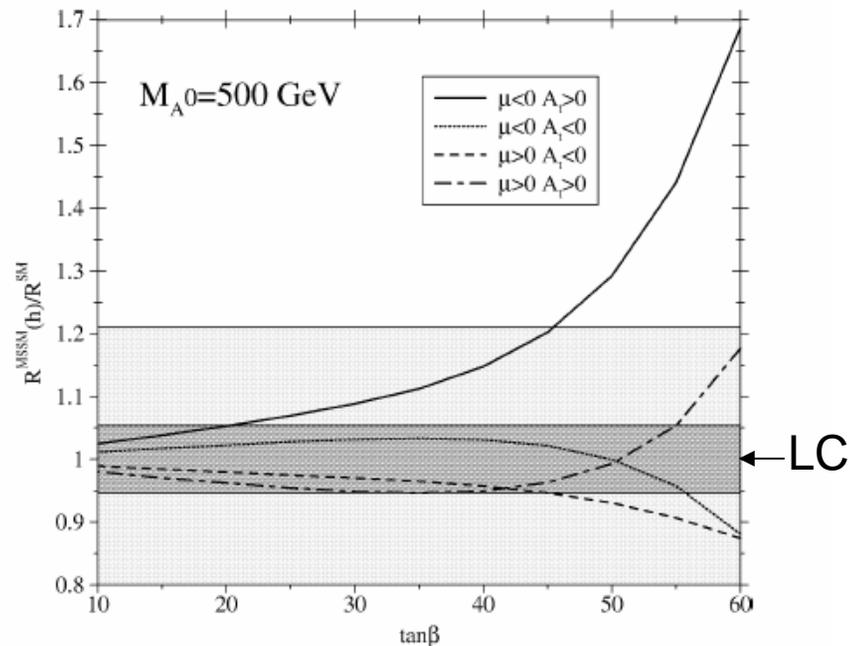
Dark region = LC  
Light region = LHC

# SUSY loop contributions to the $hbb$ Yukawa coupling

$B(h \rightarrow bb)/B(h \rightarrow \tau\tau)$  is sensitive to the SUSY loop correction to the bottom Yukawa coupling for a large  $\tan\beta$  region.



$B(h \rightarrow bb)/B(h \rightarrow \tau\tau)$  normalized by SM value



K.S.Babu, C.Kolda:  
M.Carena, D.Garcia, U.Nierste, C.E.M.Wagner

$$M_{\tilde{g}} = M_{\tilde{b}_1} = M_{\tilde{t}_1} = M_{\tilde{\tau}_1} = M_2 = |\mu| = A_b \\ = A_\tau = |A_t| = 1.5 \text{ TeV},$$

J.Guasch, W.Hollik, S.Penaranda

# SUSY Higgs sector

Two Higgs doublet model

$\tan \beta$  (vacuum angle)

$$m_h = f(m_A, \tan \beta, m_t, m_{\tilde{t}}, \dots)$$

Determination of  $\tan \beta$  from:  
 mass formula,  
 heavy Higgs decay branching,  
 stau decay,  
 chargino-neutralino sector...



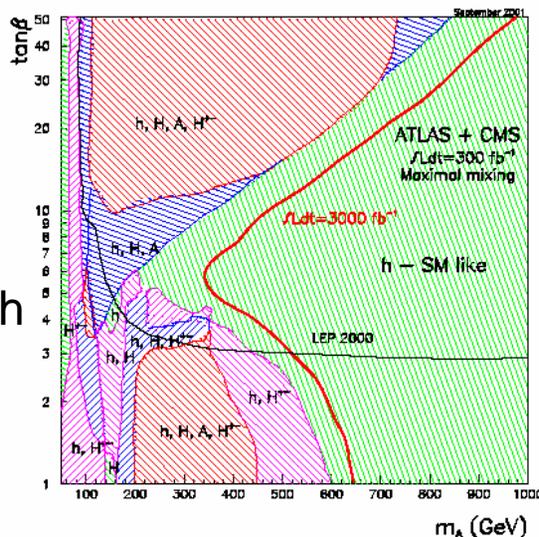
EW gauge interaction

$\sin \theta_W$  (gauge boson mixing angle)

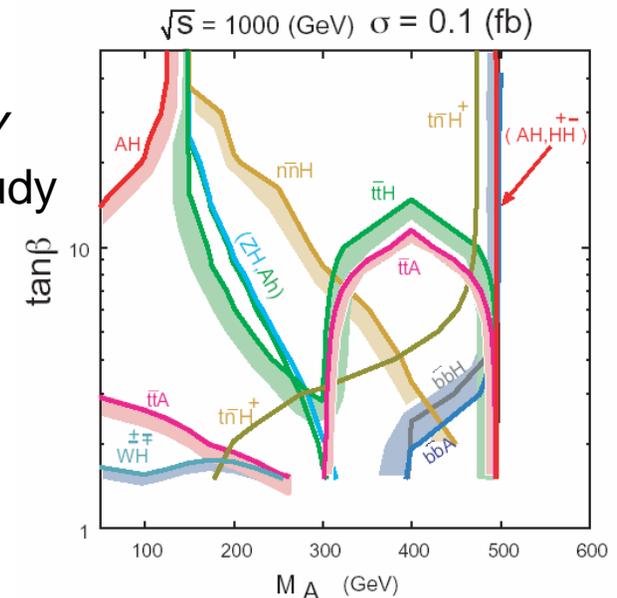
$\rho$ -parameter

Determination of  $\sin \theta_W$  from  
 various EW processes (LEP, SLC).

LHC SUSY  
 Higgs search

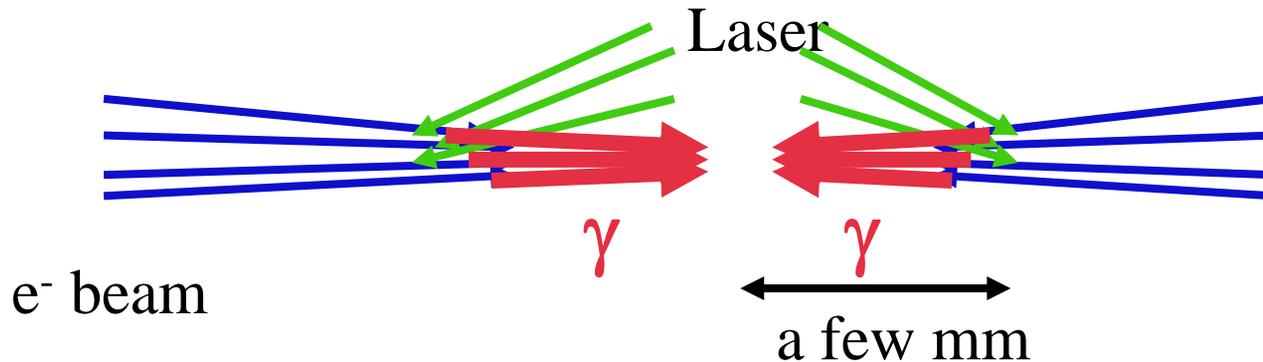


LC SUSY  
 Higgs study

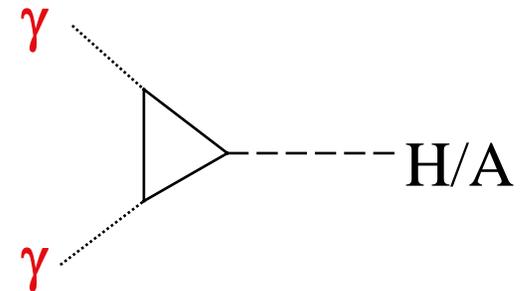


S.Kiyoura et al, GLC report

# Photon-photon collider



- ILC can have an additional interaction point with photon-photon collisions.
- The heavy Higgs boson can be produced up to 400 GeV for 500 GeV LC.
- CP properties of the heavy Higgs boson can be studied.

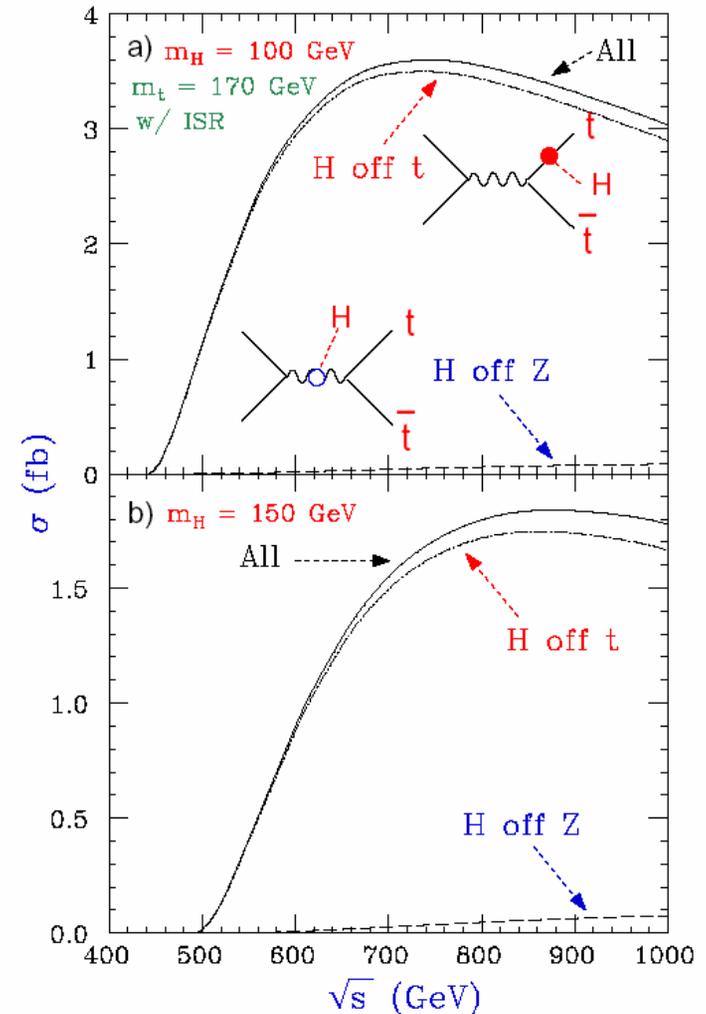


# Top Yukawa coupling

Determination of the top Yukawa coupling constants requires a higher energy. ( $E_{cm} > 700$  GeV)

The top Yukawa coupling is determined at 4-5% accuracy for  $m_H=120$  GeV and  $L_{int}=500/\text{fb}$  at  $E_{cm}=700$  GeV

-> Energy upgrade of LC



ACFA report, 2001

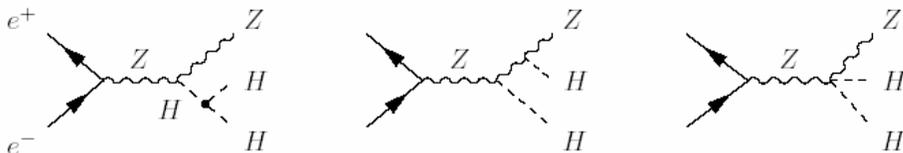
# Higgs self-coupling constant

- Determination of the Higgs potential is one of the most fundamental issues. Origin of the electroweak symmetry breaking.
- Double Higgs boson production at LC will be the first access to the Higgs potential.
- New physics effects may appear in the Higgs self-coupling constant.

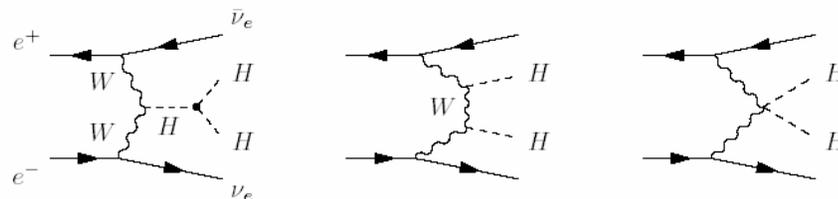
# Higgs self-coupling measurement at LC

Two production processes. The WW fusion process is more important for a higher energy.

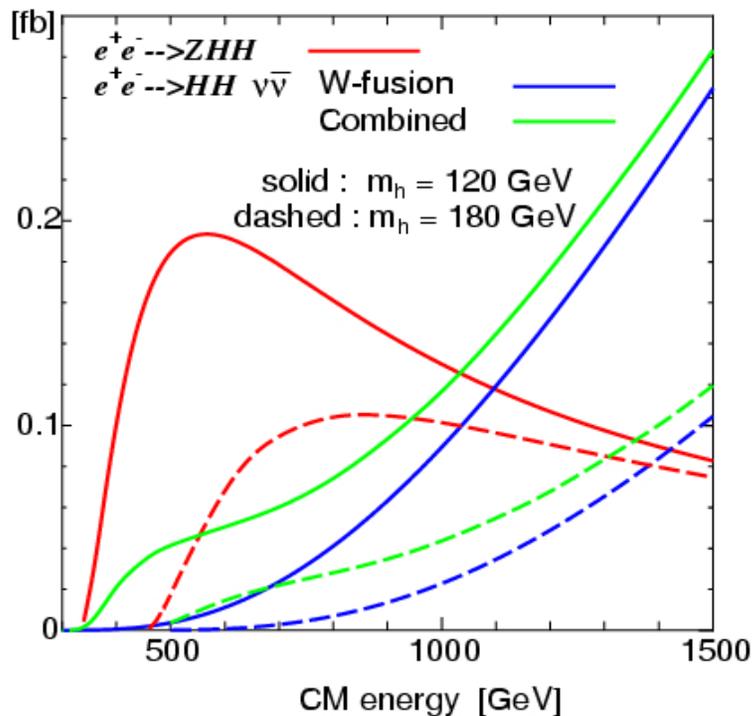
$$e^+e^- \rightarrow ZHH$$



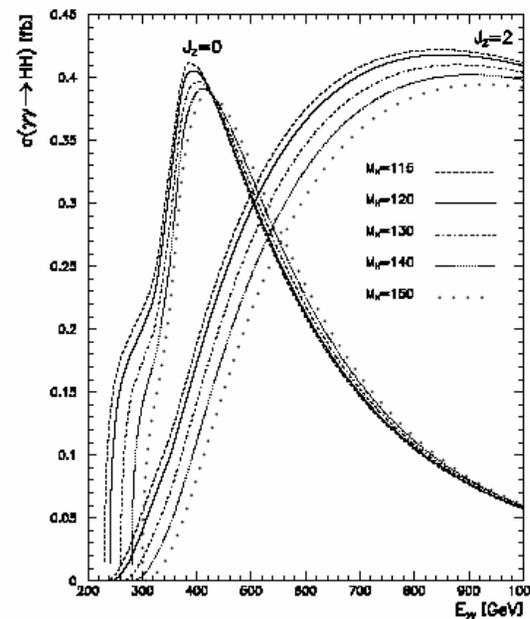
$$e^+e^- \rightarrow \nu\bar{\nu}HH$$



total cross section



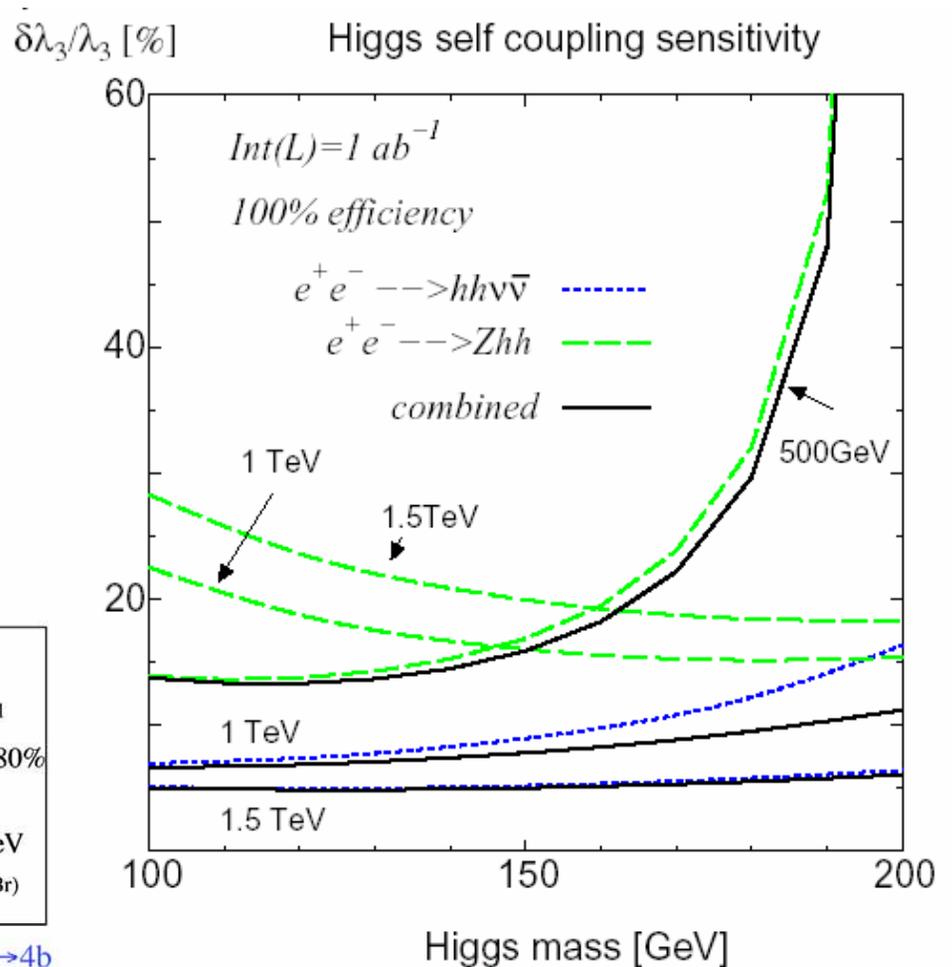
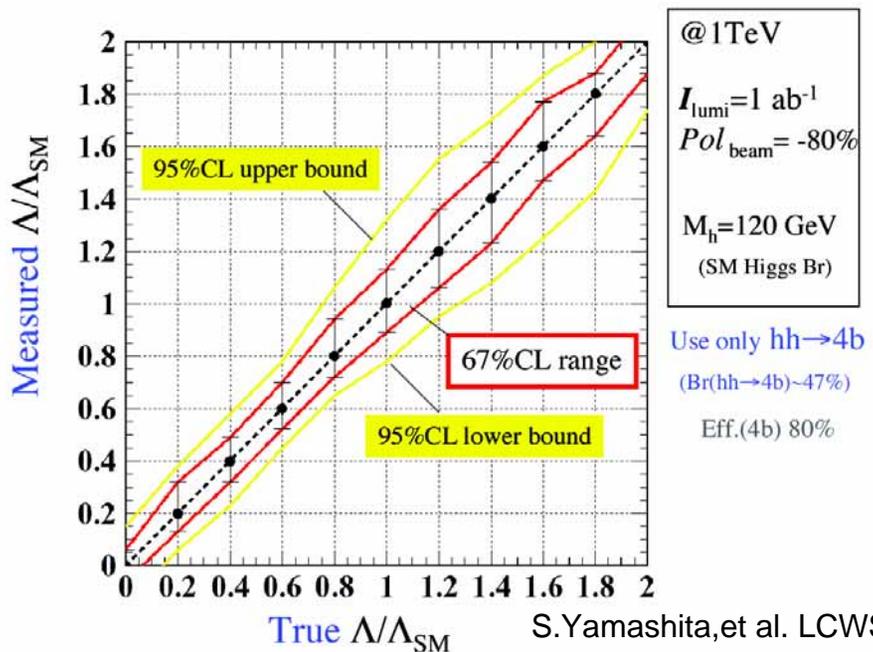
$$\gamma\gamma \rightarrow HH$$



- Meaningful measurement of the self-coupling at 500 GeV from the Zhh process (and  $\gamma\gamma$  collider option).
- For precise determination, the collider energy should be 1 TeV and more.

->Energy upgrade of LC.

~20 % determination with 1/fab at Ecm=500 GeV for mh=120 GeV,  
 ~10% with 1/ab at 1TeV



ACFA Higgs WG, Y.Yasui, et.al.

# Electroweak baryogenesis and quantum corrections to the hhh coupling in 2HDM

- Baryogenesis: Explain baryon-to-photon ratio from zero baryon number.  $n_B/s \sim 10^{-10}$
- A basic fact: B+L violation at high temperature in the SM.
- Two scenarios:
  - (1) B-L generation above the EW phase transition (leptogenesis, etc).
  - (2) Baryogenesis at the EW phase transition.
- EW baryogenesis is difficult in the minimal SM.
- 2HDM is a simple viable model. A.Nelson, D.B.Kaplan, A.G.Cohen, 91, M.Joyce, T.Prokopec, and N.Turok 91; J.M.Cline, K.Kainulainen, A.P.Vischer, 96

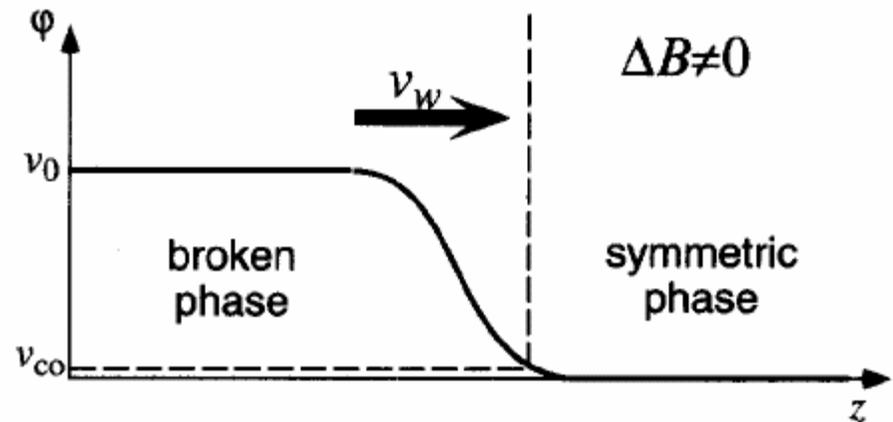
Connection between collider physics and cosmology

$$V_{eff}(\phi) \leftrightarrow V_T(\phi, T)$$

# Baryon number generation at the electroweak phase transition

- Strong first order phase transition.
- Expansion of a bubble wall.
- Charge flow of fermions due to CP violation at the wall.
- Baryon number violation in the symmetric phase.

In the minimal SM, the phase transition is not strong first order, and CP violation from the Kobayashi-Maskawa phase is too small.

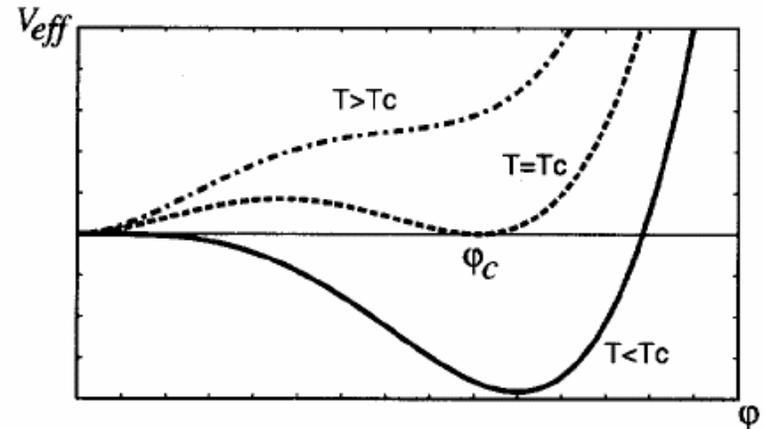


# Conditions for successful baryogenesis

## Strong first order phase transition.

Not to erase the baryon number after transition by sphaleron process.

$$\phi_c/T_c > 1$$



In the high temperature expansion ( $M=0$ ),

$$V_T(\phi, T) = D(T^2 - T_0^2)\phi^2 - ET\phi^3 + \frac{\lambda_T}{4}\phi^4 + \dots$$

$$E = \frac{1}{12\pi v^3} (6m_W^3 + 3m_Z^3 + m_h^3 + m_H^3 + m_A^3 + 2m_{H^\pm}^3)$$

$$\phi_c/T_c = 2E/\lambda_{T_c}$$

## Strong first order phase transition

<-> “Non-decoupling” effects of heavy Higgs bosons

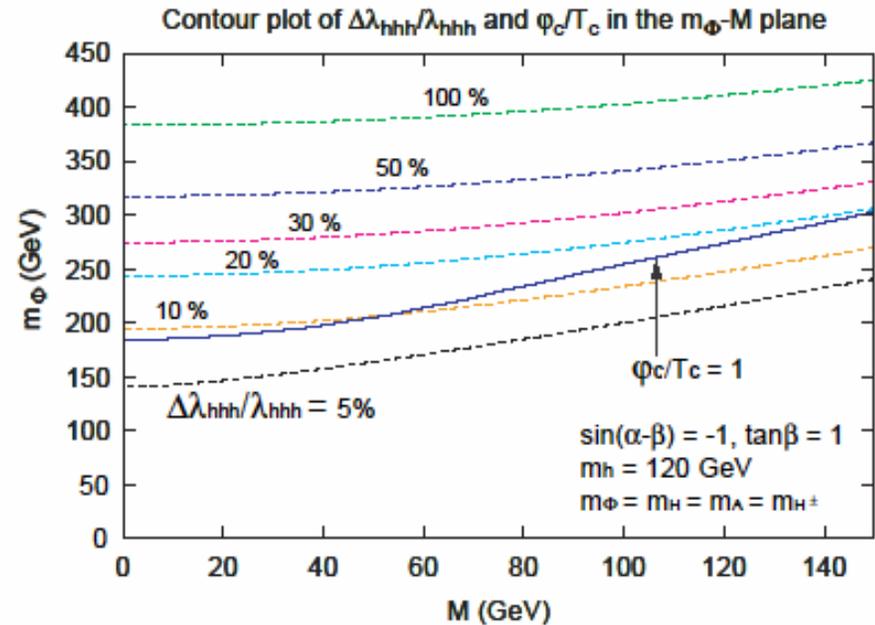
<-> Correlation with a large corrections to the hhh coupling at zero temperature

# Numerical calculation

S.Kanemura, Y.Okada, E.Senaha

We calculate the finite temperature effective potential without the high temperature expansion for  $M > 0$ .

We also study the loop correction to the hhh coupling constant.



$$\Delta\lambda_{hhh}/\lambda_{hhh} \gtrsim 10\%$$

for successful electroweak baryogenesis

$$m_\Phi^2 \simeq M^2 + \lambda_i v^2$$

Correlation between zero temperature and finite temperature potential.  
 Connection between cosmology and collider signals.

# Summary 2

- The coupling measurement is essential for establishing the Higgs mechanism. ILC is necessary for this purpose.
- Coupling determination can also provide information on physics beyond the SM.
- Information on the Higgs potential will be obtained by the double Higgs boson production at ILC. We may be able to know physics at the electroweak phase transition.